

glucat

0.8.2

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# Chapter 1

## Namespace Index

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## Chapter 5

# Namespace Documentation

### 5.1 cga3 Namespace Reference

Definitions for 3D Conformal Geometric Algebra [DL].

#### Functions

- `template<typename Multivector_T >`  
`Multivector_T cga3 (const Multivector_T &x)`  
*Convert Euclidean 3D vector to Conformal Geometric Algebra null vector [DL (10.50)].*
- `template<typename Multivector_T >`  
`Multivector_T cga3std (const Multivector_T &X)`  
*Convert CGA3 null vector to standard Conformal Geometric Algebra null vector [DL (10.52)].*
- `template<typename Multivector_T >`  
`Multivector_T agc3 (const Multivector_T &X)`  
*Convert CGA3 null vector to Euclidean 3D vector [DL (10.50)].*

#### 5.1.1 Detailed Description

Definitions for 3D Conformal Geometric Algebra [DL].

#### 5.1.2 Function Documentation

##### 5.1.2.1 agc3()

```
template<typename Multivector_T >
Multivector_T cga3::agc3 (
    const Multivector_T & X ) [inline]
```

Convert CGA3 null vector to Euclidean 3D vector [DL (10.50)].

Definition at line 138 of file PyClical.h.

References `cga3std()`, `PyClical::cl`, and `PyClical::ist`.

### 5.1.2.2 cga3()

```
template<typename Multivector_T >
Multivector_T cga3::cga3 (
    const Multivector_T & x ) [inline]
```

Convert Euclidean 3D vector to Conformal Geometric Algebra null vector [DL (10.50)].

Definition at line 115 of file PyClical.h.

References `PyClical::cl`, `PyClical::ist`, and `PyClical::ninf3`.

### 5.1.2.3 cga3std()

```
template<typename Multivector_T >
Multivector_T cga3::cga3std (
    const Multivector_T & X ) [inline]
```

Convert CGA3 null vector to standard Conformal Geometric Algebra null vector [DL (10.52)].

Definition at line 126 of file PyClical.h.

References `PyClical::cl`, `PyClical::ist`, and `PyClical::ninf3`.

Referenced by `agc3()`.

## 5.2 glucat Namespace Reference

### Namespaces

- [gen](#)
- [matrix](#)
- [timing](#)

### Classes

- class [basis\\_table](#)  
*Table of basis elements used as a cache by `basis_element()`*
- class [bool\\_to\\_type](#)  
*Bool to type.*
- class [clifford\\_algebra](#)  
*`clifford_algebra<>` declares the operations of a Clifford algebra*
- class [compare\\_types](#)  
*Type comparison.*
- class [compare\\_types< T, T >](#)
- class [control\\_t](#)  
*Parameters to control tests.*
- struct [CTAssertion](#)

- *Compile time assertion.*
- struct [CTAssertion< true >](#)
- class [error](#)
- *Specific exception class.*
- class [framed\\_multi](#)
- *A framed\_multi<Scalar\_T,LO,HI> is a framed approximation to a multivector.*
- class [glucat\\_error](#)
- *Abstract exception class.*
- class [index\\_set](#)
- *Index set class based on std::bitset<> in Gnu standard C++ library.*
- class [index\\_set\\_hash](#)
- class [matrix\\_multi](#)
- *A matrix\_multi<Scalar\_T,LO,HI> is a matrix approximation to a multivector.*
- class [numeric\\_traits](#)
- *Extra traits which extend numeric limits.*
- class [random\\_generator](#)
- *Random number generator with single instance per Scalar\_T.*
- class [sorted\\_range](#)
- *Sorted range for use with output.*
- class [sorted\\_range< Sorted\\_Map\\_T, Sorted\\_Map\\_T >](#)
- struct [tuning](#)
- *Tuning policy.*

## Typedefs

- typedef int [index\\_t](#)
- *Size of index\_t should be enough to represent LO, HI.*
- typedef unsigned long [set\\_value\\_t](#)
- *Size of set\_value\_t should be enough to contain index\_set<LO,HI>*
- typedef int(\* [intfn](#)) ()
- *For exception catching: pointer to function returning int.*
- typedef int(\* [intintfn](#)) (int)
- *For exception catching: pointer to function of int returning int.*

## Enumerations

- enum [precision\\_t](#) { [precision\\_demoted](#), [precision\\_same](#), [precision\\_promoted](#) }
- *Precision policy.*

## Functions

- template<template< typename, const index\_t, const index\_t > class Multivector, template< typename, const index\_t, const index\_t > class RHS, typename Scalar\_T , const index\_t LO, const index\_t HI>  
bool [operator!=](#) (const Multivector< Scalar\_T, LO, HI > &lhs, const RHS< Scalar\_T, LO, HI > &rhs)
- *Test for inequality of multivectors.*
- template<template< typename, const index\_t, const index\_t > class Multivector, typename Scalar\_T , const index\_t LO, const index\_t HI>  
bool [operator!=](#) (const Multivector< Scalar\_T, LO, HI > &lhs, const Scalar\_T &scr)
- *Test for inequality of multivector and scalar.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`bool operator!= (const Scalar_T &scr, const Multivector< Scalar_T, LO, HI > &rhs)`  
*Test for inequality of scalar and multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > operator+ (const Multivector< Scalar_T, LO, HI > &lhs, const Scalar_T &scr)`  
*Geometric sum of multivector and scalar.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > operator+ (const Scalar_T &scr, const Multivector< Scalar_T, LO, HI > &rhs)`  
*Geometric sum of scalar and multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > operator+ (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`  
*Geometric sum.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > operator- (const Multivector< Scalar_T, LO, HI > &lhs, const Scalar_T &scr)`  
*Geometric difference of multivector and scalar.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > operator- (const Scalar_T &scr, const Multivector< Scalar_T, LO, HI > &rhs)`  
*Geometric difference of scalar and multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > operator- (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`  
*Geometric difference.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > operator* (const Multivector< Scalar_T, LO, HI > &lhs, const Scalar_T &scr)`  
*Product of multivector and scalar.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > operator* (const Scalar_T &scr, const Multivector< Scalar_T, LO, HI > &rhs)`  
*Product of scalar and multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > operator* (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`  
*Geometric product.*
- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > operator^ (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`  
*Outer product.*

- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > operator & (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`  
*Inner product.*
- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > operator% (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`  
*Left contraction.*
- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`Scalar_T star (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`  
*Hestenes scalar product.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > operator/ (const Multivector< Scalar_T, LO, HI > &lhs, const Scalar_T &scr)`  
*Quotient of multivector and scalar.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > operator/ (const Scalar_T &scr, const Multivector< Scalar_T, LO, HI > &rhs)`  
*Quotient of scalar and multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > operator/ (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`  
*Geometric quotient.*
- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > operator| (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`  
*Transformation via twisted adjoint action.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > inv (const Multivector< Scalar_T, LO, HI > &val)`  
*Geometric multiplicative inverse.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > pow (const Multivector< Scalar_T, LO, HI > &lhs, int rhs)`  
*Integer power of multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > pow (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`  
*Multivector power of multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > outer\_pow (const Multivector< Scalar_T, LO, HI > &lhs, int rhs)`  
*Outer product power of multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`Scalar_T scalar (const Multivector< Scalar_T, LO, HI > &val)`  
*Scalar part.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`Scalar_T real (const Multivector< Scalar_T, LO, HI > &val)`  
*Real part: synonym for scalar part.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`Scalar_T imag (const Multivector< Scalar_T, LO, HI > &val)`  
*Imaginary part: deprecated (always 0)*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > pure (const Multivector< Scalar_T, LO, HI > &val)`  
*Pure part.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > even (const Multivector< Scalar_T, LO, HI > &val)`  
*Even part.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > odd (const Multivector< Scalar_T, LO, HI > &val)`  
*Odd part.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const std::vector< Scalar_T > vector_part (const Multivector< Scalar_T, LO, HI > &val)`  
*Vector part of multivector, as a vector\_t with respect to frame()*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > involute (const Multivector< Scalar_T, LO, HI > &val)`  
*Main involution, each {i} is replaced by -{i} in each term, eg. {1}\*{2} -> (-{2})\*(-{1})*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > reverse (const Multivector< Scalar_T, LO, HI > &val)`  
*Reversion, eg. {1}\*{2} -> {2}\*{1}.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > conj (const Multivector< Scalar_T, LO, HI > &val)`  
*Conjugation, rev o invo == invo o rev.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`Scalar_T quad (const Multivector< Scalar_T, LO, HI > &val)`  
*Scalar\_T quadratic form == (rev(x)\*x)(0)*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`Scalar_T norm (const Multivector< Scalar_T, LO, HI > &val)`  
*Scalar\_T norm == sum of norm of coordinates.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`Scalar_T abs (const Multivector< Scalar_T, LO, HI > &val)`  
*Absolute value == sqrt(norm)*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`Scalar_T max_abs (const Multivector< Scalar_T, LO, HI > &val)`  
*Maximum of absolute values of components of multivector: multivector infinity norm.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > complexifier (const Multivector< Scalar_T, LO, HI > &val)`

*Square root of -1 which commutes with all members of the frame of the given multivector.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > elliptic (const Multivector< Scalar_T, LO, HI > &val)`
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > sqrt (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)`

*Square root of multivector with specified complexifier.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > sqrt (const Multivector< Scalar_T, LO, HI > &val)`

*Square root of multivector.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > clifford\_exp (const Multivector< Scalar_T, LO, HI > &val)`

*Exponential of multivector.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > log (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)`

*Natural logarithm of multivector with specified complexifier.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > log (const Multivector< Scalar_T, LO, HI > &val)`

*Natural logarithm of multivector.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > cos (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)`

*Cosine of multivector with specified complexifier.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > cos (const Multivector< Scalar_T, LO, HI > &val)`

*Cosine of multivector.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > acos (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)`

*Inverse cosine of multivector with specified complexifier.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > acos (const Multivector< Scalar_T, LO, HI > &val)`

*Inverse cosine of multivector.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > cosh (const Multivector< Scalar_T, LO, HI > &val)`

*Hyperbolic cosine of multivector.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > acosh (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)`

*Inverse hyperbolic cosine of multivector with specified complexifier.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > acosh (const Multivector< Scalar_T, LO, HI > &val)`  
*Inverse hyperbolic cosine of multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > sin (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)`  
*Sine of multivector with specified complexifier.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > sin (const Multivector< Scalar_T, LO, HI > &val)`  
*Sine of multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > asin (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)`  
*Inverse sine of multivector with specified complexifier.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > asin (const Multivector< Scalar_T, LO, HI > &val)`  
*Inverse sine of multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > sinh (const Multivector< Scalar_T, LO, HI > &val)`  
*Hyperbolic sine of multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > asinh (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)`  
*Inverse hyperbolic sine of multivector with specified complexifier.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > asinh (const Multivector< Scalar_T, LO, HI > &val)`  
*Inverse hyperbolic sine of multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > tan (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)`  
*Tangent of multivector with specified complexifier.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > tan (const Multivector< Scalar_T, LO, HI > &val)`  
*Tangent of multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > atan (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)`  
*Inverse tangent of multivector with specified complexifier.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > atan (const Multivector< Scalar_T, LO, HI > &val)`  
*Inverse tangent of multivector.*

- template<template< typename, const index\_t, const index\_t > class Multivector, typename Scalar\_T , const index\_t LO, const index\_t HI>  
 const Multivector< Scalar\_T, LO, HI > [tanh](#) (const Multivector< Scalar\_T, LO, HI > &val)  
*Hyperbolic tangent of multivector.*
- template<template< typename, const index\_t, const index\_t > class Multivector, typename Scalar\_T , const index\_t LO, const index\_t HI>  
 const Multivector< Scalar\_T, LO, HI > [atanh](#) (const Multivector< Scalar\_T, LO, HI > &val, const Multivector< Scalar\_T, LO, HI > &i, const bool prechecked=false)  
*Inverse hyperbolic tangent of multivector with specified complexifier.*
- template<template< typename, const index\_t, const index\_t > class Multivector, typename Scalar\_T , const index\_t LO, const index\_t HI>  
 const Multivector< Scalar\_T, LO, HI > [atanh](#) (const Multivector< Scalar\_T, LO, HI > &val)  
*Inverse hyperbolic tangent of multivector.*
- template<template< typename, const index\_t, const index\_t > class Multivector, template< typename, const index\_t, const index\_t > class RHS, typename Scalar\_T , const index\_t LO, const index\_t HI>  
 const Multivector< Scalar\_T, LO, HI > [operator &](#) (const Multivector< Scalar\_T, LO, HI > &lhs, const RHS< Scalar\_T, LO, HI > &rhs)  
*Inner product.*
- template<template< typename, const index\_t, const index\_t > class Multivector, typename Scalar\_T , const index\_t LO, const index\_t HI>  
 static void [check\\_complex](#) (const Multivector< Scalar\_T, LO, HI > &val, const Multivector< Scalar\_T, LO, HI > &i, const bool prechecked=false)  
*Check that i is a valid complexifier for val.*
- template<typename Scalar\_T , const index\_t LO, const index\_t HI>  
 const [framed\\_multi](#)< Scalar\_T, LO, HI > [operator\\*](#) (const [framed\\_multi](#)< Scalar\_T, LO, HI > &lhs, const [framed\\_multi](#)< Scalar\_T, LO, HI > &rhs)  
*Geometric product.*
- template<typename Scalar\_T , const index\_t LO, const index\_t HI>  
 const [framed\\_multi](#)< Scalar\_T, LO, HI > [operator^](#) (const [framed\\_multi](#)< Scalar\_T, LO, HI > &lhs, const [framed\\_multi](#)< Scalar\_T, LO, HI > &rhs)  
*Outer product.*
- template<typename Scalar\_T , const index\_t LO, const index\_t HI>  
 const [framed\\_multi](#)< Scalar\_T, LO, HI > [operator &](#) (const [framed\\_multi](#)< Scalar\_T, LO, HI > &lhs, const [framed\\_multi](#)< Scalar\_T, LO, HI > &rhs)  
*Inner product.*
- template<typename Scalar\_T , const index\_t LO, const index\_t HI>  
 const [framed\\_multi](#)< Scalar\_T, LO, HI > [operator%](#) (const [framed\\_multi](#)< Scalar\_T, LO, HI > &lhs, const [framed\\_multi](#)< Scalar\_T, LO, HI > &rhs)  
*Left contraction.*
- template<typename Scalar\_T , const index\_t LO, const index\_t HI>  
 Scalar\_T [star](#) (const [framed\\_multi](#)< Scalar\_T, LO, HI > &lhs, const [framed\\_multi](#)< Scalar\_T, LO, HI > &rhs)  
*Hestenes scalar product.*
- template<typename Scalar\_T , const index\_t LO, const index\_t HI>  
 const [framed\\_multi](#)< Scalar\_T, LO, HI > [operator/](#) (const [framed\\_multi](#)< Scalar\_T, LO, HI > &lhs, const [framed\\_multi](#)< Scalar\_T, LO, HI > &rhs)  
*Geometric quotient.*
- template<typename Scalar\_T , const index\_t LO, const index\_t HI>  
 const [framed\\_multi](#)< Scalar\_T, LO, HI > [operator|](#) (const [framed\\_multi](#)< Scalar\_T, LO, HI > &lhs, const [framed\\_multi](#)< Scalar\_T, LO, HI > &rhs)  
*Transformation via twisted adjoint action.*
- template<typename Scalar\_T , const index\_t LO, const index\_t HI>  
 std::istream & [operator>>](#) (std::istream &s, [framed\\_multi](#)< Scalar\_T, LO, HI > &val)  
*Read multivector from input.*
- template<typename Scalar\_T , const index\_t LO, const index\_t HI>  
 std::ostream & [operator<<](#) (std::ostream &os, const [framed\\_multi](#)< Scalar\_T, LO, HI > &val)

*Write multivector to output.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>  
std::ostream & operator<< (std::ostream &os, const std::pair< const index_set< LO, HI >, Scalar_T > &term)`

*Write term to output.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>  
const framed_multi< Scalar_T, LO, HI > exp (const framed_multi< Scalar_T, LO, HI > &val)`

*Exponential of multivector.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>  
static Scalar_T crd_of_mult (const std::pair< const index_set< LO, HI >, Scalar_T > &lhs, const std::pair< const index_set< LO, HI >, Scalar_T > &rhs)`

*Coordinate of product of terms.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>  
const std::pair< const index_set< LO, HI >, Scalar_T > operator* (const std::pair< const index_set< LO, HI >, Scalar_T > &lhs, const std::pair< const index_set< LO, HI >, Scalar_T > &rhs)`

*Product of terms.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>  
const framed_multi< Scalar_T, LO, HI > sqrt (const framed_multi< Scalar_T, LO, HI > &val, const framed_multi< Scalar_T, LO, HI > &i, bool prechecked)`

*Square root of multivector with specified complexifier.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>  
const framed_multi< Scalar_T, LO, HI > log (const framed_multi< Scalar_T, LO, HI > &val, const framed_multi< Scalar_T, LO, HI > &i, bool prechecked)`

*Natural logarithm of multivector with specified complexifier.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>  
const framed_multi< Scalar_T, LO, HI > operator & (const framed_multi< Scalar_T, LO, HI > &lhs, const framed_multi< Scalar_T, LO, HI > &rhs)`

*Inner product.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>  
static Scalar_T crd_of_mult (const std::pair< const index_set< LO, HI >, Scalar_T > &lhs, const std::pair< const index_set< LO, HI >, Scalar_T > &rhs)`

*Coordinate of product of terms.*

- `_GLUCAT_CTAssert (std::numeric_limits< unsigned char >::radix==2, CannotDetermineBitsPerChar) const index_t BITS_PER_CHAR`

*If radix of unsigned char is not 2, we can't easily determine number of bits from sizeof.*

- `_GLUCAT_CTAssert ( _GLUCAT_BITS_PER_ULONG==BITS_PER_SET_VALUE, BitsPerULongDoesNotMatchSetValueT) const index_t DEFAULT_LO`

*Default lowest index in an index set.*

- `template<typename LHS_T , typename RHS_T >  
LHS_T pos_mod (LHS_T lhs, RHS_T rhs)`

*Modulo function which works reliably for lhs < 0.*

- `template<const index_t LO, const index_t HI>  
const index_set< LO, HI > operator^ (const index_set< LO, HI > &lhs, const index_set< LO, HI > &rhs)`

*Symmetric set difference: exclusive or.*

- `template<const index_t LO, const index_t HI>  
const index_set< LO, HI > operator & (const index_set< LO, HI > &lhs, const index_set< LO, HI > &rhs)`

*Set intersection: and.*

- `template<const index_t LO, const index_t HI>  
const index_set< LO, HI > operator| (const index_set< LO, HI > &lhs, const index_set< LO, HI > &rhs)`

*Set union: or.*

- `template<const index_t LO, const index_t HI>  
int compare (const index_set< LO, HI > &a, const index_set< LO, HI > &b)`

*"lexicographic compare" eg. {3,4,5} is less than {3,7,8}*

- `_GLUCAT_CTAssert` (`sizeof(set_value_t) >= sizeof(std::bitset< DEFAULT_HI-DEFAULT_LO >)`), Default↔  
`_index_set_too_big_for_value` template< const `index_t` LO  
*Size of set\_value\_t should be enough to contain bitset<DEFAULT\_HI-DEFAULT\_LO>*
- const `index_t` HI `std::ostream & operator<<` (`std::ostream &os`, const `index_set`< LO, HI > &ist)  
*Write out index set.*
- template<const `index_t` LO, const `index_t` HI>  
`std::istream & operator>>` (`std::istream &s`, `index_set`< LO, HI > &ist)  
*Read in index set.*
- int `sign_of_square` (`index_t` j)  
*Square of generator {j}.*
- template<const `index_t` LO, const `index_t` HI>  
`index_t min_neg` (const `index_set`< LO, HI > &ist)  
*Minimum negative index, or 0 if none.*
- template<const `index_t` LO, const `index_t` HI>  
`index_t max_pos` (const `index_set`< LO, HI > &ist)  
*Maximum positive index, or 0 if none.*
- template<const `index_t` LO, const `index_t` HI>  
`const index_set`< LO, HI > `operator &` (const `index_set`< LO, HI > &lhs, const `index_set`< LO, HI > &rhs)  
*Set intersection: and.*
- static unsigned long `inverse_reversed_gray` (unsigned long x)  
*Inverse reversed Gray code.*
- static unsigned long `inverse_gray` (unsigned long x)  
*Inverse Gray code.*
- template<typename `Scalar_T` , const `index_t` LO, const `index_t` HI>  
`const matrix_multi`< `Scalar_T`, LO, HI > `operator*` (const `matrix_multi`< `Scalar_T`, LO, HI > &lhs, const  
`matrix_multi`< `Scalar_T`, LO, HI > &rhs)  
*Geometric product.*
- template<typename `Scalar_T` , const `index_t` LO, const `index_t` HI>  
`const matrix_multi`< `Scalar_T`, LO, HI > `operator^` (const `matrix_multi`< `Scalar_T`, LO, HI > &lhs, const  
`matrix_multi`< `Scalar_T`, LO, HI > &rhs)  
*Outer product.*
- template<typename `Scalar_T` , const `index_t` LO, const `index_t` HI>  
`const matrix_multi`< `Scalar_T`, LO, HI > `operator &` (const `matrix_multi`< `Scalar_T`, LO, HI > &lhs, const  
`matrix_multi`< `Scalar_T`, LO, HI > &rhs)  
*Inner product.*
- template<typename `Scalar_T` , const `index_t` LO, const `index_t` HI>  
`const matrix_multi`< `Scalar_T`, LO, HI > `operator%` (const `matrix_multi`< `Scalar_T`, LO, HI > &lhs, const  
`matrix_multi`< `Scalar_T`, LO, HI > &rhs)  
*Left contraction.*
- template<typename `Scalar_T` , const `index_t` LO, const `index_t` HI>  
`Scalar_T star` (const `matrix_multi`< `Scalar_T`, LO, HI > &lhs, const `matrix_multi`< `Scalar_T`, LO, HI > &rhs)  
*Hestenes scalar product.*
- template<typename `Scalar_T` , const `index_t` LO, const `index_t` HI>  
`const matrix_multi`< `Scalar_T`, LO, HI > `operator/` (const `matrix_multi`< `Scalar_T`, LO, HI > &lhs, const  
`matrix_multi`< `Scalar_T`, LO, HI > &rhs)  
*Geometric quotient.*
- template<typename `Scalar_T` , const `index_t` LO, const `index_t` HI>  
`const matrix_multi`< `Scalar_T`, LO, HI > `operator|` (const `matrix_multi`< `Scalar_T`, LO, HI > &lhs, const  
`matrix_multi`< `Scalar_T`, LO, HI > &rhs)  
*Transformation via twisted adjoint action.*
- template<typename `Scalar_T` , const `index_t` LO, const `index_t` HI>  
`std::istream & operator>>` (`std::istream &s`, `matrix_multi`< `Scalar_T`, LO, HI > &val)  
*Read multivector from input.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`std::ostream & operator<< (std::ostream &os, const matrix\_multi< Scalar_T, LO, HI > &val)`  
*Write multivector to output.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const index\_set< LO, HI > reframe (const matrix\_multi< Scalar_T, LO, HI > &lhs, const matrix\_multi< Scalar_T, LO, HI > &rhs, matrix\_multi< Scalar_T, LO, HI > &lhs_reframed, matrix\_multi< Scalar_T, LO, HI > &rhs_reframed)`  
*Find a common frame for operands of a binary operator.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix\_multi< Scalar_T, LO, HI > sqrt (const matrix\_multi< Scalar_T, LO, HI > &val, const matrix\_multi< Scalar_T, LO, HI > &i, bool prechecked)`  
*Square root of multivector with specified complexifier.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix\_multi< Scalar_T, LO, HI > matrix\_sqrt (const matrix\_multi< Scalar_T, LO, HI > &val, const matrix\_multi< Scalar_T, LO, HI > &i)`  
*Square root of multivector with specified complexifier.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix\_multi< Scalar_T, LO, HI > log (const matrix\_multi< Scalar_T, LO, HI > &val, const matrix\_multi< Scalar_T, LO, HI > &i, bool prechecked)`  
*Natural logarithm of multivector with specified complexifier.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix\_multi< Scalar_T, LO, HI > matrix\_log (const matrix\_multi< Scalar_T, LO, HI > &val, const matrix\_multi< Scalar_T, LO, HI > &i)`  
*Natural logarithm of multivector with specified complexifier.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix\_multi< Scalar_T, LO, HI > exp (const matrix\_multi< Scalar_T, LO, HI > &val)`  
*Exponential of multivector.*
- `index\_t offset\_level (const index\_t p, const index\_t q)`  
*Determine the log2 dim corresponding to signature p, q.*
- `template<typename Matrix_Index_T , const index_t LO, const index_t HI>`  
`static Matrix_Index_T folded\_dim (const index\_set< LO, HI > &sub)`  
*Determine the matrix dimension of the fold of a subalegebra.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix\_multi< Scalar_T, LO, HI > operator & (const matrix\_multi< Scalar_T, LO, HI > &lhs, const matrix\_multi< Scalar_T, LO, HI > &rhs)`  
*Inner product.*
- `template<typename Multivector_T , typename Matrix_T , typename Basis_Matrix_T >`  
`static Multivector_T fast (const Matrix_T &X, index\_t level)`  
*Inverse generalized Fast Fourier Transform.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`static const matrix\_multi< Scalar_T, LO, HI > pade\_approx (const int array_size, const Scalar_T a[], const Scalar_T b[], const matrix\_multi< Scalar_T, LO, HI > &X)`  
*Pade' approximation.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`static void db\_step (matrix\_multi< Scalar_T, LO, HI > &M, matrix\_multi< Scalar_T, LO, HI > &Y)`  
*Single step of product form of Denman-Beavers square root iteration.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`static const matrix\_multi< Scalar_T, LO, HI > db\_sqrt (const matrix\_multi< Scalar_T, LO, HI > &val)`  
*Product form of Denman-Beavers square root iteration.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`static const matrix\_multi< Scalar_T, LO, HI > pade\_log (const matrix\_multi< Scalar_T, LO, HI > &val)`  
*Pade' approximation of log.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`static const matrix\_multi< Scalar_T, LO, HI > cascade\_log (const matrix\_multi< Scalar_T, LO, HI > &val)`

- Incomplete square root cascade and Pade' approximation of log.*

  - template<typename Scalar\_T >  
Scalar\_T [log2](#) (const Scalar\_T &x)

*Log base 2 of scalar.*
  - template<typename Scalar\_T >  
[numeric\\_traits](#)< Scalar\_T >::promoted::type [to\\_promote](#) (const Scalar\_T &val)

*Cast to promote.*
  - template<typename Scalar\_T >  
[numeric\\_traits](#)< Scalar\_T >::demoted::type [to\\_demote](#) (const Scalar\_T &val)

*Cast to demote.*
  - int [try\\_catch](#) (intfn f)

*Exception catching for functions returning int.*
  - int [try\\_catch](#) (intintfn f, int arg)

*Exception catching for functions of int returning int.*

## Variables

- const double [MS\\_PER\\_S](#) = 1000.0

*Timing constant: deprecated here - moved to [test/timing.h](#).*
- const [index\\_t](#) [BITS\\_PER\\_SET\\_VALUE](#) = std::numeric\_limits<[set\\_value\\_t](#)>::digits

*Number of bits in [set\\_value\\_t](#).*
- const [index\\_t](#) [DEFAULT\\_HI](#) = [index\\_t](#)([BITS\\_PER\\_SET\\_VALUE](#) / 2)

*Default highest index in an index set.*
- const double [DEFAULT\\_TRUNCATION](#) = std::numeric\_limits<float>::epsilon()

*Default for truncation.*
- const unsigned int [DEFAULT\\_Mult\\_Matrix\\_Threshold](#) = 8
- const unsigned int [DEFAULT\\_Div\\_Max\\_Steps](#) = 4
- const unsigned int [DEFAULT\\_Sqrt\\_Max\\_Steps](#) = 256
- const unsigned int [DEFAULT\\_Log\\_Max\\_Outer\\_Steps](#) = 256
- const unsigned int [DEFAULT\\_Log\\_Max\\_Inner\\_Steps](#) = 32
- const unsigned int [DEFAULT\\_Basis\\_Max\\_Count](#) = 12
- const unsigned int [DEFAULT\\_Fast\\_Size\\_Threshold](#) = 1 << 6
- const unsigned int [DEFAULT\\_Inv\\_Fast\\_Dim\\_Threshold](#) = 1 << 3
- const unsigned int [DEFAULT\\_Products\\_Size\\_Threshold](#) = 1 << 22
- const [precision\\_t](#) [DEFAULT\\_Function\\_Precision](#) = [precision\\_same](#)
- static const long double [I\\_pi](#) = 3.1415926535897932384626433832795029L
- static const long double [I\\_ln2](#) = 0.6931471805599453094172321214581766L

### 5.2.1 Typedef Documentation

#### 5.2.1.1 [index\\_t](#)

```
typedef int glucat::index\_t
```

Size of [index\\_t](#) should be enough to represent LO, HI.

Definition at line 77 of file [global.h](#).

### 5.2.1.2 intfn

```
typedef int(* glucat::intfn) ()
```

For exception catching: pointer to function returning int.

Definition at line 37 of file try\_catch.h.

### 5.2.1.3 intintfn

```
typedef int(* glucat::intintfn) (int)
```

For exception catching: pointer to function of int returning int.

Definition at line 40 of file try\_catch.h.

### 5.2.1.4 set\_value\_t

```
typedef unsigned long glucat::set_value_t
```

Size of set\_value\_t should be enough to contain index\_set<LO,HI>

Definition at line 79 of file global.h.

## 5.2.2 Enumeration Type Documentation

### 5.2.2.1 precision\_t

```
enum glucat::precision_t
```

Precision policy.

Enumerator

precision_demoted	
precision_same	
precision_promoted	

Definition at line 117 of file global.h.

### 5.2.3 Function Documentation

#### 5.2.3.1 `_GLUCAT_CTAssert()` [1/3]

```
glucat::_GLUCAT_CTAssert (
    std::numeric_limits< unsigned char >::radix  == 2,
    CannotDetermineBitsPerChar ) const
```

If radix of unsigned char is not 2, we can't easily determine number of bits from sizeof.

Number of bits per char is used to determine number of bits in `set_value_t`

#### 5.2.3.2 `_GLUCAT_CTAssert()` [2/3]

```
glucat::_GLUCAT_CTAssert (
    _GLUCAT_BITS_PER_ULONG  == BITS_PER_SET_VALUE,
    BitsPerULongDoesNotMatchSetValueT ) const
```

Default lowest index in an index set.

#### 5.2.3.3 `_GLUCAT_CTAssert()` [3/3]

```
glucat::_GLUCAT_CTAssert (
    sizeof(set_value_t) >= sizeof(std::bitset< DEFAULT_HI-DEFAULT_LO > ) ,
    Default_index_set_too_big_for_value ) const
```

Size of `set_value_t` should be enough to contain `bitset<DEFAULT_HI-DEFAULT_LO>`

Write out index set

#### 5.2.3.4 `abs()`

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↔
_T , const index_t LO, const index_t HI>
Scalar_T glucat::abs (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Absolute value == `sqrt(norm)`

Definition at line 491 of file `clifford_algebra_imp.h`.

References `glucat::numeric_traits< Scalar_T >::sqrt()`.

Referenced by `PyClical.clifford::abs()`, `acos()`, `asin()`, `glucat::matrix::classify_eigenvalues()`, `clifford_to_str()`, `glucat::framed_multi< Scalar_T, LO, HI >::framed_multi()`, `matrix_log()`, and `matrix_sqrt()`.

### 5.2.3.5 `acos()` [1/2]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::acos (
    const Multivector< Scalar_T, LO, HI > & val,
    const Multivector< Scalar_T, LO, HI > & i,
    const bool prechecked = false ) [inline]
```

Inverse cosine of multivector with specified complexifier.

Definition at line 798 of file `clifford_algebra_imp.h`.

References `abs()`, `acosh()`, `check_complex()`, and `PyClical::i`.

Referenced by `glucat::numeric_traits< Scalar_T >::acos()`, and `acos()`.

### 5.2.3.6 `acos()` [2/2]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::acos (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Inverse cosine of multivector.

Definition at line 818 of file `clifford_algebra_imp.h`.

References `acos()`, and `complexifier()`.

### 5.2.3.7 `acosh()` [1/2]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::acosh (
    const Multivector< Scalar_T, LO, HI > & val,
    const Multivector< Scalar_T, LO, HI > & i,
    const bool prechecked = false ) [inline]
```

Inverse hyperbolic cosine of multivector with specified complexifier.

Definition at line 738 of file `clifford_algebra_imp.h`.

References `check_complex()`, `PyClical::i`, `log()`, `norm()`, and `sqrt()`.

Referenced by `acos()`, and `acosh()`.

**5.2.3.8** `acosh()` [2/2]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::acosh (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Inverse hyperbolic cosine of multivector.

Definition at line 758 of file `clifford_algebra_imp.h`.

References `acosh()`, and `complexifier()`.

**5.2.3.9** `asin()` [1/2]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::asin (
    const Multivector< Scalar_T, LO, HI > & val,
    const Multivector< Scalar_T, LO, HI > & i,
    const bool prechecked = false ) [inline]
```

Inverse sine of multivector with specified complexifier.

Definition at line 905 of file `clifford_algebra_imp.h`.

References `abs()`, `asinh()`, `check_complex()`, and `PyClical::i`.

Referenced by `glucat::numeric_traits< Scalar_T >::asin()`, and `asin()`.

**5.2.3.10** `asin()` [2/2]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::asin (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Inverse sine of multivector.

Definition at line 925 of file `clifford_algebra_imp.h`.

References `asin()`, and `complexifier()`.

**5.2.3.11 asinh()** [1/2]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::asinh (
    const Multivector< Scalar_T, LO, HI > & val,
    const Multivector< Scalar_T, LO, HI > & i,
    const bool prechecked = false ) [inline]
```

Inverse hyperbolic sine of multivector with specified complexifier.

Definition at line 845 of file clifford\_algebra\_imp.h.

References `check_complex()`, `PyClical::i`, `log()`, `norm()`, and `sqrt()`.

Referenced by `asin()`, and `asinh()`.

**5.2.3.12 asinh()** [2/2]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::asinh (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Inverse hyperbolic sine of multivector.

Definition at line 865 of file clifford\_algebra\_imp.h.

References `asinh()`, and `complexifier()`.

**5.2.3.13 atan()** [1/2]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::atan (
    const Multivector< Scalar_T, LO, HI > & val,
    const Multivector< Scalar_T, LO, HI > & i,
    const bool prechecked = false ) [inline]
```

Inverse tangent of multivector with specified complexifier.

Definition at line 1005 of file clifford\_algebra\_imp.h.

References `atanh()`, `check_complex()`, `PyClical::i`, and `scalar()`.

Referenced by `glucat::numeric_traits< Scalar_T >::atan()`, and `atan()`.

**5.2.3.14 atan()** [2/2]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::atan (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Inverse tangent of multivector.

Definition at line 1025 of file clifford\_algebra\_imp.h.

References atan(), and complexifier().

**5.2.3.15 atanh()** [1/2]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::atanh (
    const Multivector< Scalar_T, LO, HI > & val,
    const Multivector< Scalar_T, LO, HI > & i,
    const bool prechecked = false ) [inline]
```

Inverse hyperbolic tangent of multivector with specified complexifier.

Definition at line 952 of file clifford\_algebra\_imp.h.

References check\_complex(), PyClical::i, log(), and norm().

Referenced by atan(), and atanh().

**5.2.3.16 atanh()** [2/2]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::atanh (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Inverse hyperbolic tangent of multivector.

Definition at line 969 of file clifford\_algebra\_imp.h.

References atanh(), and complexifier().

### 5.2.3.17 cascade\_log()

```
template<typename Scalar_T , const index_t LO, const index_t HI>
static const matrix_multi<Scalar_T,LO,HI> glucat::cascade_log (
    const matrix_multi< Scalar_T, LO, HI > & val ) [static]
```

Incomplete square root cascade and Pade' approximation of log.

Definition at line 1976 of file matrix\_multi\_imp.h.

References db\_step(), glucat::clifford\_algebra< Scalar\_T, index\_set< LO, HI >, matrix\_multi< Scalar\_T, LO, HI > >::isnan(), glucat::tuning< Mult\_Matrix\_Threshold, Div\_Max\_Steps, Sqrt\_Max\_Steps, Log\_Max\_Outer\_Steps, Log\_Max\_Inner\_Steps, Basis\_Max\_Count, Fast\_Size\_Threshold, Inv\_Fast\_Dim\_Threshold, Products\_Size\_Threshold, Function\_Precision >::log\_max\_inner\_steps, glucat::tuning< Mult\_Matrix\_Threshold, Div\_Max\_Steps, Sqrt\_Max\_Steps, Log\_Max\_Outer\_Steps, Log\_Max\_Inner\_Steps, Basis\_Max\_Count, Fast\_Size\_Threshold, Inv\_Fast\_Dim\_Threshold, Products\_Size\_Threshold, Function\_Precision >::log\_max\_outer\_steps, norm(), pade\_log(), and pow().

Referenced by matrix\_log().

### 5.2.3.18 check\_complex()

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>
static void glucat::check_complex (
    const Multivector< Scalar_T, LO, HI > & val,
    const Multivector< Scalar_T, LO, HI > & i,
    const bool prechecked = false ) [inline], [static]
```

Check that i is a valid complexifier for val.

Definition at line 566 of file clifford\_algebra\_imp.h.

References complexifier(), and PyClical::i.

Referenced by acos(), acosh(), asin(), asinh(), atan(), atanh(), cos(), log(), sin(), sqrt(), and tan().

### 5.2.3.19 clifford\_exp()

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::clifford_exp (
    const Multivector< Scalar_T, LO, HI > & val )
```

Exponential of multivector.

Definition at line 604 of file clifford\_algebra\_imp.h.

References exp(), log2(), pow(), and scalar().

Referenced by exp().

## 5.2.3.20 compare()

```
template<const index_t LO, const index_t HI>
int glucat::compare (
    const index_set< LO, HI > & a,
    const index_set< LO, HI > & b ) [inline]
```

"lexicographic compare" eg. {3,4,5} is less than {3,7,8}

Lexicographic ordering of two sets: -1 if  $a < b$ , +1 if  $a > b$ , 0 if  $a == b$ .

Definition at line 573 of file index\_set\_imp.h.

References glucat::index\_set< LO, HI >::lex\_less\_than().

## 5.2.3.21 complexifier()

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::complexifier (
    const Multivector< Scalar_T, LO, HI > & val )
```

Square root of -1 which commutes with all members of the frame of the given multivector.

Definition at line 506 of file clifford\_algebra\_imp.h.

References pos\_mod().

Referenced by acos(), acosh(), asin(), asinh(), atan(), atanh(), check\_complex(), cos(), elliptic(), log(), sin(), sqrt(), and tan().

## 5.2.3.22 conj()

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::conj (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Conjugation,  $rev \circ inv == inv \circ rev$ .

Definition at line 467 of file clifford\_algebra\_imp.h.

**5.2.3.23 cos()** [1/2]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::cos (
    const Multivector< Scalar_T, LO, HI > & val,
    const Multivector< Scalar_T, LO, HI > & i,
    const bool prechecked = false )
```

Cosine of multivector with specified complexifier.

Definition at line 765 of file `clifford_algebra_imp.h`.

References `check_complex()`, `exp()`, `PyClical::i`, `PyClical::pi`, and `scalar()`.

Referenced by `glucat::numeric_traits< Scalar_T >::cos()`, `cos()`, and `tan()`.

**5.2.3.24 cos()** [2/2]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::cos (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Cosine of multivector.

Definition at line 789 of file `clifford_algebra_imp.h`.

References `complexifier()`, and `cos()`.

**5.2.3.25 cosh()**

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::cosh (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Hyperbolic cosine of multivector.

Definition at line 720 of file `clifford_algebra_imp.h`.

References `exp()`, and `scalar()`.

Referenced by `glucat::numeric_traits< Scalar_T >::cosh()`, and `tanh()`.

**5.2.3.26** `crd_of_mult()` [1/2]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
static Scalar_T glucat::crd_of_mult (
    const std::pair< const index\_set< LO, HI >, Scalar_T > & lhs,
    const std::pair< const index\_set< LO, HI >, Scalar_T > & rhs ) [inline], [static]
```

Coordinate of product of terms.

Referenced by operator &(), operator%(), operator\*(), and operator^().

**5.2.3.27** `crd_of_mult()` [2/2]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
static Scalar_T glucat::crd_of_mult (
    const std::pair< const index\_set< LO, HI >, Scalar_T > & lhs,
    const std::pair< const index\_set< LO, HI >, Scalar_T > & rhs ) [inline], [static]
```

Coordinate of product of terms.

Definition at line 1906 of file `framed_multi_imp.h`.

**5.2.3.28** `db_sqrt()`

```
template<typename Scalar_T , const index_t LO, const index_t HI>
static const matrix\_multi<Scalar_T,LO,HI> glucat::db_sqrt (
    const matrix\_multi< Scalar_T, LO, HI > & val ) [static]
```

Product form of Denman-Beavers square root iteration.

Definition at line 1375 of file `matrix_multi_imp.h`.

References `db_step()`, `norm()`, `pow()`, and `glucat::tuning< Mult_Matrix_Threshold, Div_Max_Steps, Sqrt_Max_Steps, Log_Max_Outer_Steps, Log_Max_Inner_Steps, Basis_Max_Count, Fast_Size_Threshold, Inv_Fast_Dim_Threshold, Products_Size_Threshold, Function_Precision >::sqrt_max_steps`.

Referenced by `matrix_sqrt()`.

**5.2.3.29** `db_step()`

```
template<typename Scalar_T , const index_t LO, const index_t HI>
static void glucat::db_step (
    matrix\_multi< Scalar_T, LO, HI > & M,
    matrix\_multi< Scalar_T, LO, HI > & Y ) [inline], [static]
```

Single step of product form of Denman-Beavers square root iteration.

Definition at line 1362 of file `matrix_multi_imp.h`.

References `inv()`.

Referenced by `cascade_log()`, and `db_sqrt()`.

### 5.2.3.30 elliptic()

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T, const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::elliptic (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Square root of -1 which commutes with all members of the frame of the given multivector The name "elliptic" is now deprecated: use "complexifier" instead.

Definition at line 557 of file clifford\_algebra\_imp.h.

References complexifier().

### 5.2.3.31 even()

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T, const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::even (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Even part.

Definition at line 427 of file clifford\_algebra\_imp.h.

### 5.2.3.32 exp() [1/2]

```
template<typename Scalar_T, const index_t LO, const index_t HI>
const framed_multi< Scalar_T, LO, HI > glucat::exp (
    const framed_multi< Scalar_T, LO, HI > & val )
```

Exponential of multivector.

Definition at line 1947 of file framed\_multi\_imp.h.

References clifford\_exp(), glucat::clifford\_algebra< Scalar\_T, index\_set< LO, HI >, framed\_multi< Scalar\_T, LO, HI > >::frame(), glucat::tuning< Mult\_Matrix\_Threshold, Div\_Max\_Steps, Sqrt\_Max\_Steps, Log\_Max\_Outer\_Steps, Log\_Max\_Inner\_Steps, Basis\_Max\_Count, Fast\_Size\_Threshold, Inv\_Fast\_Dim\_Threshold, Products\_Size\_Threshold, Function\_Precision >::function\_precision, glucat::clifford\_algebra< Scalar\_T, index\_set< LO, HI >, framed\_multi< Scalar\_T, LO, HI > >::isnan(), glucat::tuning< Mult\_Matrix\_Threshold, Div\_Max\_Steps, Sqrt\_Max\_Steps, Log\_Max\_Outer\_Steps, Log\_Max\_Inner\_Steps, Basis\_Max\_Count, Fast\_Size\_Threshold, Inv\_Fast\_Dim\_Threshold, Products\_Size\_Threshold, Function\_Precision >::mult\_matrix\_threshold, precision\_demoted, precision\_promoted, and scalar().

Referenced by clifford\_exp(), cos(), cosh(), glucat::numeric\_traits< Scalar\_T >::exp(), exp(), matrix\_log(), matrix\_sqrt(), pow(), PyClical.clifford::pow(), sin(), and sinh().

**5.2.3.33 exp()** [2/2]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const matrix_multi< Scalar_T, LO, HI > glucat::exp (
    const matrix_multi< Scalar_T, LO, HI > & val )
```

Exponential of multivector.

Definition at line 2140 of file matrix\_multi\_imp.h.

References `clifford_exp()`, `exp()`, `glucat::tuning< Mult_Matrix_Threshold, Div_Max_Steps, Sqrt_Max_Steps, Log_Max_Outer_Steps, Log_Max_Inner_Steps, Basis_Max_Count, Fast_Size_Threshold, Inv_Fast_Dim_Threshold, Products_Size_Threshold, Function_Precision >::function_precision`, `glucat::clifford_algebra< Scalar_T, index_set< LO, HI >, matrix_multi< Scalar_T, LO, HI > >::isnan()`, `precision_demoted`, `precision_promoted`, and `scalar()`.

**5.2.3.34 fast()**

```
template<typename Multivector_T , typename Matrix_T , typename Basis_Matrix_T >
static Multivector_T glucat::fast (
    const Matrix_T & X,
    index_t level ) [static]
```

Inverse generalized Fast Fourier Transform.

Definition at line 1083 of file matrix\_multi\_imp.h.

References `glucat::matrix::signed_perm_nork()`.

**5.2.3.35 folded\_dim()**

```
template<typename Matrix_Index_T , const index_t LO, const index_t HI>
static Matrix_Index_T glucat::folded_dim (
    const index_set< LO, HI > & sub ) [inline], [static]
```

Determine the matrix dimension of the fold of a subalgebra.

Definition at line 91 of file matrix\_multi\_imp.h.

References `glucat::index_set< LO, HI >::count_neg()`, `glucat::index_set< LO, HI >::count_pos()`, and `offset_level()`.

**5.2.3.36 imag()**

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar←
_T , const index_t LO, const index_t HI>
Scalar_T glucat::imag (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Imaginary part: deprecated (always 0)

Definition at line 411 of file clifford\_algebra\_imp.h.

Referenced by glucat::matrix::classify\_eigenvalues().

**5.2.3.37 inv()**

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar←
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::inv (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Geometric multiplicative inverse.

Definition at line 321 of file clifford\_algebra\_imp.h.

Referenced by db\_step(), matrix\_log(), and matrix\_sqrt().

**5.2.3.38 inverse\_gray()**

```
static unsigned long glucat::inverse_gray (
    unsigned long x ) [inline], [static]
```

Inverse Gray code.

Definition at line 861 of file index\_set\_imp.h.

Referenced by glucat::index\_set< LO, HI >::sign\_of\_mult().

**5.2.3.39 inverse\_reversed\_gray()**

```
static unsigned long glucat::inverse_reversed_gray (
    unsigned long x ) [inline], [static]
```

Inverse reversed Gray code.

Definition at line 844 of file index\_set\_imp.h.

Referenced by glucat::index\_set< LO, HI >::sign\_of\_mult().

## 5.2.3.40 involute()

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T, const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::involute (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Main involution, each {i} is replaced by -{i} in each term, eg. {1}\*{2} -> (-{2})\*(-{1})

Main involution, each {i} is replaced by -{i} in each term, eg. {1} -> -{1}.

Definition at line 451 of file clifford\_algebra\_imp.h.

## 5.2.3.41 log() [1/4]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const matrix_multi< Scalar_T, LO, HI > glucat::log (
    const matrix_multi< Scalar_T, LO, HI > & val,
    const matrix_multi< Scalar_T, LO, HI > & i,
    bool prechecked )
```

Natural logarithm of multivector with specified complexifier.

Definition at line 2023 of file matrix\_multi\_imp.h.

References `check_complex()`, `glucat::tuning< Mult_Matrix_Threshold, Div_Max_Steps, Sqrt_Max_Steps, Log_Max_Outer_Steps, Log_Max_Inner_Steps, Basis_Max_Count, Fast_Size_Threshold, Inv_Fast_Dim_Threshold, Products_Size_Threshold, Function_Precision >::function_precision`, `PyClical::i`, `glucat::clifford_algebra< Scalar_T, index_set< LO, HI >, matrix_multi< Scalar_T, LO, HI > >::isnan()`, `matrix_log()`, `precision_demoted`, and `precision_promoted`.

## 5.2.3.42 log() [2/4]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const framed_multi< Scalar_T, LO, HI > glucat::log (
    const framed_multi< Scalar_T, LO, HI > & val,
    const framed_multi< Scalar_T, LO, HI > & i,
    bool prechecked )
```

Natural logarithm of multivector with specified complexifier.

Definition at line 1997 of file framed\_multi\_imp.h.

References `check_complex()`, `PyClical::i`, `glucat::clifford_algebra< Scalar_T, index_set< LO, HI >, framed_multi< Scalar_T, LO, HI > >::isnan()`, `log()`, `PyClical::pi`, and `glucat::clifford_algebra< Scalar_T, index_set< LO, HI >, framed_multi< Scalar_T, LO, HI > >::scalar()`.

**5.2.3.43 log()** [3/4]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::log (
    const Multivector< Scalar_T, LO, HI > & val,
    const Multivector< Scalar_T, LO, HI > & i,
    const bool prechecked = false ) [inline]
```

Natural logarithm of multivector with specified complexifier.

Definition at line 704 of file clifford\_algebra\_imp.h.

References PyClical::i.

Referenced by acosh(), asinh(), atanh(), glucat::numeric\_traits< Scalar\_T >::log(), log(), matrix\_log(), glucat↵
::numeric\_traits< Scalar\_T >::NaN(), pow(), and PyClical.clifford::pow().

**5.2.3.44 log()** [4/4]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::log (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Natural logarithm of multivector.

Definition at line 712 of file clifford\_algebra\_imp.h.

References complexifier(), and log().

**5.2.3.45 log2()**

```
template<typename Scalar_T >
Scalar_T glucat::log2 (
    const Scalar_T & x ) [inline]
```

Log base 2 of scalar.

Definition at line 302 of file scalar.h.

References glucat::numeric\_traits< Scalar\_T >::log2().

Referenced by clifford\_exp().

5.2.3.46 `matrix_log()`

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const matrix_multi< Scalar_T, LO, HI > glucat::matrix_log (
    const matrix_multi< Scalar_T, LO, HI > & val,
    const matrix_multi< Scalar_T, LO, HI > & i )
```

Natural logarithm of multivector with specified complexifier.

Definition at line 2064 of file `matrix_multi_imp.h`.

References `abs()`, `glucat::matrix::both_eig_case`, `cascade_log()`, `glucat::matrix::classify_eigenvalues()`, `exp()`, `PyClicl::i`, `inv()`, `glucat::matrix::isnan()`, `glucat::clifford_algebra< Scalar_T, index_set< LO, HI >, matrix_multi< Scalar_T, LO, HI > >::isnan()`, `log()`, `glucat::matrix::eig_genus< Matrix_T >::m_eig_case`, `glucat::matrix::eig_genus< Matrix_T >::m_safe_arg`, `glucat::matrix::negative_eig_case`, `norm()`, `PyClicl::pi`, and `glucat::clifford_algebra< Scalar_T, index_set< LO, HI >, matrix_multi< Scalar_T, LO, HI > >::scalar()`.

Referenced by `log()`.

5.2.3.47 `matrix_sqrt()`

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const matrix_multi< Scalar_T, LO, HI > glucat::matrix_sqrt (
    const matrix_multi< Scalar_T, LO, HI > & val,
    const matrix_multi< Scalar_T, LO, HI > & i )
```

Square root of multivector with specified complexifier.

Definition at line 1645 of file `matrix_multi_imp.h`.

References `abs()`, `glucat::matrix::both_eig_case`, `glucat::matrix::classify_eigenvalues()`, `db_sqrt()`, `exp()`, `PyClicl::i`, `inv()`, `glucat::clifford_algebra< Scalar_T, index_set< LO, HI >, matrix_multi< Scalar_T, LO, HI > >::isnan()`, `glucat::matrix::eig_genus< Matrix_T >::m_eig_case`, `glucat::matrix::eig_genus< Matrix_T >::m_safe_arg`, `glucat::matrix::negative_eig_case`, `norm()`, `pade_approx()`, `glucat::clifford_algebra< Scalar_T, index_set< LO, HI >, matrix_multi< Scalar_T, LO, HI > >::scalar()`, and `sqrt()`.

Referenced by `sqrt()`.

5.2.3.48 `max_abs()`

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>
Scalar_T glucat::max_abs (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Maximum of absolute values of components of multivector: multivector infinity norm.

Definition at line 499 of file `clifford_algebra_imp.h`.

**5.2.3.49 max\_pos()**

```
template<const index_t LO, const index_t HI>
index_t glucat::max_pos (
    const index_set< LO, HI > & ist ) [inline]
```

Maximum positive index, or 0 if none.

Definition at line 974 of file index\_set\_imp.h.

References PyClical::ist.

**5.2.3.50 min\_neg()**

```
template<const index_t LO, const index_t HI>
index_t glucat::min_neg (
    const index_set< LO, HI > & ist ) [inline]
```

Minimum negative index, or 0 if none.

Definition at line 967 of file index\_set\_imp.h.

References PyClical::ist.

**5.2.3.51 norm()**

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
Scalar_T glucat::norm (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Scalar\_T norm == sum of norm of coordinates.

Definition at line 483 of file clifford\_algebra\_imp.h.

Referenced by acosh(), asinh(), atanh(), cascade\_log(), glucat::matrix::classify\_eigenvalues(), db\_sqrt(), matrix\_↵log(), and matrix\_sqrt().

**5.2.3.52 odd()**

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::odd (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Odd part.

Definition at line 435 of file clifford\_algebra\_imp.h.

Referenced by glucat::framed\_multi< Scalar\_T, LO, HI >::fast().

**5.2.3.53 offset\_level()**

```
index_t glucat::offset_level (
    const index_t p,
    const index_t q ) [inline]
```

Determine the log2 dim corresponding to signature p, q.

Definition at line 76 of file matrix\_multi\_imp.h.

References pos\_mod().

Referenced by glucat::matrix\_multi< Scalar\_T, LO, HI >::basis\_element(), and folded\_dim().

**5.2.3.54 operator &() [1/8]**

```
template<const index_t LO, const index_t HI>
const index_set<LO,HI> glucat::operator& (
    const index_set< LO, HI > & lhs,
    const index_set< LO, HI > & rhs ) [inline]
```

Set intersection: and.

Definition at line 186 of file index\_set\_imp.h.

**5.2.3.55 operator &() [2/8]**

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const matrix_multi<Scalar_T,LO,HI> glucat::operator& (
    const matrix_multi< Scalar_T, LO, HI > & lhs,
    const matrix_multi< Scalar_T, LO, HI > & rhs ) [inline]
```

Inner product.

Definition at line 616 of file matrix\_multi\_imp.h.

**5.2.3.56 operator &() [3/8]**

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const framed_multi<Scalar_T,LO,HI> glucat::operator& (
    const framed_multi< Scalar_T, LO, HI > & lhs,
    const framed_multi< Scalar_T, LO, HI > & rhs )
```

Inner product.

Definition at line 601 of file framed\_multi\_imp.h.

References \_GLUCAT\_HASH\_SIZE\_T, crd\_of\_mult(), glucat::clifford\_algebra< Scalar\_T, index\_set< LO, HI >, framed\_multi< Scalar\_T, LO, HI > >::frame(), and glucat::tuning< Mult\_Matrix\_Threshold, Div\_Max\_Steps, Sqrt\_Max\_Steps, Log\_Max\_Outer\_Steps, Log\_Max\_Inner\_Steps, Basis\_Max\_Count, Fast\_Size\_Threshold, Inv\_Fast\_Dim\_Threshold, Products\_Size\_Threshold, Function\_Precision >::products\_size\_threshold.

**5.2.3.57 operator &()** [4/8]

```
template<const index_t LO, const index_t HI>
const index_set<LO,HI> glucat::operator& (
    const index_set< LO, HI > & lhs,
    const index_set< LO, HI > & rhs ) [inline]
```

Set intersection: and.

Definition at line 186 of file index\_set\_imp.h.

**5.2.3.58 operator &()** [5/8]

```
template<template< typename, const index_t, const index_t > class Multivector, template<
typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO,
const index_t HI>
const Multivector<Scalar_T,LO,HI> glucat::operator& (
    const Multivector< Scalar_T, LO, HI > & lhs,
    const RHS< Scalar_T, LO, HI > & rhs ) [inline]
```

Inner product.

Definition at line 228 of file clifford\_algebra\_imp.h.

**5.2.3.59 operator &()** [6/8]

```
template<template< typename, const index_t, const index_t > class Multivector, template<
typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO,
const index_t HI>
const Multivector<Scalar_T,LO,HI> glucat::operator& (
    const Multivector< Scalar_T, LO, HI > & lhs,
    const RHS< Scalar_T, LO, HI > & rhs ) [inline]
```

Inner product.

Definition at line 228 of file clifford\_algebra\_imp.h.

**5.2.3.60 operator &()** [7/8]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const framed_multi<Scalar_T,LO,HI> glucat::operator& (
    const framed_multi< Scalar_T, LO, HI > & lhs,
    const framed_multi< Scalar_T, LO, HI > & rhs )
```

Inner product.

Definition at line 601 of file framed\_multi\_imp.h.

References `_GLUCAT_HASH_SIZE_T`, `crd_of_mult()`, `glucat::clifford_algebra< Scalar_T, index_set< LO, HI >, framed_multi< Scalar_T, LO, HI > >::frame()`, and `glucat::tuning< Mult_Matrix_Threshold, Div_Max_Steps, Sqrt_Max_Steps, Log_Max_Outer_Steps, Log_Max_Inner_Steps, Basis_Max_Count, Fast_Size_Threshold, Inv_Fast_Dim_Threshold, Products_Size_Threshold, Function_Precision >::products_size_threshold`.

**5.2.3.61 operator &()** [8/8]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const matrix_multi<Scalar_T,LO,HI> glucat::operator& (
    const matrix_multi< Scalar_T, LO, HI > & lhs,
    const matrix_multi< Scalar_T, LO, HI > & rhs ) [inline]
```

Inner product.

Definition at line 616 of file matrix\_multi\_imp.h.

**5.2.3.62 operator!=(())** [1/3]

```
template<template< typename, const index_t, const index_t > class Multivector, template<
typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO,
const index_t HI>
bool glucat::operator!=( (
    const Multivector< Scalar_T, LO, HI > & lhs,
    const RHS< Scalar_T, LO, HI > & rhs ) [inline]
```

Test for inequality of multivectors.

Definition at line 78 of file clifford\_algebra\_imp.h.

**5.2.3.63 operator!=(())** [2/3]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
bool glucat::operator!=( (
    const Multivector< Scalar_T, LO, HI > & lhs,
    const Scalar_T & scr ) [inline]
```

Test for inequality of multivector and scalar.

Definition at line 86 of file clifford\_algebra\_imp.h.

**5.2.3.64 operator!=(())** [3/3]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
bool glucat::operator!=( (
    const Scalar_T & scr,
    const Multivector< Scalar_T, LO, HI > & rhs ) [inline]
```

Test for inequality of scalar and multivector.

Definition at line 94 of file clifford\_algebra\_imp.h.

**5.2.3.65 operator%()** [1/3]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const matrix_multi< Scalar_T, LO, HI > glucat::operator% (
    const matrix_multi< Scalar_T, LO, HI > & lhs,
    const matrix_multi< Scalar_T, LO, HI > & rhs ) [inline]
```

Left contraction.

Definition at line 635 of file matrix\_multi\_imp.h.

**5.2.3.66 operator%()** [2/3]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const framed_multi< Scalar_T, LO, HI > glucat::operator% (
    const framed_multi< Scalar_T, LO, HI > & lhs,
    const framed_multi< Scalar_T, LO, HI > & rhs )
```

Left contraction.

Definition at line 719 of file framed\_multi\_imp.h.

References `_GLUCAT_HASH_SIZE_T`, `crd_of_mult()`, `glucat::clifford_algebra< Scalar_T, index_set< LO, HI >, framed_multi< Scalar_T, LO, HI > >::frame()`, and `glucat::tuning< Mult_Matrix_Threshold, Div_Max_Steps, Sqrt↵_Max_Steps, Log_Max_Outer_Steps, Log_Max_Inner_Steps, Basis_Max_Count, Fast_Size_Threshold, Inv_↵Fast_Dim_Threshold, Products_Size_Threshold, Function_Precision >::products_size_threshold`.

**5.2.3.67 operator%()** [3/3]

```
template<template< typename, const index_t, const index_t > class Multivector, template<
typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO,
const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::operator% (
    const Multivector< Scalar_T, LO, HI > & lhs,
    const RHS< Scalar_T, LO, HI > & rhs ) [inline]
```

Left contraction.

Definition at line 243 of file clifford\_algebra\_imp.h.

**5.2.3.68 operator\*()** [1/6]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const matrix\_multi< Scalar_T, LO, HI > glucat::operator* (
    const matrix\_multi< Scalar_T, LO, HI > & lhs,
    const matrix\_multi< Scalar_T, LO, HI > & rhs ) [inline]
```

Geometric product.

Definition at line 547 of file `matrix_multi_imp.h`.

References `glucat::clifford_algebra< Scalar_T, index_set< LO, HI >, matrix_multi< Scalar_T, LO, HI > >::isnan()`, `glucat::matrix_multi< Scalar_T, LO, HI >::m_frame`, `glucat::matrix_multi< Scalar_T, LO, HI >::m_matrix`, and `re-frame()`.

**5.2.3.69 operator\*()** [2/6]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const framed\_multi< Scalar_T, LO, HI > glucat::operator* (
    const framed\_multi< Scalar_T, LO, HI > & lhs,
    const framed\_multi< Scalar_T, LO, HI > & rhs )
```

Geometric product.

Definition at line 400 of file `framed_multi_imp.h`.

References `_GLUCAT_HASH_SIZE_T`, `glucat::clifford_algebra< Scalar_T, index_set< LO, HI >, framed_multi< Scalar_T, LO, HI > >::frame()`, `glucat::clifford_algebra< Scalar_T, index_set< LO, HI >, framed_multi< Scalar_T, LO, HI > >::isnan()`, and `glucat::tuning< Mult_Matrix_Threshold, Div_Max_Steps, Sqrt_Max_Steps, Log_Max_Outer_Steps, Log_Max_Inner_Steps, Basis_Max_Count, Fast_Size_Threshold, Inv_Fast_Dim_Threshold, Products_Size_Threshold, Function_Precision >::mult_matrix_threshold`.

**5.2.3.70 operator\*()** [3/6]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::operator* (
    const Multivector< Scalar_T, LO, HI > & lhs,
    const Scalar_T & scr ) [inline]
```

Product of multivector and scalar.

Definition at line 172 of file `clifford_algebra_imp.h`.

**5.2.3.71 operator\*()** [4/6]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::operator* (
    const Scalar_T & scr,
    const Multivector< Scalar_T, LO, HI > & rhs ) [inline]
```

Product of scalar and multivector.

Definition at line 183 of file clifford\_algebra\_imp.h.

**5.2.3.72 operator\*()** [5/6]

```
template<template< typename, const index_t, const index_t > class Multivector, template<
typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO,
const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::operator* (
    const Multivector< Scalar_T, LO, HI > & lhs,
    const RHS< Scalar_T, LO, HI > & rhs ) [inline]
```

Geometric product.

Definition at line 198 of file clifford\_algebra\_imp.h.

**5.2.3.73 operator\*()** [6/6]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const std::pair< const index\_set< LO, HI >, Scalar_T > glucat::operator* (
    const std::pair< const index\_set< LO, HI >, Scalar_T > & lhs,
    const std::pair< const index\_set< LO, HI >, Scalar_T > & rhs ) [inline]
```

Product of terms.

Definition at line 1914 of file framed\_multi\_imp.h.

References [crd\\_of\\_mult\(\)](#).

**5.2.3.74 operator+()** [1/3]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::operator+ (
    const Multivector< Scalar_T, LO, HI > & lhs,
    const Scalar_T & scr ) [inline]
```

Geometric sum of multivector and scalar.

Definition at line 102 of file clifford\_algebra\_imp.h.

**5.2.3.75 operator+()** [2/3]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::operator+ (
    const Scalar_T & scr,
    const Multivector< Scalar_T, LO, HI > & rhs ) [inline]
```

Geometric sum of scalar and multivector.

Definition at line 113 of file clifford\_algebra\_imp.h.

**5.2.3.76 operator+()** [3/3]

```
template<template< typename, const index_t, const index_t > class Multivector, template<
typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO,
const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::operator+ (
    const Multivector< Scalar_T, LO, HI > & lhs,
    const RHS< Scalar_T, LO, HI > & rhs ) [inline]
```

Geometric sum.

Definition at line 127 of file clifford\_algebra\_imp.h.

**5.2.3.77 operator-()** [1/3]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::operator- (
    const Multivector< Scalar_T, LO, HI > & lhs,
    const Scalar_T & scr ) [inline]
```

Geometric difference of multivector and scalar.

Definition at line 138 of file clifford\_algebra\_imp.h.

**5.2.3.78 operator-()** [2/3]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::operator- (
    const Scalar_T & scr,
    const Multivector< Scalar_T, LO, HI > & rhs ) [inline]
```

Geometric difference of scalar and multivector.

Definition at line 149 of file clifford\_algebra\_imp.h.

**5.2.3.79 operator-()** [3/3]

```
template<template< typename, const index_t, const index_t > class Multivector, template<
typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO,
const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::operator- (
    const Multivector< Scalar_T, LO, HI > & lhs,
    const RHS< Scalar_T, LO, HI > & rhs ) [inline]
```

Geometric difference.

Definition at line 161 of file clifford\_algebra\_imp.h.

**5.2.3.80 operator/()** [1/5]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const matrix_multi< Scalar_T, LO, HI > glucat::operator/ (
    const matrix_multi< Scalar_T, LO, HI > & lhs,
    const matrix_multi< Scalar_T, LO, HI > & rhs )
```

Geometric quotient.

Definition at line 668 of file matrix\_multi\_imp.h.

References glucat::tuning< Mult\_Matrix\_Threshold, Div\_Max\_Steps, Sqrt\_Max\_Steps, Log\_Max\_Outer\_Steps, Log\_Max\_Inner\_Steps, Basis\_Max\_Count, Fast\_Size\_Threshold, Inv\_Fast\_Dim\_Threshold, Products\_Size\_Threshold, Function\_Precision >::div\_max\_steps, glucat::matrix::isnan(), glucat::clifford\_algebra< Scalar\_T, index\_set< LO, HI >, matrix\_multi< Scalar\_T, LO, HI > >::isnan(), glucat::matrix\_multi< Scalar\_T, LO, HI >::m\_frame, and reframe().

**5.2.3.81 operator/()** [2/5]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const framed_multi< Scalar_T, LO, HI > glucat::operator/ (
    const framed_multi< Scalar_T, LO, HI > & lhs,
    const framed_multi< Scalar_T, LO, HI > & rhs ) [inline]
```

Geometric quotient.

Definition at line 914 of file framed\_multi\_imp.h.

References glucat::clifford\_algebra< Scalar\_T, index\_set< LO, HI >, framed\_multi< Scalar\_T, LO, HI > >::frame().

**5.2.3.82 operator/()** [3/5]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::operator/ (
    const Multivector< Scalar_T, LO, HI > & lhs,
    const Scalar_T & scr ) [inline]
```

Quotient of multivector and scalar.

Definition at line 269 of file clifford\_algebra\_imp.h.

**5.2.3.83 operator/()** [4/5]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::operator/ (
    const Scalar_T & scr,
    const Multivector< Scalar_T, LO, HI > & rhs ) [inline]
```

Quotient of scalar and multivector.

Definition at line 280 of file clifford\_algebra\_imp.h.

**5.2.3.84 operator/()** [5/5]

```
template<template< typename, const index_t, const index_t > class Multivector, template<
typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO,
const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::operator/ (
    const Multivector< Scalar_T, LO, HI > & lhs,
    const RHS< Scalar_T, LO, HI > & rhs ) [inline]
```

Geometric quotient.

Definition at line 295 of file clifford\_algebra\_imp.h.

**5.2.3.85 operator<<()** [1/4]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
std::ostream & glucat::operator<< (
    std::ostream & os,
    const matrix\_multi< Scalar_T, LO, HI > & val ) [inline]
```

Write multivector to output.

Definition at line 1025 of file matrix\_multi\_imp.h.

**5.2.3.86 operator<<()** [2/4]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
std::ostream & glucat::operator<< (
    std::ostream & os,
    const framed_multi< Scalar_T, LO, HI > & val )
```

Write multivector to output.

Definition at line 1366 of file framed\_multi\_imp.h.

References glucat::sorted\_range< Map\_T, Sorted\_Map\_T >::sorted\_begin, and glucat::sorted\_range< Map\_T, Sorted\_Map\_T >::sorted\_end.

**5.2.3.87 operator<<()** [3/4]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
std::ostream & glucat::operator<< (
    std::ostream & os,
    const std::pair< const index_set< LO, HI >, Scalar_T > & term )
```

Write term to output.

Definition at line 1398 of file framed\_multi\_imp.h.

References pow(), and glucat::numeric\_traits< Scalar\_T >::to\_double().

**5.2.3.88 operator<<()** [4/4]

```
std::ostream & glucat::operator<< (
    std::ostream & os,
    const index_set< LO, HI > & ist )
```

Write out index set.

Definition at line 611 of file index\_set\_imp.h.

References PyClical::i, and PyClical::ist.

**5.2.3.89 operator>>()** [1/3]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
std::istream & glucat::operator>> (
    std::istream & s,
    matrix_multi< Scalar_T, LO, HI > & val ) [inline]
```

Read multivector from input.

Definition at line 1035 of file matrix\_multi\_imp.h.

**5.2.3.90 operator>>()** [2/3]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
std::istream & glucat::operator>> (
    std::istream & s,
    framed_multi< Scalar_T, LO, HI > & val )
```

Read multivector from input.

Definition at line 1436 of file framed\_multi\_imp.h.

References PyClical::ist.

**5.2.3.91 operator>>()** [3/3]

```
template<const index_t LO, const index_t HI>
std::istream & glucat::operator>> (
    std::istream & s,
    index_set< LO, HI > & ist )
```

Read in index set.

Definition at line 633 of file index\_set\_imp.h.

References PyClical::i, PyClical::ist, and glucat::index\_set< LO, HI >::set().

**5.2.3.92 operator^()** [1/4]

```
template<const index_t LO, const index_t HI>
const index_set< LO, HI > glucat::operator^ (
    const index_set< LO, HI > & lhs,
    const index_set< LO, HI > & rhs ) [inline]
```

Symmetric set difference: exclusive or.

Definition at line 161 of file index\_set\_imp.h.

**5.2.3.93 operator^()** [2/4]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const matrix_multi< Scalar_T, LO, HI > glucat::operator^ (
    const matrix_multi< Scalar_T, LO, HI > & lhs,
    const matrix_multi< Scalar_T, LO, HI > & rhs ) [inline]
```

Outer product.

Definition at line 597 of file matrix\_multi\_imp.h.

**5.2.3.94** `operator^()` [3/4]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const framed_multi< Scalar_T, LO, HI > glucat::operator^ (
    const framed_multi< Scalar_T, LO, HI > & lhs,
    const framed_multi< Scalar_T, LO, HI > & rhs )
```

Outer product.

Definition at line 501 of file framed\_multi\_imp.h.

References `_GLUCAT_HASH_SIZE_T`, `crd_of_mult()`, `glucat::clifford_algebra< Scalar_T, index_set< LO, HI >, framed_multi< Scalar_T, LO, HI > >::frame()`, and `glucat::tuning< Mult_Matrix_Threshold, Div_Max_Steps, Sqrt_↵_Max_Steps, Log_Max_Outer_Steps, Log_Max_Inner_Steps, Basis_Max_Count, Fast_Size_Threshold, Inv_↵Fast_Dim_Threshold, Products_Size_Threshold, Function_Precision >::products_size_threshold`.

**5.2.3.95** `operator^()` [4/4]

```
template<template< typename, const index_t, const index_t > class Multivector, template<
typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO,
const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::operator^ (
    const Multivector< Scalar_T, LO, HI > & lhs,
    const RHS< Scalar_T, LO, HI > & rhs ) [inline]
```

Outer product.

Definition at line 213 of file clifford\_algebra\_imp.h.

**5.2.3.96** `operator" |()` [1/4]

```
template<const index_t LO, const index_t HI>
const index_set< LO, HI > glucat::operator| (
    const index_set< LO, HI > & lhs,
    const index_set< LO, HI > & rhs ) [inline]
```

Set union: or.

Definition at line 211 of file index\_set\_imp.h.

**5.2.3.97** `operator" |()` [2/4]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const matrix_multi< Scalar_T, LO, HI > glucat::operator| (
    const matrix_multi< Scalar_T, LO, HI > & lhs,
    const matrix_multi< Scalar_T, LO, HI > & rhs ) [inline]
```

Transformation via twisted adjoint action.

Definition at line 777 of file matrix\_multi\_imp.h.

References `glucat::clifford_algebra< Scalar_T, index_set< LO, HI >, matrix_multi< Scalar_T, LO, HI > >↵::involute()`.

**5.2.3.98 operator" | () [3/4]**

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const framed_multi< Scalar_T, LO, HI > glucat::operator| (
    const framed_multi< Scalar_T, LO, HI > & lhs,
    const framed_multi< Scalar_T, LO, HI > & rhs ) [inline]
```

Transformation via twisted adjoint action.

Definition at line 940 of file framed\_multi\_imp.h.

References glucat::clifford\_algebra< Scalar\_T, index\_set< LO, HI >, framed\_multi< Scalar\_T, LO, HI > >::involute().

**5.2.3.99 operator" | () [4/4]**

```
template<template< typename, const index_t, const index_t > class Multivector, template<
typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO,
const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::operator| (
    const Multivector< Scalar_T, LO, HI > & lhs,
    const RHS< Scalar_T, LO, HI > & rhs ) [inline]
```

Transformation via twisted adjoint action.

Definition at line 310 of file clifford\_algebra\_imp.h.

**5.2.3.100 outer\_pow()**

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::outer_pow (
    const Multivector< Scalar_T, LO, HI > & lhs,
    int rhs )
```

Outer product power of multivector.

Definition at line 384 of file clifford\_algebra\_imp.h.

**5.2.3.101 pade\_approx()**

```
template<typename Scalar_T , const index_t LO, const index_t HI>
static const matrix_multi<Scalar_T,LO,HI> glucat::pade_approx (
    const int array_size,
    const Scalar_T a[],
    const Scalar_T b[],
    const matrix_multi< Scalar_T, LO, HI > & X ) [inline], [static]
```

Pade' approximation.

Definition at line 1302 of file matrix\_multi\_imp.h.

References glucat::clifford\_algebra< Scalar\_T, index\_set< LO, HI >, matrix\_multi< Scalar\_T, LO, HI > >::isnan().

Referenced by matrix\_sqrt(), and pade\_log().

### 5.2.3.102 pade\_log()

```
template<typename Scalar_T , const index_t LO, const index_t HI>
static const matrix_multi<Scalar_T,LO,HI> glucat::pade_log (
    const matrix_multi< Scalar_T, LO, HI > & val ) [static]
```

Pade' approximation of log.

Definition at line 1955 of file matrix\_multi\_imp.h.

References glucat::clifford\_algebra< Scalar\_T, index\_set< LO, HI >, matrix\_multi< Scalar\_T, LO, HI > >::isnan(), and pade\_approx().

Referenced by cascade\_log().

### 5.2.3.103 pos\_mod()

```
template<typename LHS_T , typename RHS_T >
LHS_T glucat::pos_mod (
    LHS_T lhs,
    RHS_T rhs ) [inline]
```

Modulo function which works reliably for lhs < 0.

Definition at line 187 of file global.h.

Referenced by complexifier(), glucat::matrix\_multi< Scalar\_T, LO, HI >::fast\_framed\_multi(), glucat::framed\_multi< Scalar\_T, LO, HI >::fast\_matrix\_multi(), glucat::gen::generator\_table< Matrix\_T >::gen\_vector(), offset\_level(), and glucat::gen::generator\_table< Matrix\_T >::operator().

### 5.2.3.104 pow() [1/2]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::pow (
    const Multivector< Scalar_T, LO, HI > & lhs,
    int rhs )
```

Integer power of multivector.

Definition at line 328 of file clifford\_algebra\_imp.h.

Referenced by cascade\_log(), clifford\_exp(), db\_sqrt(), operator<<(), and glucat::numeric\_traits< Scalar\_T >↵::pow().

**5.2.3.105 pow()** [2/2]

```
template<template< typename, const index_t, const index_t > class Multivector, template<
typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO,
const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::pow (
    const Multivector< Scalar_T, LO, HI > & lhs,
    const RHS< Scalar_T, LO, HI > & rhs ) [inline]
```

Multivector power of multivector.

Definition at line 361 of file clifford\_algebra\_imp.h.

References `exp()`, and `log()`.

**5.2.3.106 pure()**

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::pure (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Pure part.

Definition at line 419 of file clifford\_algebra\_imp.h.

**5.2.3.107 quad()**

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
Scalar_T glucat::quad (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Scalar\_T quadratic form == (rev(x)\*x)(0)

Definition at line 475 of file clifford\_algebra\_imp.h.

**5.2.3.108 real()**

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
Scalar_T glucat::real (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Real part: synonym for scalar part.

Definition at line 400 of file clifford\_algebra\_imp.h.

Referenced by `glucat::matrix::classify_eigenvalues()`.

**5.2.3.109 `reframe()`**

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const index_set< LO, HI > glucat::reframe (
    const matrix_multi< Scalar_T, LO, HI > & lhs,
    const matrix_multi< Scalar_T, LO, HI > & rhs,
    matrix_multi< Scalar_T, LO, HI > & lhs_reframed,
    matrix_multi< Scalar_T, LO, HI > & rhs_reframed ) [inline]
```

Find a common frame for operands of a binary operator.

Definition at line 350 of file `matrix_multi_imp.h`.

References `glucat::matrix_multi< Scalar_T, LO, HI >::m_frame`.

Referenced by `operator*()`, and `operator/()`.

**5.2.3.110 `reverse()`**

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↔
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::reverse (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Reversion, eg.  $\{1\}*\{2\} \rightarrow \{2\}*\{1\}$ .

Definition at line 459 of file `clifford_algebra_imp.h`.

**5.2.3.111 `scalar()`**

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↔
_T , const index_t LO, const index_t HI>
Scalar_T glucat::scalar (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Scalar part.

Definition at line 392 of file `clifford_algebra_imp.h`.

Referenced by `atan()`, `clifford_exp()`, `cos()`, `cosh()`, `exp()`, `glucat::framed_multi< Scalar_T, LO, HI >::fast()`, `sin()`, `sinh()`, `tan()`, and `tanh()`.

**5.2.3.112 sign\_of\_square()**

```
int glucat::sign_of_square (
    index_t j ) [inline]
```

Square of generator {j}.

Square of generator index j.

Definition at line 960 of file index\_set\_imp.h.

**5.2.3.113 sin()** [1/2]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↔
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::sin (
    const Multivector< Scalar_T, LO, HI > & val,
    const Multivector< Scalar_T, LO, HI > & i,
    const bool prechecked = false )
```

Sine of multivector with specified complexifier.

Definition at line 872 of file clifford\_algebra\_imp.h.

References `check_complex()`, `exp()`, `PyClical::i`, `PyClical::pi`, and `scalar()`.

Referenced by `glucat::numeric_traits< Scalar_T >::sin()`, `sin()`, and `tan()`.

**5.2.3.114 sin()** [2/2]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↔
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::sin (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Sine of multivector.

Definition at line 896 of file clifford\_algebra\_imp.h.

References `complexifier()`, and `sin()`.

### 5.2.3.115 sinh()

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T, const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::sinh (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Hyperbolic sine of multivector.

Definition at line 826 of file `clifford_algebra_imp.h`.

References `exp()`, and `scalar()`.

Referenced by `glucat::numeric_traits< Scalar_T >::sinh()`, and `tanh()`.

### 5.2.3.116 sqrt() [1/4]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const matrix_multi< Scalar_T, LO, HI > glucat::sqrt (
    const matrix_multi< Scalar_T, LO, HI > & val,
    const matrix_multi< Scalar_T, LO, HI > & i,
    bool prechecked )
```

Square root of multivector with specified complexifier.

Definition at line 1600 of file `matrix_multi_imp.h`.

References `check_complex()`, `glucat::tuning< Mult_Matrix_Threshold, Div_Max_Steps, Sqrt_Max_Steps, Log_Max_Outer_Steps, Log_Max_Inner_Steps, Basis_Max_Count, Fast_Size_Threshold, Inv_Fast_Dim_Threshold, Products_Size_Threshold, Function_Precision >::function_precision`, `PyClical::i`, `glucat::clifford_algebra< Scalar_T, index_set< LO, HI >, matrix_multi< Scalar_T, LO, HI > >::isnan()`, `matrix_sqrt()`, `precision_demoted`, and `precision_promoted`.

### 5.2.3.117 sqrt() [2/4]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const framed_multi< Scalar_T, LO, HI > glucat::sqrt (
    const framed_multi< Scalar_T, LO, HI > & val,
    const framed_multi< Scalar_T, LO, HI > & i,
    bool prechecked )
```

Square root of multivector with specified complexifier.

Definition at line 1924 of file `framed_multi_imp.h`.

References `check_complex()`, `PyClical::i`, `glucat::clifford_algebra< Scalar_T, index_set< LO, HI >, framed_multi< Scalar_T, LO, HI > >::isnan()`, `glucat::clifford_algebra< Scalar_T, index_set< LO, HI >, framed_multi< Scalar_T, LO, HI > >::scalar()`, and `sqrt()`.

**5.2.3.118** `sqrt()` [3/4]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T, const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::sqrt (
    const Multivector< Scalar_T, LO, HI > & val,
    const Multivector< Scalar_T, LO, HI > & i,
    const bool prechecked = false ) [inline]
```

Square root of multivector with specified complexifier.

Definition at line 589 of file `clifford_algebra_imp.h`.

References `PyClical::i`.

Referenced by `acosh()`, `asinh()`, `matrix_sqrt()`, `glucat::framed_multi< Scalar_T, LO, HI >::random()`, and `sqrt()`.

**5.2.3.119** `sqrt()` [4/4]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T, const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::sqrt (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Square root of multivector.

Definition at line 597 of file `clifford_algebra_imp.h`.

References `complexifier()`, and `sqrt()`.

**5.2.3.120** `star()` [1/3]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
Scalar_T glucat::star (
    const matrix_multi< Scalar_T, LO, HI > & lhs,
    const matrix_multi< Scalar_T, LO, HI > & rhs ) [inline]
```

Hestenes scalar product.

Definition at line 654 of file `matrix_multi_imp.h`.

**5.2.3.121** `star()` [2/3]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
Scalar_T glucat::star (
    const framed_multi< Scalar_T, LO, HI > & lhs,
    const framed_multi< Scalar_T, LO, HI > & rhs )
```

Hestenes scalar product.

Definition at line 855 of file `framed_multi_imp.h`.

**5.2.3.122 star()** [3/3]

```
template<template< typename, const index_t, const index_t > class Multivector, template<
typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO,
const index_t HI>
Scalar_T glucat::star (
    const Multivector< Scalar_T, LO, HI > & lhs,
    const RHS< Scalar_T, LO, HI > & rhs ) [inline]
```

Hestenes scalar product.

Definition at line 258 of file clifford\_algebra\_imp.h.

**5.2.3.123 tan()** [1/2]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::tan (
    const Multivector< Scalar_T, LO, HI > & val,
    const Multivector< Scalar_T, LO, HI > & i,
    const bool prechecked = false ) [inline]
```

Tangent of multivector with specified complexifier.

Definition at line 977 of file clifford\_algebra\_imp.h.

References check\_complex(), cos(), PyClical::i, scalar(), and sin().

Referenced by glucat::numeric\_traits< Scalar\_T >::tan(), and tan().

**5.2.3.124 tan()** [2/2]

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::tan (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Tangent of multivector.

Definition at line 996 of file clifford\_algebra\_imp.h.

References complexifier(), and tan().

**5.2.3.125 tanh()**

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T, const index_t LO, const index_t HI>
const Multivector< Scalar_T, LO, HI > glucat::tanh (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Hyperbolic tangent of multivector.

Definition at line 933 of file clifford\_algebra\_imp.h.

References cosh(), scalar(), and sinh().

Referenced by glucat::numeric\_traits< Scalar\_T >::tanh().

**5.2.3.126 to\_demote()**

```
template<typename Scalar_T >
numeric_traits<Scalar_T>::demoted::type glucat::to_demote (
    const Scalar_T & val ) [inline]
```

Cast to demote.

Definition at line 134 of file scalar\_imp.h.

References glucat::numeric\_traits< Scalar\_T >::to\_scalar\_t().

**5.2.3.127 to\_promote()**

```
template<typename Scalar_T >
numeric_traits<Scalar_T>::promoted::type glucat::to_promote (
    const Scalar_T & val ) [inline]
```

Cast to promote.

Definition at line 124 of file scalar\_imp.h.

References glucat::numeric\_traits< Scalar\_T >::to\_scalar\_t().

**5.2.3.128 try\_catch()** [1/2]

```
int glucat::try_catch (
    intfn f )
```

Exception catching for functions returning int.

Definition at line 49 of file try\_catch.h.

References PyClical::e().

Referenced by glucat::control\_t::call().

**5.2.3.129 try\_catch()** [2/2]

```
int glucat::try_catch (
    intintfn f,
    int arg )
```

Exception catching for functions of int returning int.

Definition at line 64 of file try\_catch.h.

References PyClical::e().

**5.2.3.130 vector\_part()**

```
template<template< typename, const index_t, const index_t > class Multivector, typename Scalar↵
_T , const index_t LO, const index_t HI>
const std::vector< Scalar_T > glucat::vector_part (
    const Multivector< Scalar_T, LO, HI > & val ) [inline]
```

Vector part of multivector, as a vector\_t with respect to frame()

Definition at line 443 of file clifford\_algebra\_imp.h.

**5.2.4 Variable Documentation****5.2.4.1 BITS\_PER\_SET\_VALUE**

```
const index_t glucat::BITS_PER_SET_VALUE = std::numeric_limits<set_value_t>::digits
```

Number of bits in set\_value\_t.

Definition at line 103 of file global.h.

**5.2.4.2 DEFAULT\_Basis\_Max\_Count**

```
const unsigned int glucat::DEFAULT_Basis_Max_Count = 12
```

Definition at line 130 of file global.h.

#### 5.2.4.3 DEFAULT\_Div\_Max\_Steps

```
const unsigned int glucat::DEFAULT_Div_Max_Steps = 4
```

Definition at line 126 of file global.h.

#### 5.2.4.4 DEFAULT\_Fast\_Size\_Threshold

```
const unsigned int glucat::DEFAULT_Fast_Size_Threshold = 1 << 6
```

Definition at line 131 of file global.h.

#### 5.2.4.5 DEFAULT\_Function\_Precision

```
const precision_t glucat::DEFAULT_Function_Precision = precision_same
```

Definition at line 134 of file global.h.

#### 5.2.4.6 DEFAULT\_HI

```
const index_t glucat::DEFAULT_HI = index_t(BITS_PER_SET_VALUE / 2)
```

Default highest index in an index set.

Definition at line 111 of file global.h.

#### 5.2.4.7 DEFAULT\_Inv\_Fast\_Dim\_Threshold

```
const unsigned int glucat::DEFAULT_Inv_Fast_Dim_Threshold = 1 << 3
```

Definition at line 132 of file global.h.

#### 5.2.4.8 DEFAULT\_Log\_Max\_Inner\_Steps

```
const unsigned int glucat::DEFAULT_Log_Max_Inner_Steps = 32
```

Definition at line 129 of file global.h.

#### 5.2.4.9 DEFAULT\_Log\_Max\_Outer\_Steps

```
const unsigned int glucat::DEFAULT_Log_Max_Outer_Steps = 256
```

Definition at line 128 of file global.h.

#### 5.2.4.10 DEFAULT\_Mult\_Matrix\_Threshold

```
const unsigned int glucat::DEFAULT_Mult_Matrix_Threshold = 8
```

Definition at line 125 of file global.h.

#### 5.2.4.11 DEFAULT\_Products\_Size\_Threshold

```
const unsigned int glucat::DEFAULT_Products_Size_Threshold = 1 << 22
```

Definition at line 133 of file global.h.

#### 5.2.4.12 DEFAULT\_Sqrt\_Max\_Steps

```
const unsigned int glucat::DEFAULT_Sqrt_Max_Steps = 256
```

Definition at line 127 of file global.h.

#### 5.2.4.13 DEFAULT\_TRUNCATION

```
const double glucat::DEFAULT_TRUNCATION = std::numeric_limits<float>::epsilon()
```

Default for truncation.

Definition at line 114 of file global.h.

#### 5.2.4.14 l\_ln2

```
const long double glucat::l_ln2 = 0.6931471805599453094172321214581766L [static]
```

Definition at line 41 of file long\_double.h.

Referenced by glucat::numeric\_traits< Scalar\_T >::ln\_2().

## 5.2.4.15 l\_pi

```
const long double glucat::l_pi = 3.1415926535897932384626433832795029L [static]
```

Definition at line 40 of file long\_double.h.

Referenced by glucat::numeric\_traits< Scalar\_T >::pi().

## 5.2.4.16 MS\_PER\_S

```
const double glucat::MS_PER_S = 1000.0
```

Timing constant: deprecated here - moved to [test/timing.h](#).

Definition at line 83 of file global.h.

## 5.3 glucat::gen Namespace Reference

### Classes

- class [generator\\_table](#)  
*Table of generators for specific signatures.*

### Typedefs

- typedef std::pair< [index\\_t](#), [index\\_t](#) > [signature\\_t](#)  
*A signature is a pair of indices, p, q, with p == frame.max(), q == -frame.min()*

### Variables

- static const [index\\_t](#) [offset\\_to\\_super](#) [] = {0,-1, 0,-1,-2, 3, 2, 1}  
*Offsets between the current signature and that of the real superalgebra.*

### 5.3.1 Typedef Documentation

## 5.3.1.1 signature\_t

```
typedef std::pair<index\_t, index\_t> glucat::gen::signature\_t
```

A signature is a pair of indices, p, q, with p == frame.max(), q == -frame.min()

Definition at line 43 of file generation.h.

### 5.3.2 Variable Documentation

#### 5.3.2.1 offset\_to\_super

```
const index_t glucat::gen::offset_to_super[] = {0,-1, 0,-1,-2, 3, 2, 1} [static]
```

Offsets between the current signature and that of the real superalgebra.

Definition at line 81 of file generation.h.

Referenced by glucat::matrix\_multi< Scalar\_T, LO, HI >::fast\_framed\_multi(), glucat::framed\_multi< Scalar\_T, LO, HI >::fast\_matrix\_multi(), and glucat::gen::generator\_table< Matrix\_T >::operator()().

## 5.4 glucat::matrix Namespace Reference

### Classes

- struct [eig\\_genus](#)  
*Structure containing classification of eigenvalues.*

### Enumerations

- enum [eig\\_case\\_t](#) { [safe\\_eig\\_case](#), [negative\\_eig\\_case](#), [both\\_eig\\_case](#) }  
*Classification of eigenvalues of a matrix.*

### Functions

- template<typename LHS\_T, typename RHS\_T >  
const RHS\_T [kron](#) (const LHS\_T &lhs, const RHS\_T &rhs)  
*Kronecker tensor product of matrices - as per Matlab kron.*
- template<typename LHS\_T, typename RHS\_T >  
const RHS\_T [mono\\_kron](#) (const LHS\_T &lhs, const RHS\_T &rhs)  
*Sparse Kronecker tensor product of monomial matrices.*
- template<typename LHS\_T, typename RHS\_T >  
const RHS\_T [nork](#) (const LHS\_T &lhs, const RHS\_T &rhs, const bool mono=true)  
*Left inverse of Kronecker product.*
- template<typename LHS\_T, typename RHS\_T >  
const RHS\_T [signed\\_perm\\_nork](#) (const LHS\_T &lhs, const RHS\_T &rhs)  
*Left inverse of Kronecker product where lhs is a signed permutation matrix.*
- template<typename Matrix\_T >  
Matrix\_T::size\_type [nnz](#) (const Matrix\_T &m)  
*Number of non-zeros.*
- template<typename Matrix\_T >  
bool [isnan](#) (const Matrix\_T &m)  
*Not a Number.*

- `template<typename Matrix_T >`  
`const Matrix_T unit (const typename Matrix_T::size_type n)`  
*Unit matrix - as per Matlab eye.*
- `template<typename LHS_T , typename RHS_T >`  
`const RHS_T::expression_type mono\_prod (const ublas::matrix_expression< LHS_T > &lhs, const ublas::matrix_expression< RHS_T > &rhs)`  
*Product of monomial matrices.*
- `template<typename LHS_T , typename RHS_T >`  
`const RHS_T::expression_type sparse\_prod (const ublas::matrix_expression< LHS_T > &lhs, const ublas::matrix_expression< RHS_T > &rhs)`  
*Product of sparse matrices.*
- `template<typename LHS_T , typename RHS_T >`  
`const RHS_T::expression_type prod (const ublas::matrix_expression< LHS_T > &lhs, const ublas::matrix_expression< RHS_T > &rhs)`  
*Product of matrices.*
- `template<typename Scalar_T , typename LHS_T , typename RHS_T >`  
`Scalar_T inner (const LHS_T &lhs, const RHS_T &rhs)`  
*Inner product:  $\sum(x(i,j)*y(i,j))/x.nrows()$*
- `template<typename Matrix_T >`  
`Matrix_T::value_type norm\_frob2 (const Matrix_T &val)`  
*Square of Frobenius norm.*
- `template<typename Matrix_T >`  
`Matrix_T::value_type trace (const Matrix_T &val)`  
*Matrix trace.*
- `template<typename Matrix_T >`  
`ublas::vector< std::complex< double > > eigenvalues (const Matrix_T &val)`  
*Eigenvalues of a matrix.*
- `template<typename Matrix_T >`  
`eig\_genus< Matrix_T > classify\_eigenvalues (const Matrix_T &val)`  
*Classify the eigenvalues of a matrix.*
- `template<typename LHS_T , typename RHS_T >`  
`void nork\_range (RHS_T &result, const typename LHS_T::const_iterator2 lhs_it2, const RHS_T &rhs, const typename RHS_T::size_type res_s1, const typename RHS_T::size_type res_s2)`  
*Utility routine for nork: calculate result for a range of indices.*
- `template<typename Matrix_T >`  
`static ublas::matrix< double, ublas::column_major > to\_lapack (const Matrix_T &val)`  
*Convert matrix to LAPACK format.*

## 5.4.1 Enumeration Type Documentation

### 5.4.1.1 eig\_case\_t

enum [glucat::matrix::eig\\_case\\_t](#)

Classification of eigenvalues of a matrix.

Enumerator

<code>safe_eig_case</code>	
<code>negative_eig_case</code>	
<code>both_eig_case</code>	

Definition at line 127 of file matrix.h.

## 5.4.2 Function Documentation

### 5.4.2.1 classify\_eigenvalues()

```
template<typename Matrix_T >
eig_genus< Matrix_T > glucat::matrix::classify_eigenvalues (
    const Matrix_T & val )
```

Classify the eigenvalues of a matrix.

Definition at line 526 of file matrix\_imp.h.

References glucat::abs(), both\_eig\_case, eigenvalues(), glucat::imag(), glucat::matrix::eig\_genus< Matrix\_T >::m\_eig\_case, glucat::matrix::eig\_genus< Matrix\_T >::m\_safe\_arg, negative\_eig\_case, glucat::norm(), glucat::numeric\_traits< Scalar\_T >::pi(), PyClical::pi, glucat::real(), and safe\_eig\_case.

Referenced by glucat::matrix\_log(), and glucat::matrix\_sqrt().

### 5.4.2.2 eigenvalues()

```
template<typename Matrix_T >
ublas::vector< std::complex< double > > glucat::matrix::eigenvalues (
    const Matrix_T & val )
```

Eigenvalues of a matrix.

Definition at line 493 of file matrix\_imp.h.

References to\_lapack().

Referenced by classify\_eigenvalues().

### 5.4.2.3 inner()

```
template<typename Scalar_T , typename LHS_T , typename RHS_T >
Scalar_T glucat::matrix::inner (
    const LHS_T & lhs,
    const RHS_T & rhs )
```

Inner product:  $\sum(x(i,j)*y(i,j))/x.nrows()$

Inner product:  $\sum(lhs(i,j)*rhs(i,j))/lhs.nrows()$

Definition at line 391 of file matrix\_imp.h.

## 5.4.2.4 isnan()

```
template<typename Matrix_T >
bool glucat::matrix::isnan (
    const Matrix_T & m )
```

Not a Number.

Definition at line 292 of file matrix\_imp.h.

Referenced by glucat::matrix\_log(), and glucat::operator/().

## 5.4.2.5 kron()

```
template<typename LHS_T , typename RHS_T >
const RHS_T glucat::matrix::kron (
    const LHS_T & lhs,
    const RHS_T & rhs )
```

Kronecker tensor product of matrices - as per Matlab kron.

Definition at line 73 of file matrix\_imp.h.

Referenced by glucat::framed\_multi< Scalar\_T, LO, HI >::fast().

## 5.4.2.6 mono\_kron()

```
template<typename LHS_T , typename RHS_T >
const RHS_T glucat::matrix::mono_kron (
    const LHS_T & lhs,
    const RHS_T & rhs )
```

Sparse Kronecker tensor product of monomial matrices.

Definition at line 116 of file matrix\_imp.h.

Referenced by glucat::gen::generator\_table< Matrix\_T >::gen\_from\_pm1\_qm1().

## 5.4.2.7 mono\_prod()

```
template<typename LHS_T , typename RHS_T >
const RHS_T::expression_type glucat::matrix::mono_prod (
    const ublas::matrix_expression< LHS_T > & lhs,
    const ublas::matrix_expression< RHS_T > & rhs )
```

Product of monomial matrices.

Definition at line 326 of file matrix\_imp.h.

Referenced by glucat::matrix\_multi< Scalar\_T, LO, HI >::basis\_element(), glucat::gen::generator\_table< Matrix\_T >::gen\_from\_pm4\_qp4(), glucat::gen::generator\_table< Matrix\_T >::gen\_from\_pp4\_qm4(), and glucat::gen::generator\_table< Matrix\_T >::gen\_from\_qp1\_pm1().

#### 5.4.2.8 nnz()

```
template<typename Matrix_T >
Matrix_T::size_type glucat::matrix::nnz (
    const Matrix_T & m )
```

Number of non-zeros.

Definition at line 269 of file matrix\_imp.h.

Referenced by glucat::framed\_multi< Scalar\_T, LO, HI >::framed\_multi().

#### 5.4.2.9 nork()

```
template<typename LHS_T , typename RHS_T >
const RHS_T glucat::matrix::nork (
    const LHS_T & lhs,
    const RHS_T & rhs,
    const bool mono = true )
```

Left inverse of Kronecker product.

Definition at line 188 of file matrix\_imp.h.

References norm\_frob2().

#### 5.4.2.10 nork\_range()

```
template<typename LHS_T , typename RHS_T >
void glucat::matrix::nork_range (
    RHS_T & result,
    const typename LHS_T::const_iterator2 lhs_it2,
    const RHS_T & rhs,
    const typename RHS_T::size_type res_s1,
    const typename RHS_T::size_type res_s2 )
```

Utility routine for nork: calculate result for a range of indices.

Definition at line 155 of file matrix\_imp.h.

References glucat::numeric\_traits< Scalar\_T >::to\_scalar\_t().

## 5.4.2.11 norm\_frob2()

```
template<typename Matrix_T >
Matrix_T::value_type glucat::matrix::norm_frob2 (
    const Matrix_T & val )
```

Square of Frobenius norm.

Definition at line 413 of file matrix\_imp.h.

Referenced by nork().

## 5.4.2.12 prod()

```
template<typename LHS_T , typename RHS_T >
const RHS_T::expression_type glucat::matrix::prod (
    const ublas::matrix_expression< LHS_T > & lhs,
    const ublas::matrix_expression< RHS_T > & rhs ) [inline]
```

Product of matrices.

Definition at line 373 of file matrix\_imp.h.

## 5.4.2.13 signed\_perm\_nork()

```
template<typename LHS_T , typename RHS_T >
const RHS_T glucat::matrix::signed_perm_nork (
    const LHS_T & lhs,
    const RHS_T & rhs )
```

Left inverse of Kronecker product where lhs is a signed permutation matrix.

Definition at line 237 of file matrix\_imp.h.

Referenced by glucat::fast().

## 5.4.2.14 sparse\_prod()

```
template<typename LHS_T , typename RHS_T >
const RHS_T::expression_type glucat::matrix::sparse_prod (
    const ublas::matrix_expression< LHS_T > & lhs,
    const ublas::matrix_expression< RHS_T > & rhs ) [inline]
```

Product of sparse matrices.

Definition at line 362 of file matrix\_imp.h.

#### 5.4.2.15 to\_lapack()

```
template<typename Matrix_T >
static ublas::matrix<double, ublas::column_major> glucat::matrix::to_lapack (
    const Matrix_T & val ) [static]
```

Convert matrix to LAPACK format.

Definition at line 461 of file matrix\_imp.h.

Referenced by eigenvalues().

#### 5.4.2.16 trace()

```
template<typename Matrix_T >
Matrix_T::value_type glucat::matrix::trace (
    const Matrix_T & val )
```

Matrix trace.

Definition at line 437 of file matrix\_imp.h.

References glucat::numeric\_traits< Scalar\_T >::NaN().

#### 5.4.2.17 unit()

```
template<typename Matrix_T >
const Matrix_T glucat::matrix::unit (
    const typename Matrix_T::size_type n ) [inline]
```

Unit matrix - as per Matlab eye.

Definition at line 317 of file matrix\_imp.h.

## 5.5 glucat::timing Namespace Reference

### Functions

- static double [elapsed](#) (clock\_t cpu\_time)  
*Elapsed time in milliseconds.*

### Variables

- const double [MS\\_PER\\_SEC](#) = 1000.0  
*Timing constant: milliseconds per second.*
- const double [MS\\_PER\\_CLOCK](#) = [MS\\_PER\\_SEC](#) / double(CLOCKS\_PER\_SEC)  
*Timing constant: milliseconds per clock.*
- const int [EXTRA\\_TRIALS](#) = 2  
*Timing constant: trial expansion factor.*

## 5.5.1 Function Documentation

### 5.5.1.1 elapsed()

```
static double glucat::timing::elapsed (  
    clock_t cpu_time ) [inline], [static]
```

Elapsed time in milliseconds.

Definition at line 51 of file timing.h.

References `MS_PER_CLOCK`.

## 5.5.2 Variable Documentation

### 5.5.2.1 EXTRA\_TRIALS

```
const int glucat::timing::EXTRA_TRIALS = 2
```

Timing constant: trial expansion factor.

Definition at line 45 of file timing.h.

### 5.5.2.2 MS\_PER\_CLOCK

```
const double glucat::timing::MS_PER_CLOCK = MS\_PER\_SEC / double(CLOCKS_PER_SEC)
```

Timing constant: milliseconds per clock.

Definition at line 42 of file timing.h.

Referenced by `elapsed()`.

### 5.5.2.3 MS\_PER\_SEC

```
const double glucat::timing::MS_PER_SEC = 1000.0
```

Timing constant: milliseconds per second.

Definition at line 39 of file timing.h.

## 5.6 PyClical Namespace Reference

### Classes

- class [clifford](#)
- class [index\\_set](#)

### Functions

- def [index\\_set\\_hidden\\_doctests](#) ()
- def [clifford\\_hidden\\_doctests](#) ()
- def [e](#) (obj)
- def [istpq](#) (p, q)
- def [\\_test](#) ()

### Variables

- string [\\_\\_version\\_\\_](#) = "0.8.2"
- [obj](#)
- [i](#)
- [ixt](#)
- [fill](#)
- float [tau](#) = atan([clifford](#)(1.0)) \* 8.0
- float [pi](#) = [tau](#) / 2.0
- [cl](#) = [clifford](#)
- [ist](#) = [index\\_set](#)
- def [ninf3](#) = [e](#)(4) + [e](#)(-1)
- def [nbar3](#) = [e](#)(4) - [e](#)(-1)

### 5.6.1 Function Documentation

#### 5.6.1.1 [\\_test\(\)](#)

```
def PyClical._test ( ) [private]
```

Definition at line 1913 of file PyClical.pyx.

## 5.6.1.2 clifford\_hidden\_doctests()

```
def PyClical.clifford_hidden_doctests ( )
```

Tests for functions that Doctest cannot see.

For clifford.\_\_cinit\_\_: Construct an object of type clifford.

```
>>> print clifford(2)
2
>>> print clifford(2L)
2
>>> print clifford(2.0)
2
>>> print clifford(1.0e-1)
0.1
>>> print clifford("2")
2
>>> print clifford("2{1,2,3}")
2{1,2,3}
>>> print clifford(clifford("2{1,2,3}"))
2{1,2,3}
>>> print clifford("-{1}")
-{1}
>>> print clifford(2,index_set({1,2}))
2{1,2}
>>> print clifford([2,3],index_set({1,2}))
2{1}+3{2}
>>> print clifford([1,2])
Traceback (most recent call last):
...
TypeError: Cannot initialize clifford object from <type 'list'>.
>>> print clifford(None)
Traceback (most recent call last):
...
TypeError: Cannot initialize clifford object from <type 'NoneType'>.
>>> print clifford(None,[1,2])
Traceback (most recent call last):
...
TypeError: Cannot initialize clifford object from (<type 'NoneType'>, <type 'list'>).
>>> print clifford([1,2],[1,2])
Traceback (most recent call last):
...
TypeError: Cannot initialize clifford object from (<type 'list'>, <type 'list'>).
>>> print clifford("")
Traceback (most recent call last):
...
ValueError: Cannot initialize clifford object from invalid string ''.
>>> print clifford("{")
Traceback (most recent call last):
...
ValueError: Cannot initialize clifford object from invalid string '{'.
>>> print clifford("{1}")
Traceback (most recent call last):
...
ValueError: Cannot initialize clifford object from invalid string '{1'.
>>> print clifford("{+")
Traceback (most recent call last):
...
ValueError: Cannot initialize clifford object from invalid string '{+'.
>>> print clifford("-")
Traceback (most recent call last):
...
ValueError: Cannot initialize clifford object from invalid string '-'.
>>> print clifford("{1}+")
Traceback (most recent call last):
...
ValueError: Cannot initialize clifford object from invalid string '{1}+'.

```

For clifford.\_\_richcmp\_\_: Compare objects of type clifford.

```

>>> clifford("{1}") == clifford("1{1}")
True
>>> clifford("{1}") != clifford("1.0{1}")
False
>>> clifford("{1}") != clifford("1.0")
True
>>> clifford("{1,2}") == None
False
>>> clifford("{1,2}") != None
True
>>> None == clifford("{1,2}")
False
>>> None != clifford("{1,2}")
True

```

Definition at line 1243 of file PyClicl.pyx.

#### 5.6.1.3 e()

```

def PyClicl.e (
    obj )

```

Abbreviation for `clifford(index_set(obj))`.

```

>>> print e(1)
{1}
>>> print e(-1)
{-1}
>>> print e(0)
1

```

Definition at line 1887 of file PyClicl.pyx.

Referenced by `glucat::matrix_multi< Scalar_T, LO, HI >.basis_element()`, `clifford_to_str()`, `glucat::framed_multi< Scalar_T, LO, HI >.framed_multi()`, `glucat::matrix_multi< Scalar_T, LO, HI >.matrix_multi()`, and `glucat.try_catch()`.

#### 5.6.1.4 index\_set\_hidden\_doctests()

```

def PyClicl.index_set_hidden_doctests ( )

```

Tests for functions that Doctest cannot see.

For `index_set.__cinit__`: Construct `index_set`.

```

>>> print index_set(1)
{1}
>>> print index_set({1,2})
{1,2}
>>> print index_set(index_set({1,2}))
{1,2}
>>> print index_set({1,2})
{1,2}
>>> print index_set({1,2,1})
{1,2}
>>> print index_set({1,2,1})
{1,2}

```

```

>>> print index_set("")
{}
>>> print index_set("{}")
Traceback (most recent call last):
...
ValueError: Cannot initialize index_set object from invalid string '{}'.
>>> print index_set("{1}")
Traceback (most recent call last):
...
ValueError: Cannot initialize index_set object from invalid string '{1}'.
>>> print index_set("{1,2,100}")
Traceback (most recent call last):
...
ValueError: Cannot initialize index_set object from invalid string '{1,2,100}'.
>>> print index_set({1,2,100})
Traceback (most recent call last):
...
IndexError: Cannot initialize index_set object from invalid set([1, 2, 100]).
>>> print index_set([1,2])
Traceback (most recent call last):
...
TypeError: Cannot initialize index_set object from <type 'list'>.

For index_set.__richcmp__: Compare two objects of class index_set.

>>> index_set(1) == index_set({1})
True
>>> index_set({1}) != index_set({1})
False
>>> index_set({1}) != index_set({2})
True
>>> index_set({1}) == index_set({2})
False
>>> index_set({1}) < index_set({2})
True
>>> index_set({1}) <= index_set({2})
True
>>> index_set({1}) > index_set({2})
False
>>> index_set({1}) >= index_set({2})
False
>>> None == index_set({1,2})
False
>>> None != index_set({1,2})
True
>>> None < index_set({1,2})
False
>>> None <= index_set({1,2})
False
>>> None > index_set({1,2})
False
>>> None >= index_set({1,2})
False
>>> index_set({1,2}) == None
False
>>> index_set({1,2}) != None
True
>>> index_set({1,2}) < None
False
>>> index_set({1,2}) <= None
False
>>> index_set({1,2}) > None
False
>>> index_set({1,2}) >= None
False

```

Definition at line 404 of file PyClical.pyx.

#### 5.6.1.5 istpq()

```
def PyClical.istpq (
    p,
    q )
```

Abbreviation for `index_set({-q,...p})`.

```
>>> print istpq(2,3)
{-3,-2,-1,1,2}
```

Definition at line 1900 of file PyClical.pyx.

### 5.6.2 Variable Documentation

#### 5.6.2.1 \_\_version\_\_

```
string PyClical.__version__ = "0.8.2" [private]
```

Definition at line 32 of file PyClical.pyx.

#### 5.6.2.2 cl

```
PyClical.cl = clifford
```

Definition at line 1859 of file PyClical.pyx.

Referenced by `cga3.agc3()`, `cga3.cga3()`, and `cga3.cga3std()`.

#### 5.6.2.3 fill

```
PyClical.fill
```

Definition at line 1815 of file PyClical.pyx.

Referenced by `glucat::matrix_multi< Scalar_T, LO, HI >.random()`, and `glucat::framed_multi< Scalar_T, LO, HI >.random()`.

#### 5.6.2.4 i

`PyClical.i`

Definition at line 1542 of file `PyClical.pyx`.

Referenced by `glucat.acos()`, `glucat.acosh()`, `glucat.asin()`, `glucat.asinh()`, `glucat.atan()`, `glucat.atanh()`, `glucat.check_complex()`, `glucat.cos()`, `glucat.log()`, `glucat.matrix_log()`, `glucat.matrix_sqrt()`, `glucat.operator<<()`, `glucat.operator>>()`, `glucat.sin()`, `glucat.sqrt()`, and `glucat.tan()`.

#### 5.6.2.5 ist

`PyClical.ist = index_set`

Definition at line 1879 of file `PyClical.pyx`.

Referenced by `cga3.agc3()`, `glucat::matrix_multi< Scalar_T, LO, HI >.basis_element()`, `glucat::framed_multi< Scalar_T, LO, HI >.centre_pm4_qp4()`, `glucat::framed_multi< Scalar_T, LO, HI >.centre_pp4_qm4()`, `glucat::framed_multi< Scalar_T, LO, HI >.centre_qp1_pm1()`, `cga3.cga3()`, `cga3.cga3std()`, `glucat::framed_multi< Scalar_T, LO, HI >.divide()`, `glucat::framed_multi< Scalar_T, LO, HI >.framed_multi()`, `index_set_to_repr()`, `index_set_to_str()`, `glucat::matrix_multi< Scalar_T, LO, HI >.matrix_multi()`, `glucat.max_pos()`, `glucat.min_neg()`, `glucat.operator<<()`, and `glucat.operator>>()`.

#### 5.6.2.6 ixt

`PyClical.ixt`

Definition at line 1815 of file `PyClical.pyx`.

#### 5.6.2.7 nbar3

`def PyClical.nbar3 = e(4) - e(-1)`

Definition at line 1910 of file `PyClical.pyx`.

#### 5.6.2.8 ninf3

`def PyClical.ninf3 = e(4) + e(-1)`

Definition at line 1909 of file `PyClical.pyx`.

Referenced by `cga3.cga3()`, and `cga3.cga3std()`.

### 5.6.2.9 obj

`PyClical.obj`

Definition at line 1542 of file `PyClical.pyx`.

### 5.6.2.10 pi

```
float PyClical.pi = tau / 2.0
```

Definition at line 1857 of file `PyClical.pyx`.

Referenced by `glucat::matrix.classify_eigenvalues()`, `glucat.cos()`, `glucat.log()`, `glucat.matrix_log()`, and `glucat.sin()`.

### 5.6.2.11 tau

```
float PyClical.tau = atan(clifford(1.0)) * 8.0
```

Definition at line 1856 of file `PyClical.pyx`.

## 5.7 std Namespace Reference

### Classes

- struct `numeric_limits< glucat::framed_multi< Scalar_T, LO, HI > >`  
*Numeric limits for framed\_multi inherit limits for the corresponding scalar type.*
- struct `numeric_limits< glucat::matrix_multi< Scalar_T, LO, HI > >`  
*Numeric limits for matrix\_multi inherit limits for the corresponding scalar type.*

## Chapter 6

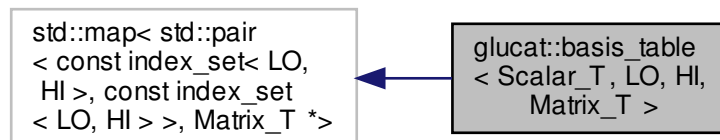
# Class Documentation

### 6.1 `glucat::basis_table< Scalar_T, LO, HI, Matrix_T >` Class Template Reference

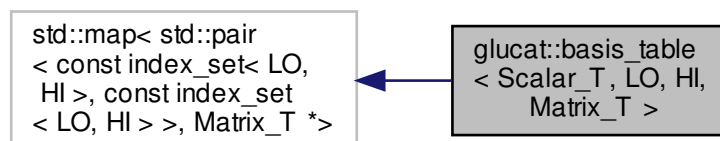
Table of basis elements used as a cache by `basis_element()`

```
#include <matrix_multi_imp.h>
```

Inheritance diagram for `glucat::basis_table< Scalar_T, LO, HI, Matrix_T >`:



Collaboration diagram for `glucat::basis_table< Scalar_T, LO, HI, Matrix_T >`:



## Static Public Member Functions

- static [basis\\_table](#) & [basis](#) ()  
*Single instance of basis table.*

## Private Member Functions

- [basis\\_table](#) ()
- [~basis\\_table](#) ()
- [basis\\_table](#) (const [basis\\_table](#) &)
- [basis\\_table](#) & [operator=](#) (const [basis\\_table](#) &)

## Friends

- class [friend\\_for\\_private\\_destructor](#)

### 6.1.1 Detailed Description

```
template<typename Scalar_T, const index_t LO, const index_t HI, typename Matrix_T>
class glucat::basis_table< Scalar_T, LO, HI, Matrix_T >
```

Table of basis elements used as a cache by [basis\\_element](#)()

Definition at line 1218 of file [matrix\\_multi\\_imp.h](#).

### 6.1.2 Constructor & Destructor Documentation

#### 6.1.2.1 [basis\\_table](#)() [1/2]

```
template<typename Scalar_T , const index_t LO, const index_t HI, typename Matrix_T >
glucat::basis_table< Scalar_T, LO, HI, Matrix_T >::basis_table ( ) [inline], [private]
```

Definition at line 1228 of file [matrix\\_multi\\_imp.h](#).

#### 6.1.2.2 [~basis\\_table](#)()

```
template<typename Scalar_T , const index_t LO, const index_t HI, typename Matrix_T >
glucat::basis_table< Scalar_T, LO, HI, Matrix_T >::~basis_table ( ) [inline], [private]
```

Definition at line 1229 of file [matrix\\_multi\\_imp.h](#).

### 6.1.2.3 basis\_table() [2/2]

```
template<typename Scalar_T , const index_t LO, const index_t HI, typename Matrix_T >
glucat::basis_table< Scalar_T, LO, HI, Matrix_T >::basis_table (
    const basis_table< Scalar_T, LO, HI, Matrix_T > & ) [private]
```

## 6.1.3 Member Function Documentation

### 6.1.3.1 basis()

```
template<typename Scalar_T , const index_t LO, const index_t HI, typename Matrix_T >
static basis_table& glucat::basis_table< Scalar_T, LO, HI, Matrix_T >::basis ( ) [inline],
[static]
```

Single instance of basis table.

Definition at line 1224 of file matrix\_multi\_imp.h.

### 6.1.3.2 operator=()

```
template<typename Scalar_T , const index_t LO, const index_t HI, typename Matrix_T >
basis_table& glucat::basis_table< Scalar_T, LO, HI, Matrix_T >::operator= (
    const basis_table< Scalar_T, LO, HI, Matrix_T > & ) [private]
```

## 6.1.4 Friends And Related Function Documentation

### 6.1.4.1 friend\_for\_private\_destructor

```
template<typename Scalar_T , const index_t LO, const index_t HI, typename Matrix_T >
friend class friend_for_private_destructor [friend]
```

Friend declaration to avoid compiler warning: "... only defines a private destructor and has no friends" Ref: Carlos O'Ryan, ACE <http://doc.ece.uci.edu>

Definition at line 1236 of file matrix\_multi\_imp.h.

The documentation for this class was generated from the following file:

- glucat/[matrix\\_multi\\_imp.h](#)

## 6.2 glucat::bool\_to\_type< truth\_value > Class Template Reference

Bool to type.

```
#include <global.h>
```

### Private Types

- enum { [value](#) = truth\_value }

### 6.2.1 Detailed Description

```
template<bool truth_value>  
class glucat::bool_to_type< truth_value >
```

Bool to type.

Definition at line 69 of file global.h.

### 6.2.2 Member Enumeration Documentation

#### 6.2.2.1 anonymous enum

```
template<bool truth_value>  
anonymous enum [private]
```

#### Enumerator

value	
-------	--

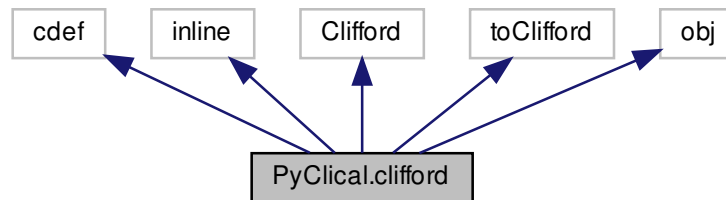
Definition at line 72 of file global.h.

The documentation for this class was generated from the following file:

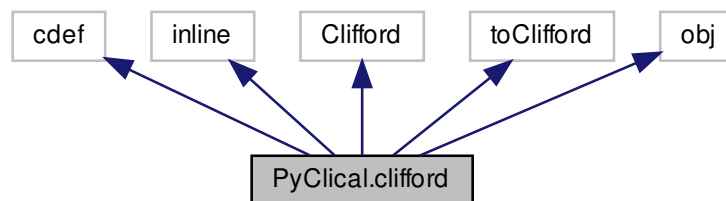
- [glucat/global.h](#)

## 6.3 PyClical.clifford Class Reference

Inheritance diagram for PyClical.clifford:



Collaboration diagram for PyClical.clifford:



### Public Member Functions

- def `__cinit__` (self, other=0, [ixt](#)=None)
- def `__dealloc__` (self)
- def `__contains__` (self, x)
- def `__iter__` (self)
- def `reframe` (self, [ixt](#))
- def `__richcmp__` (lhs, rhs, int, op)
- def `__getitem__` (self, [ixt](#))
- def `__neg__` (self)
- def `__pos__` (self)
- def `__add__` (lhs, rhs)
- def `__iadd__` (self, rhs)
- def `__sub__` (lhs, rhs)
- def `__isub__` (self, rhs)
- def `__mul__` (lhs, rhs)
- def `__imul__` (self, rhs)
- def `__mod__` (lhs, rhs)
- def `__imod__` (self, rhs)

- def [\\_\\_and\\_\\_](#) (lhs, rhs)
- def [\\_\\_iand\\_\\_](#) (self, rhs)
- def [\\_\\_xor\\_\\_](#) (lhs, rhs)
- def [\\_\\_ixor\\_\\_](#) (self, rhs)
- def [\\_\\_div\\_\\_](#) (lhs, rhs)
- def [\\_\\_idiv\\_\\_](#) (self, rhs)
- def [inv](#) (self)
- def [\\_\\_or\\_\\_](#) (lhs, rhs)
- def [\\_\\_ior\\_\\_](#) (self, rhs)
- def [\\_\\_pow\\_\\_](#) (self, m, dummy)
- def [pow](#) (self, m)
- def [outer\\_pow](#) (self, m)
- def [\\_\\_call\\_\\_](#) (self, grade)
- def [scalar](#) (self)
- def [pure](#) (self)
- def [even](#) (self)
- def [odd](#) (self)
- def [vector\\_part](#) (self, frm=None)
- def [involute](#) (self)
- def [reverse](#) (self)
- def [conj](#) (self)
- def [quad](#) (self)
- def [norm](#) (self)
- def [abs](#) (self)
- def [max\\_abs](#) (self)
- def [truncated](#) (self, limit)
- def [isnan](#) (self)
- def [frame](#) (self)
- def [\\_\\_repr\\_\\_](#) (self)
- def [\\_\\_str\\_\\_](#) (self)

## Public Attributes

- [instance](#)

### 6.3.1 Detailed Description

Python class `clifford` wraps C++ class `Clifford`.

Definition at line 532 of file `PyClical.pyx`.

### 6.3.2 Member Function Documentation

**6.3.2.1 `__add__()`**

```
def PyClical.clifford.__add__ (
    lhs,
    rhs )

Geometric sum.

>>> print clifford(1) + clifford("{2}")
1+{2}
>>> print clifford("{1}") + clifford("{2}")
{1}+{2}
```

Definition at line 739 of file PyClical.pyx.

**6.3.2.2 `__and__()`**

```
def PyClical.clifford.__and__ (
    lhs,
    rhs )

Inner product.

>>> print clifford("{1}") & clifford("{2}")
0
>>> print clifford(2) & clifford("{2}")
0
>>> print clifford("{1}") & clifford("{1}")
1
>>> print clifford("{1}") & clifford("{1,2}")
{2}
```

Definition at line 835 of file PyClical.pyx.

**6.3.2.3 `__call__()`**

```
def PyClical.clifford.__call__ (
    self,
    grade )

Pure grade-vector part.

>>> print clifford("{1}") (1)
{1}
>>> print clifford("{1}") (0)
0
>>> print clifford("1+{1}+{1,2}") (0)
1
>>> print clifford("1+{1}+{1,2}") (1)
{1}
>>> print clifford("1+{1}+{1,2}") (2)
{1,2}
>>> print clifford("1+{1}+{1,2}") (3)
0
```

Definition at line 1019 of file PyClical.pyx.

References `PyClical.index_set.instance`, and `PyClical.clifford.instance`.

#### 6.3.2.4 `__cinit__()`

```
def PyClical.clifford.__cinit__ (
    self,
    other = 0,
    ixt = None )
```

Construct an object of type clifford.

```
>>> print clifford(2)
2
>>> print clifford(2L)
2
>>> print clifford(2.0)
2
>>> print clifford(1.0e-1)
0.1
>>> print clifford("2")
2
>>> print clifford("2{1,2,3}")
2{1,2,3}
>>> print clifford(clifford("2{1,2,3}"))
2{1,2,3}
>>> print clifford("-{1}")
-{1}
>>> print clifford(2,index_set ({1,2}))
2{1,2}
>>> print clifford([2,3],index_set ({1,2}))
2{1}+3{2}
```

Definition at line 563 of file PyClical.pyx.

#### 6.3.2.5 `__contains__()`

```
def PyClical.clifford.__contains__ (
    self,
    x )
```

Not applicable.

```
>>> x=clifford(index_set ({-3,4,7})); -3 in x
Traceback (most recent call last):
...
TypeError: Not applicable.
```

Definition at line 626 of file PyClical.pyx.

#### 6.3.2.6 `__dealloc__()`

```
def PyClical.clifford.__dealloc__ (
    self )
```

Clean up by deallocating the instance of C++ class Clifford.

Definition at line 620 of file PyClical.pyx.

References `PyClical.index_set.instance`, and `PyClical.clifford.instance`.

**6.3.2.7 `__div__()`**

```
def PyClical.clifford.__div__ (
    lhs,
    rhs )
```

Geometric quotient.

```
>>> print clifford("{1}") / clifford("{2}")
{1,2}
>>> print clifford(2) / clifford("{2}")
2{2}
>>> print clifford("{1}") / clifford("{1}")
1
>>> print clifford("{1}") / clifford("{1,2}")
-{2}
```

Definition at line 895 of file PyClical.pyx.

**6.3.2.8 `__getitem__()`**

```
def PyClical.clifford.__getitem__ (
    self,
    ixt )
```

Subscripting: map from index set to scalar coordinate.

```
>>> clifford("{1}") [index_set(1)]
1.0
>>> clifford("{1}") [index_set({1})]
1.0
>>> clifford("{1}") [index_set({1,2})]
0.0
>>> clifford("2{1,2}") [index_set({1,2})]
2.0
```

Definition at line 706 of file PyClical.pyx.

References `PyClical.index_set.instance`, and `PyClical.clifford.instance`.

**6.3.2.9 `__iadd__()`**

```
def PyClical.clifford.__iadd__ (
    self,
    rhs )
```

Geometric sum.

```
>>> x = clifford(1); x += clifford("{2}"); print x
1+{2}
```

Definition at line 750 of file PyClical.pyx.

**6.3.2.10** `__iand__()`

```
def PyClical.clifford.__iand__ (
    self,
    rhs )
```

Inner product.

```
>>> x = clifford("{1}"); x &= clifford("{2}"); print x
0
>>> x = clifford(2); x &= clifford("{2}"); print x
0
>>> x = clifford("{1}"); x &= clifford("{1}"); print x
1
>>> x = clifford("{1}"); x &= clifford("{1,2}"); print x
{2}
```

Definition at line 850 of file PyClical.pyx.

**6.3.2.11** `__idiv__()`

```
def PyClical.clifford.__idiv__ (
    self,
    rhs )
```

Geometric quotient.

```
>>> x = clifford("{1}"); x /= clifford("{2}"); print x
{1,2}
>>> x = clifford(2); x /= clifford("{2}"); print x
2{2}
>>> x = clifford("{1}"); x /= clifford("{1}"); print x
1
>>> x = clifford("{1}"); x /= clifford("{1,2}"); print x
-{2}
```

Definition at line 910 of file PyClical.pyx.

**6.3.2.12** `__imod__()`

```
def PyClical.clifford.__imod__ (
    self,
    rhs )
```

Contraction.

```
>>> x = clifford("{1}"); x %= clifford("{2}"); print x
0
>>> x = clifford(2); x %= clifford("{2}"); print x
2{2}
>>> x = clifford("{1}"); x %= clifford("{1}"); print x
1
>>> x = clifford("{1}"); x %= clifford("{1,2}"); print x
{2}
```

Definition at line 820 of file PyClical.pyx.

**6.3.2.13** `__imul__()`

```
def PyClical.clifford.__imul__ (
    self,
    rhs )
```

Geometric product.

```
>>> x = clifford(2); x *= clifford("{2}"); print x
2{2}
>>> x = clifford("{1}"); x *= clifford("{2}"); print x
{1,2}
>>> x = clifford("{1}"); x *= clifford("{1,2}"); print x
{2}
```

Definition at line 792 of file PyClical.pyx.

**6.3.2.14** `__ior__()`

```
def PyClical.clifford.__ior__ (
    self,
    rhs )
```

Transform left hand side, using right hand side as a transformation.

```
>>> x=clifford("{1,2}") * pi/2; y=clifford("{1}"); y|=x; print y
-{1}
>>> x=clifford("{1,2}") * pi/2; y=clifford("{1}"); y|=exp(x); print y
-{1}
```

Definition at line 949 of file PyClical.pyx.

**6.3.2.15** `__isub__()`

```
def PyClical.clifford.__isub__ (
    self,
    rhs )
```

Geometric difference.

```
>>> x = clifford(1); x -= clifford("{2}"); print x
1-{2}
```

Definition at line 770 of file PyClical.pyx.

**6.3.2.16** `__iter__()`

```
def PyClical.clifford.__iter__ (
    self )
```

Not applicable.

```
>>> for a in clifford(index_set({-3,4,7})): print a,
Traceback (most recent call last):
...
TypeError: Not applicable.
```

Definition at line 637 of file PyClical.pyx.

**6.3.2.17** `__ixor__()`

```
def PyClical.clifford.__ixor__ (
    self,
    rhs )
```

Outer product.

```
>>> x = clifford("{1}"); x ^= clifford("{2}"); print x
{1,2}
>>> x = clifford(2); x ^= clifford("{2}"); print x
2{2}
>>> x = clifford("{1}"); x ^= clifford("{1}"); print x
0
>>> x = clifford("{1}"); x ^= clifford("{1,2}"); print x
0
```

Definition at line 880 of file PyClical.pyx.

**6.3.2.18** `__mod__()`

```
def PyClical.clifford.__mod__ (
    lhs,
    rhs )
```

Contraction.

```
>>> print clifford("{1}") % clifford("{2}")
0
>>> print clifford(2) % clifford("{2}")
2{2}
>>> print clifford("{1}") % clifford("{1}")
1
>>> print clifford("{1}") % clifford("{1,2}")
{2}
```

Definition at line 805 of file PyClical.pyx.

**6.3.2.19 `__mul__()`**

```
def PyClical.clifford.__mul__ (
    lhs,
    rhs )
```

Geometric product.

```
>>> print clifford("{1}") * clifford("{2}")
{1,2}
>>> print clifford(2) * clifford("{2}")
2{2}
>>> print clifford("{1}") * clifford("{1,2}")
{2}
```

Definition at line 779 of file PyClical.pyx.

**6.3.2.20 `__neg__()`**

```
def PyClical.clifford.__neg__ (
    self )
```

Unary `-`.

```
>>> print -clifford("{1}")
-{1}
```

Definition at line 721 of file PyClical.pyx.

References `PyClical.index_set.instance`, and `PyClical.clifford.instance`.

**6.3.2.21 `__or__()`**

```
def PyClical.clifford.__or__ (
    lhs,
    rhs )
```

Transform left hand side, using right hand side as a transformation.

```
>>> x=clifford("{1,2}") * pi/2; y=clifford("{1}"); print y|x
-{1}
>>> x=clifford("{1,2}") * pi/2; y=clifford("{1}"); print y|exp(x)
-{1}
```

Definition at line 938 of file PyClical.pyx.

**6.3.2.22 \_\_pos\_\_()**

```
def PyClical.clifford.__pos__ (
    self )
```

Unary +.

```
>>> print +clifford("{1}")
{1}
```

Definition at line 730 of file PyClical.pyx.

**6.3.2.23 \_\_pow\_\_()**

```
def PyClical.clifford.__pow__ (
    self,
    m,
    dummy )
```

Power: self to the m.

```
>>> x=clifford("{1}"); print x ** 2
1
>>> x=clifford("2"); print x ** 2
4
>>> x=clifford("2+{1}"); print x ** 0
1
>>> x=clifford("2+{1}"); print x ** 1
2+{1}
>>> x=clifford("2+{1}"); print x ** 2
5+4{1}
>>> i=clifford("{1,2}");print exp(pi/2) * (i ** i)
1
```

Definition at line 960 of file PyClical.pyx.

References PyClical.clifford.pow().

**6.3.2.24 \_\_repr\_\_()**

```
def PyClical.clifford.__repr__ (
    self )
```

The "official" string representation of self.

```
>>> clifford("1+3{-1}+2{1,2}+4{-2,7}").__repr__()
'clifford("1+3{-1}+2{1,2}+4{-2,7}")'
```

Definition at line 1225 of file PyClical.pyx.

References clifford\_to\_repr().

**6.3.2.25** `__richcmp__()`

```
def PyClical.clifford.__richcmp__ (
    lhs,
    rhs,
    int,
    op )
```

Compare objects of type clifford.

```
>>> clifford("{1}") == clifford("1{1}")
True
>>> clifford("{1}") != clifford("1.0{1}")
False
>>> clifford("{1}") != clifford("1.0")
True
>>> clifford("{1,2}") == None
False
>>> clifford("{1,2}") != None
True
>>> None == clifford("{1,2}")
False
>>> None != clifford("{1,2}")
True
```

Definition at line 671 of file PyClical.pyx.

**6.3.2.26** `__str__()`

```
def PyClical.clifford.__str__ (
    self )
```

The “informal” string representation of self.

```
>>> clifford("1+3{-1}+2{1,2}+4{-2,7}").__str__()
'1+3{-1}+2{1,2}+4{-2,7}'
```

Definition at line 1234 of file PyClical.pyx.

References `clifford_to_str()`.

**6.3.2.27** `__sub__()`

```
def PyClical.clifford.__sub__ (
    lhs,
    rhs )
```

Geometric difference.

```
>>> print clifford(1) - clifford("{2}")
1-{2}
>>> print clifford("{1}") - clifford("{2}")
{1}-{2}
```

Definition at line 759 of file PyClical.pyx.

**6.3.2.28 `__xor__()`**

```
def PyClical.clifford.__xor__ (
    lhs,
    rhs )
```

Outer product.

```
>>> print clifford("{1}") ^ clifford("{2}")
{1,2}
>>> print clifford(2) ^ clifford("{2}")
2{2}
>>> print clifford("{1}") ^ clifford("{1}")
0
>>> print clifford("{1}") ^ clifford("{1,2}")
0
```

Definition at line 865 of file PyClical.pyx.

**6.3.2.29 `abs()`**

```
def PyClical.clifford.abs (
    self )
```

Absolute value: square root of norm.

```
>>> clifford("1+{-1}+{1,2}+{1,2,3}").abs()
2.0
```

Definition at line 1174 of file PyClical.pyx.

References `glucat.abs()`.

**6.3.2.30 `conj()`**

```
def PyClical.clifford.conj (
    self )
```

Conjugation, reverse o involute == involute o reverse.

```
>>> print (clifford("{1}")).conj()
-1
>>> print (clifford("{2}") * clifford("{1}")).conj()
{1,2}
>>> print (clifford("{1}") * clifford("{2}")).conj()
-1,2
>>> print clifford("1+{1}+{1,2}").conj()
1-1-1,2
```

Definition at line 1137 of file PyClical.pyx.

References `PyClical.index_set.instance`, and `PyClical.clifford.instance`.

**6.3.2.31 even()**

```
def PyClical.clifford.even (
    self )
```

Even part of multivector, sum of even grade terms.

```
>>> print clifford("1+{1}+{1,2}").even()
1+{1,2}
```

Definition at line 1060 of file PyClical.pyx.

References `PyClical.index_set.instance`, and `PyClical.clifford.instance`.

**6.3.2.32 frame()**

```
def PyClical.clifford.frame (
    self )
```

Subalgebra generated by all generators of terms of given multivector.

```
>>> print clifford("1+3{-1}+2{1,2}+4{-2,7}").frame()
{-2,-1,1,2,7}
>>> s=clifford("1+3{-1}+2{1,2}+4{-2,7}").frame(); type(s)
<type 'PyClical.index_set'>
```

Definition at line 1214 of file PyClical.pyx.

References `PyClical.index_set.instance`, and `PyClical.clifford.instance`.

**6.3.2.33 inv()**

```
def PyClical.clifford.inv (
    self )
```

Geometric multiplicative inverse.

```
>>> x = clifford("{1}"); print x.inv()
{1}
>>> x = clifford(2); print x.inv()
0.5
>>> x = clifford("{1,2}"); print x.inv()
-{1,2}
```

Definition at line 925 of file PyClical.pyx.

References `PyClical.index_set.instance`, and `PyClical.clifford.instance`.

**6.3.2.34 involute()**

```
def PyClical.clifford.involute (
    self )
```

Main involution, each {i} is replaced by -{i} in each term,  
eg. clifford("{1}") -> -clifford("{1}").

```
>>> print clifford("{1}").involute()
-{1}
>>> print (clifford("{2}") * clifford("{1}")).involute()
-{1,2}
>>> print (clifford("{1}") * clifford("{2}")).involute()
{1,2}
>>> print clifford("1+{1}+{1,2}").involute()
1-{1}+{1,2}
```

Definition at line 1106 of file PyClical.pyx.

References PyClical.index\_set.instance, and PyClical.clifford.instance.

**6.3.2.35 isnan()**

```
def PyClical.clifford.isnan (
    self )
```

Check if a multivector contains any IEEE NaN values.

```
>>> clifford().isnan()
False
```

Definition at line 1205 of file PyClical.pyx.

References PyClical.index\_set.instance, and PyClical.clifford.instance.

**6.3.2.36 max\_abs()**

```
def PyClical.clifford.max_abs (
    self )
```

Maximum of absolute values of components of multivector: multivector infinity norm.

```
>>> clifford("1+{-1}+{1,2}+{1,2,3}").max_abs()
1.0
>>> clifford("3+2{1}+{1,2}").max_abs()
3.0
```

Definition at line 1183 of file PyClical.pyx.

References PyClical.index\_set.instance, and PyClical.clifford.instance.

**6.3.2.37 norm()**

```
def PyClical.clifford.norm (
    self )
```

Norm == sum of squares of coordinates.

```
>>> clifford("1+{1}+{1,2}").norm()
3.0
>>> clifford("1+{-1}+{1,2}+{1,2,3}").norm()
4.0
```

Definition at line 1163 of file PyClical.pyx.

References PyClical.index\_set.instance, and PyClical.clifford.instance.

**6.3.2.38 odd()**

```
def PyClical.clifford.odd (
    self )
```

Odd part of multivector, sum of odd grade terms.

```
>>> print clifford("1+{1}+{1,2}").odd()
{1}
```

Definition at line 1069 of file PyClical.pyx.

References PyClical.index\_set.instance, and PyClical.clifford.instance.

**6.3.2.39 outer\_pow()**

```
def PyClical.clifford.outer_pow (
    self,
    m )
```

Outer product power.

```
>>> x=clifford("2+{1}"); print x.outer_pow(0)
1
>>> x=clifford("2+{1}"); print x.outer_pow(1)
2+{1}
>>> x=clifford("2+{1}"); print x.outer_pow(2)
4+4{1}
>>> print clifford("1+{1}+{1,2}").outer_pow(3)
1+3{1}+3{1,2}
```

Definition at line 1003 of file PyClical.pyx.

References PyClical.index\_set.instance, and PyClical.clifford.instance.

**6.3.2.40 pow()**

```
def PyClical.clifford.pow (
    self,
    m )

Power: self to the m.

>>> x=clifford("{1}"); print x.pow(2)
1
>>> x=clifford("2"); print x.pow(2)
4
>>> x=clifford("2+{1}"); print x.pow(0)
1
>>> x=clifford("2+{1}"); print x.pow(1)
2+{1}
>>> x=clifford("2+{1}"); print x.pow(2)
5+4{1}
>>> print clifford("1+{1}+{1,2}").pow(3)
1+3{1}+3{1,2}
>>> i=clifford("{1,2}");print exp(pi/2) * i.pow(i)
1
```

Definition at line 979 of file PyClical.pyx.

References `glucat.exp()`, `PyClical.index_set.instance`, `PyClical.clifford.instance`, and `glucat.log()`.

Referenced by `PyClical.clifford.__pow__()`.

**6.3.2.41 pure()**

```
def PyClical.clifford.pure (
    self )

Pure part.

>>> print clifford("1+{1}+{1,2}").pure()
{1}+{1,2}
>>> print clifford("{1,2}").pure()
{1,2}
```

Definition at line 1049 of file PyClical.pyx.

References `PyClical.index_set.instance`, and `PyClical.clifford.instance`.

**6.3.2.42 quad()**

```
def PyClical.clifford.quad (
    self )

Quadratic form == (rev(x)*x)(0).

>>> print clifford("1+{1}+{1,2}").quad()
3.0
>>> print clifford("1+{-1}+{1,2}+{1,2,3}").quad()
2.0
```

Definition at line 1152 of file PyClical.pyx.

References `PyClical.index_set.instance`, and `PyClical.clifford.instance`.

**6.3.2.43 reframe()**

```
def PyClical.clifford.reframe (
    self,
    ixt )
```

Put self into a larger frame, containing the union of self.frame() and index set ixt. This can be used to make multiplication faster, by multiplying within a common frame.

```
>>> clifford("2+3{1}").reframe(index_set({1,2,3}))
clifford("2+3{1}")
>>> s=index_set({1,2,3});t=index_set({-3,-2,-1});x=random_clifford(s); x.reframe(t).frame() == (s|t);
True
```

Definition at line 648 of file PyClical.pyx.

**6.3.2.44 reverse()**

```
def PyClical.clifford.reverse (
    self )
```

Reversion, eg. clifford("{1}")\*clifford("{2}") -> clifford("{2}")\*clifford("{1}").

```
>>> print clifford("{1}").reverse()
{1}
>>> print (clifford("{2}") * clifford("{1}")).reverse()
{1,2}
>>> print (clifford("{1}") * clifford("{2}")).reverse()
-{1,2}
>>> print clifford("1+{1}+{1,2}").reverse()
1+{1}-{1,2}
```

Definition at line 1122 of file PyClical.pyx.

References PyClical.index\_set.instance, and PyClical.clifford.instance.

**6.3.2.45 scalar()**

```
def PyClical.clifford.scalar (
    self )
```

Scalar part.

```
>>> clifford("1+{1}+{1,2}").scalar()
1.0
>>> clifford("{1,2}").scalar()
0.0
```

Definition at line 1038 of file PyClical.pyx.

References PyClical.index\_set.instance, and PyClical.clifford.instance.

### 6.3.2.46 truncated()

```
def PyClical.clifford.truncated (
    self,
    limit )
```

Remove all terms of self with relative size smaller than limit.

```
>>> clifford("1e8+{1}+1e-8{1,2}").truncated(1.0e-6)
clifford("100000000")
>>> clifford("1e4+{1}+1e-4{1,2}").truncated(1.0e-6)
clifford("10000+{1}")
```

Definition at line 1194 of file PyClical.pyx.

References PyClical.index\_set.instance, and PyClical.clifford.instance.

### 6.3.2.47 vector\_part()

```
def PyClical.clifford.vector_part (
    self,
    frm = None )
```

Vector part of multivector, as a Python list, with respect to frm.

```
>>> print clifford("1+2{1}+3{2}+4{1,2}").vector_part()
[2.0, 3.0]
>>> print clifford("1+2{1}+3{2}+4{1,2}").vector_part(index_set({-1,1,2}))
[0.0, 2.0, 3.0]
```

Definition at line 1078 of file PyClical.pyx.

References PyClical.index\_set.instance, and PyClical.clifford.instance.

## 6.3.3 Member Data Documentation

### 6.3.3.1 instance

PyClical.clifford.instance

Definition at line 592 of file PyClical.pyx.

Referenced by PyClical.clifford.\_\_call\_\_(), PyClical.clifford.\_\_dealloc\_\_(), PyClical.clifford.\_\_getitem\_\_(), PyClical.clifford.\_\_neg\_\_(), PyClical.clifford.conj(), PyClical.clifford.even(), PyClical.clifford.frame(), PyClical.clifford.inv(), PyClical.clifford.involute(), PyClical.clifford.isnan(), PyClical.clifford.max\_abs(), PyClical.clifford.norm(), PyClical.clifford.odd(), PyClical.clifford.outer\_pow(), PyClical.clifford.pow(), PyClical.clifford.pure(), PyClical.clifford.quad(), PyClical.clifford.reverse(), PyClical.clifford.scalar(), PyClical.clifford.truncated(), and PyClical.clifford.vector\_part().

The documentation for this class was generated from the following file:

- [pyclical/PyClical.pyx](#)

## 6.4 glucat::clifford\_algebra< Scalar\_T, Index\_Set\_T, Multivector\_T > Class Template Reference

clifford\_algebra<> declares the operations of a Clifford algebra

```
#include <clifford_algebra.h>
```

### Public Types

- typedef Scalar\_T [scalar\\_t](#)
- typedef Index\_Set\_T [index\\_set\\_t](#)
- typedef Multivector\_T [multivector\\_t](#)
- typedef std::pair< const [index\\_set\\_t](#), Scalar\_T > [pair\\_t](#)
- typedef std::vector< Scalar\_T > [vector\\_t](#)

### Public Member Functions

- virtual [~clifford\\_algebra](#) ()
- virtual bool [operator==](#) (const [multivector\\_t](#) &val) const =0  
*Test for equality of multivectors.*
- virtual bool [operator==](#) (const Scalar\_T &scr) const =0  
*Test for equality of multivector and scalar.*
- virtual [multivector\\_t](#) & [operator+=](#) (const [multivector\\_t](#) &rhs)=0  
*Geometric sum.*
- virtual [multivector\\_t](#) & [operator+=](#) (const Scalar\_T &scr)=0  
*Geometric sum of multivector and scalar.*
- virtual [multivector\\_t](#) & [operator-=](#) (const [multivector\\_t](#) &rhs)=0  
*Geometric difference.*
- virtual const [multivector\\_t](#) [operator-](#) () const =0  
*Unary -.*
- virtual [multivector\\_t](#) & [operator\\*=](#) (const Scalar\_T &scr)=0  
*Product of multivector and scalar.*
- virtual [multivector\\_t](#) & [operator\\*=](#) (const [multivector\\_t](#) &rhs)=0  
*Geometric product.*
- virtual [multivector\\_t](#) & [operator%=>](#) (const [multivector\\_t](#) &rhs)=0  
*Contraction.*
- virtual [multivector\\_t](#) & [operator &=](#) (const [multivector\\_t](#) &rhs)=0  
*Inner product.*
- virtual [multivector\\_t](#) & [operator^=](#) (const [multivector\\_t](#) &rhs)=0  
*Outer product.*
- virtual [multivector\\_t](#) & [operator/=](#) (const Scalar\_T &scr)=0  
*Quotient of multivector and scalar.*
- virtual [multivector\\_t](#) & [operator/=](#) (const [multivector\\_t](#) &rhs)=0  
*Geometric quotient.*
- virtual [multivector\\_t](#) & [operator|=](#) (const [multivector\\_t](#) &rhs)=0  
*Transformation via twisted adjoint action.*
- virtual const [multivector\\_t](#) [inv](#) () const =0  
*Geometric multiplicative inverse.*
- virtual const [multivector\\_t](#) [pow](#) (int m) const =0

- *\*this to the m*
- virtual const [multivector\\_t](#) [outer\\_pow](#) (int m) const =0  
*Outer product power.*
- virtual const [index\\_set\\_t](#) [frame](#) () const =0  
*Subalgebra generated by all generators of terms of given multivector.*
- virtual [index\\_t](#) [grade](#) () const =0  
*Maximum of the grades of each term.*
- virtual Scalar\_T [operator\[\]](#) (const [index\\_set\\_t](#) ist) const =0  
*Subscripting: map from index set to scalar coordinate.*
- virtual const [multivector\\_t](#) [operator\(\)](#) ([index\\_t](#) grade) const =0  
*Pure grade-vector part.*
- virtual Scalar\_T [scalar](#) () const =0  
*Scalar part.*
- virtual const [multivector\\_t](#) [pure](#) () const =0  
*Pure part.*
- virtual const [multivector\\_t](#) [even](#) () const =0  
*Even part of multivector, sum of even grade terms.*
- virtual const [multivector\\_t](#) [odd](#) () const =0  
*Odd part of multivector, sum of odd grade terms.*
- virtual const [vector\\_t](#) [vector\\_part](#) () const =0  
*Vector part of multivector, as a vector\_t with respect to [frame\(\)](#)*
- virtual const [vector\\_t](#) [vector\\_part](#) (const [index\\_set\\_t](#) frm, const bool prechecked) const =0  
*Vector part of multivector, as a vector\_t with respect to frm.*
- virtual const [multivector\\_t](#) [involute](#) () const =0  
*Main involution, each {i} is replaced by -{i} in each term, eg. {1} -> -{1}.*
- virtual const [multivector\\_t](#) [reverse](#) () const =0  
*Reversion, eg. {1}\*{2} -> {2}\*{1}.*
- virtual const [multivector\\_t](#) [conj](#) () const =0  
*Conjugation, reverse o involute == involute o reverse.*
- virtual Scalar\_T [quad](#) () const =0  
*Scalar\_T quadratic form == (rev(x)\*x)(0)*
- virtual Scalar\_T [norm](#) () const =0  
*Scalar\_T norm == sum of norm of coordinates.*
- virtual Scalar\_T [max\\_abs](#) () const =0  
*Maximum of absolute values of components of multivector: multivector infinity norm.*
- virtual const [multivector\\_t](#) [truncated](#) (const Scalar\_T &limit=Scalar\_T(DEFAULT\_TRUNCATION)) const =0  
*Remove all terms with relative size smaller than limit.*
- virtual bool [isnan](#) () const =0  
*Check if a multivector contains any IEEE NaN values.*
- virtual void [write](#) (const std::string &msg="") const =0  
*Write formatted multivector to output.*
- virtual void [write](#) (std::ofstream &ofile, const std::string &msg="") const =0  
*Write formatted multivector to file.*

## Static Public Member Functions

- static const std::string [classname](#) ()

### 6.4.1 Detailed Description

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
class glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >
```

clifford\_algebra<> declares the operations of a Clifford algebra

Definition at line 42 of file clifford\_algebra.h.

### 6.4.2 Member Typedef Documentation

#### 6.4.2.1 index\_set\_t

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
typedef Index_Set_T glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >::index_set_t
```

Definition at line 46 of file clifford\_algebra.h.

#### 6.4.2.2 multivector\_t

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
typedef Multivector_T glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >::multivector_t
```

Definition at line 47 of file clifford\_algebra.h.

#### 6.4.2.3 pair\_t

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
typedef std::pair< const index_set_t, Scalar_T > glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >::pair_t
```

Definition at line 48 of file clifford\_algebra.h.

#### 6.4.2.4 scalar\_t

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
typedef Scalar_T glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >::scalar_t
```

Definition at line 45 of file clifford\_algebra.h.

#### 6.4.2.5 vector\_t

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
typedef std::vector<Scalar_T> glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T
>::vector_t
```

Definition at line 49 of file clifford\_algebra.h.

### 6.4.3 Constructor & Destructor Documentation

#### 6.4.3.1 ~clifford\_algebra()

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >::~~clifford_algebra (
) [inline], [virtual]
```

Definition at line 53 of file clifford\_algebra.h.

### 6.4.4 Member Function Documentation

#### 6.4.4.1 classname()

```
template<typename Scalar_T , typename Index_Set_T , typename Multivector_T >
const std::string glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >::classname
( ) [static]
```

Definition at line 66 of file clifford\_algebra\_imp.h.

#### 6.4.4.2 conj()

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual const multivector_t glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↔
::conj ( ) const [pure virtual]
```

Conjugation, reverse o involute == involute o reverse.

#### 6.4.4.3 even()

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual const multivector_t glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >::
even ( ) const [pure virtual]
```

Even part of multivector, sum of even grade terms.

Referenced by glucat::framed\_multi< Scalar\_T, LO, HI >::fast\_matrix\_multi().

#### 6.4.4.4 frame()

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual const index_set_t glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >::
frame ( ) const [pure virtual]
```

Subalgebra generated by all generators of terms of given multivector.

#### 6.4.4.5 grade()

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual index_t glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >::grade ( )
const [pure virtual]
```

Maximum of the grades of each term.

#### 6.4.4.6 inv()

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual const multivector_t glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >::
inv ( ) const [pure virtual]
```

Geometric multiplicative inverse.

#### 6.4.4.7 involute()

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual const multivector_t glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >::
involute ( ) const [pure virtual]
```

Main involution, each {i} is replaced by -{i} in each term, eg. {1} -> -{1}.

**6.4.4.8 isnan()**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual bool glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >::isnan ( ) const
[pure virtual]
```

Check if a multivector contains any IEEE NaN values.

**6.4.4.9 max\_abs()**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual Scalar_T glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >::max_abs ( )
const [pure virtual]
```

Maximum of absolute values of components of multivector: multivector infinity norm.

**6.4.4.10 norm()**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual Scalar_T glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >::norm ( )
const [pure virtual]
```

Scalar\_T norm == sum of norm of coordinates.

**6.4.4.11 odd()**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual const multivector_t glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↔
::odd ( ) const [pure virtual]
```

Odd part of multivector, sum of odd grade terms.

Referenced by glucat::framed\_multi< Scalar\_T, LO, HI >::fast\_matrix\_multi().

**6.4.4.12 operator &=()**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual multivector_t& glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↔
::operator&= (
    const multivector_t & rhs ) [pure virtual]
```

Inner product.

**6.4.4.13 operator%=( )**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual multivector_t& glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↔
::operator%= (
    const multivector_t & rhs ) [pure virtual]
```

Contraction.

**6.4.4.14 operator()( )**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual const multivector_t glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↔
::operator() (
    index_t grade ) const [pure virtual]
```

Pure grade-vector part.

**6.4.4.15 operator\*=( ) [1/2]**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual multivector_t& glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↔
::operator*= (
    const Scalar_T & scr ) [pure virtual]
```

Product of multivector and scalar.

**6.4.4.16 operator\*=( ) [2/2]**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual multivector_t& glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↔
::operator*= (
    const multivector_t & rhs ) [pure virtual]
```

Geometric product.

**6.4.4.17 operator+=( ) [1/2]**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual multivector_t& glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↔
::operator+= (
    const multivector_t & rhs ) [pure virtual]
```

Geometric sum.

**6.4.4.18 operator+=()** [2/2]

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual multivector_t& glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↔
::operator+= (
    const Scalar_T & scr ) [pure virtual]
```

Geometric sum of multivector and scalar.

**6.4.4.19 operator-()**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual const multivector_t glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↔
::operator- ( ) const [pure virtual]
```

Unary -.

**6.4.4.20 operator-=()**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual multivector_t& glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↔
::operator-= (
    const multivector_t & rhs ) [pure virtual]
```

Geometric difference.

**6.4.4.21 operator/=(** [1/2]

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual multivector_t& glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↔
::operator/= (
    const Scalar_T & scr ) [pure virtual]
```

Quotient of multivector and scalar.

**6.4.4.22 operator/=(** [2/2]

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual multivector_t& glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↔
::operator/= (
    const multivector_t & rhs ) [pure virtual]
```

Geometric quotient.

**6.4.4.23 operator==( )** [1/2]

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual bool glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >::operator== (
    const multivector_t & val ) const [pure virtual]
```

Test for equality of multivectors.

**6.4.4.24 operator==( )** [2/2]

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual bool glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >::operator== (
    const Scalar_T & scr ) const [pure virtual]
```

Test for equality of multivector and scalar.

**6.4.4.25 operator[]()**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual Scalar_T glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >::operator[]
(
    const index_set_t ist ) const [pure virtual]
```

Subscripting: map from index set to scalar coordinate.

**6.4.4.26 operator^=()**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual multivector_t& glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↔
::operator^= (
    const multivector_t & rhs ) [pure virtual]
```

Outer product.

**6.4.4.27 operator" |=()**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual multivector_t& glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↔
::operator|= (
    const multivector_t & rhs ) [pure virtual]
```

Transformation via twisted adjoint action.

**6.4.4.28 outer\_pow()**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual const multivector_t glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↔
::outer_pow (
    int m ) const [pure virtual]
```

Outer product power.

**6.4.4.29 pow()**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual const multivector_t glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↔
::pow (
    int m ) const [pure virtual]
```

\*this to the m

**6.4.4.30 pure()**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual const multivector_t glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↔
::pure ( ) const [pure virtual]
```

Pure part.

**6.4.4.31 quad()**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual Scalar_T glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >::quad ( )
const [pure virtual]
```

Scalar\_T quadratic form == (rev(x)\*x)(0)

**6.4.4.32 reverse()**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual const multivector_t glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↔
::reverse ( ) const [pure virtual]
```

Reversion, eg. {1}\*{2} -> {2}\*{1}.

**6.4.4.33 scalar()**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual Scalar_T glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >::scalar ( )
const [pure virtual]
```

Scalar part.

**6.4.4.34 truncated()**

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual const multivector_t glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↵
::truncated (
    const Scalar_T & limit = Scalar_T(DEFAULT_TRUNCATION) ) const [pure virtual]
```

Remove all terms with relative size smaller than limit.

**6.4.4.35 vector\_part()** [1/2]

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual const vector_t glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↵
::vector_part ( ) const [pure virtual]
```

Vector part of multivector, as a vector\_t with respect to [frame\(\)](#)

**6.4.4.36 vector\_part()** [2/2]

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual const vector_t glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >↵
::vector_part (
    const index_set_t frm,
    const bool prechecked ) const [pure virtual]
```

Vector part of multivector, as a vector\_t with respect to frm.

**6.4.4.37 write()** [1/2]

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual void glucat::clifford_algebra< Scalar_T, Index_Set_T, Multivector_T >::write (
    const std::string & msg = "" ) const [pure virtual]
```

Write formatted multivector to output.

#### 6.4.4.38 write() [2/2]

```
template<typename Scalar_T, typename Index_Set_T, typename Multivector_T>
virtual void glucat::clifford\_algebra< Scalar_T, Index_Set_T, Multivector_T >::write (
    std::ofstream & ofile,
    const std::string & msg = "" ) const [pure virtual]
```

Write formatted multivector to file.

The documentation for this class was generated from the following files:

- [glucat/clifford\\_algebra.h](#)
- [glucat/clifford\\_algebra\\_imp.h](#)

## 6.5 [glucat::compare\\_types](#)< LHS\_T, RHS\_T > Class Template Reference

Type comparison.

```
#include <global.h>
```

### Public Types

- enum { [are\\_same](#) = false }

#### 6.5.1 Detailed Description

```
template<typename LHS_T, typename RHS_T>
class glucat::compare\_types< LHS_T, RHS_T >
```

Type comparison.

Definition at line 54 of file `global.h`.

#### 6.5.2 Member Enumeration Documentation

##### 6.5.2.1 anonymous enum

```
template<typename LHS_T , typename RHS_T >
anonymous enum
```

##### Enumerator

<a href="#">are_same</a>	
--------------------------	--

Definition at line 57 of file global.h.

The documentation for this class was generated from the following file:

- [glucat/global.h](#)

## 6.6 glucat::compare\_types< T, T > Class Template Reference

```
#include <global.h>
```

### Public Types

- enum { [are\\_same](#) = true }

### 6.6.1 Detailed Description

```
template<typename T>
class glucat::compare_types< T, T >
```

Definition at line 60 of file global.h.

### 6.6.2 Member Enumeration Documentation

#### 6.6.2.1 anonymous enum

```
template<typename T >
anonymous enum
```

#### Enumerator

<a href="#">are_same</a>	
--------------------------	--

Definition at line 63 of file global.h.

The documentation for this class was generated from the following file:

- [glucat/global.h](#)

## 6.7 glucat::control\_t Class Reference

Parameters to control tests.

```
#include <control.h>
```

## Public Member Functions

- int [call](#) ([intfn](#) f) const  
*Call a function that returns int.*
- int [call](#) ([intintfn](#) f, int arg) const  
*Call a function of int that returns int.*

## Static Public Member Functions

- static const [control\\_t](#) & [control](#) (int argc, char \*\*argv)
- static bool [verbose](#) ()  
*Produce more detailed output from tests.*

## Private Member Functions

- bool [valid](#) () const
- bool [catch\\_exceptions](#) () const
- [control\\_t](#) (int argc, char \*\*argv)  
*Constructor from program arguments.*
- [control\\_t](#) ()
- [~control\\_t](#) ()
- [control\\_t](#) (const [control\\_t](#) &)
- [control\\_t](#) & [operator=](#) (const [control\\_t](#) &)

## Private Attributes

- bool [m\\_valid](#)  
*Test parameters are valid.*
- bool [m\\_catch\\_exceptions](#)  
*Catch exceptions.*

## Static Private Attributes

- static bool [m\\_verbose\\_output](#) = false  
*Produce more detailed output from tests.*

## Friends

- class [friend\\_for\\_private\\_destructor](#)

### 6.7.1 Detailed Description

Parameters to control tests.

Definition at line 39 of file control.h.

## 6.7.2 Constructor & Destructor Documentation

### 6.7.2.1 control\_t() [1/3]

```
glucat::control_t::control_t (
    int argc,
    char ** argv ) [private]
```

Constructor from program arguments.

Test control constructor from program arguments.

Definition at line 89 of file control.h.

References GLUCAT\_PACKAGE\_NAME, GLUCAT\_VERSION, m\_catch\_exceptions, m\_valid, m\_verbose\_output, and valid().

### 6.7.2.2 control\_t() [2/3]

```
glucat::control_t::control_t ( ) [inline], [private]
```

Definition at line 59 of file control.h.

### 6.7.2.3 ~control\_t()

```
glucat::control_t::~~control_t ( ) [inline], [private]
```

Definition at line 60 of file control.h.

### 6.7.2.4 control\_t() [3/3]

```
glucat::control_t::control_t (
    const control_t & ) [private]
```

## 6.7.3 Member Function Documentation

#### 6.7.3.1 `call()` [1/2]

```
int glucat::control_t::call (
    intfn f ) const [inline]
```

Call a function that returns int.

Definition at line 137 of file control.h.

References `catch_exceptions()`, `glucat::try_catch()`, and `valid()`.

#### 6.7.3.2 `call()` [2/2]

```
int glucat::control_t::call (
    intintfn f,
    int arg ) const [inline]
```

Call a function of int that returns int.

Definition at line 151 of file control.h.

References `catch_exceptions()`, `glucat::try_catch()`, and `valid()`.

#### 6.7.3.3 `catch_exceptions()`

```
bool glucat::control_t::catch_exceptions ( ) const [inline], [private]
```

Definition at line 49 of file control.h.

References `m_catch_exceptions`.

Referenced by `call()`.

#### 6.7.3.4 `control()`

```
static const control_t& glucat::control_t::control (
    int argc,
    char ** argv ) [inline], [static]
```

Single instance Ref: Scott Meyers, "Effective C++" Second Edition, Addison-Wesley, 1998.

Definition at line 71 of file control.h.

#### 6.7.3.5 operator=()

```
control_t& glucat::control_t::operator= (
    const control_t & ) [private]
```

#### 6.7.3.6 valid()

```
bool glucat::control_t::valid ( ) const [inline], [private]
```

Definition at line 44 of file control.h.

References m\_valid.

Referenced by call(), and control\_t().

#### 6.7.3.7 verbose()

```
static bool glucat::control_t::verbose ( ) [inline], [static]
```

Produce more detailed output from tests.

Definition at line 80 of file control.h.

References m\_verbose\_output.

### 6.7.4 Friends And Related Function Documentation

#### 6.7.4.1 friend\_for\_private\_destructor

```
friend class friend_for_private_destructor [friend]
```

Friend declaration to avoid compiler warning: "... only defines a private destructor and has no friends" Ref: Carlos O'Ryan, ACE <http://doc.ece.uci.edu>

Definition at line 67 of file control.h.

### 6.7.5 Member Data Documentation

#### 6.7.5.1 m\_catch\_exceptions

```
bool glucat::control_t::m_catch_exceptions [private]
```

Catch exceptions.

Definition at line 48 of file control.h.

Referenced by `catch_exceptions()`, and `control_t()`.

#### 6.7.5.2 m\_valid

```
bool glucat::control_t::m_valid [private]
```

Test parameters are valid.

Definition at line 43 of file control.h.

Referenced by `control_t()`, and `valid()`.

#### 6.7.5.3 m\_verbose\_output

```
bool glucat::control_t::m_verbose_output = false [static], [private]
```

Produce more detailed output from tests.

Definition at line 53 of file control.h.

Referenced by `control_t()`, and `verbose()`.

The documentation for this class was generated from the following file:

- [test/control.h](#)

## 6.8 glucat::CTAssertion< bool > Struct Template Reference

Compile time assertion.

```
#include <global.h>
```

### 6.8.1 Detailed Description

```
template<bool>
struct glucat::CTAssertion< bool >
```

Compile time assertion.

Definition at line 46 of file global.h.

The documentation for this struct was generated from the following file:

- [glucat/global.h](#)

## 6.9 glucat::CTAssertion< true > Struct Template Reference

```
#include <global.h>
```

### 6.9.1 Detailed Description

```
template<>
struct glucat::CTAssertion< true >
```

Definition at line 47 of file global.h.

The documentation for this struct was generated from the following file:

- [glucat/global.h](#)

## 6.10 glucat::numeric\_traits< Scalar\_T >::demoted<> Struct Template Reference

Demoted type for long double.

```
#include <long_double.h>
```

### Public Types

- typedef long double [type](#)
- typedef float [type](#)

### 6.10.1 Detailed Description

```
template<typename Scalar_T>
template<>
struct glucat::numeric_traits< Scalar_T >::demoted<>
```

Demoted type for long double.

Demoted type.

Definition at line 47 of file long\_double.h.

## 6.10.2 Member Typedef Documentation

### 6.10.2.1 `type` [1/2]

```
template<typename Scalar_T >
typedef long double glucat::numeric\_traits< Scalar_T >::demoted<>::type
```

Definition at line 49 of file `long_double.h`.

### 6.10.2.2 `type` [2/2]

```
template<typename Scalar_T >
typedef float glucat::numeric\_traits< Scalar_T >::demoted<>::type
```

Definition at line 147 of file `scalar.h`.

The documentation for this struct was generated from the following files:

- [glucat/long\\_double.h](#)
- [glucat/scalar.h](#)

## 6.11 `glucat::matrix::eig_genus< Matrix_T >` Struct Template Reference

Structure containing classification of eigenvalues.

```
#include <matrix.h>
```

### Public Types

- typedef `Matrix_T::value_type` [Scalar\\_T](#)

### Public Attributes

- [eig\\_case\\_t m\\_eig\\_case](#)  
*What kind of eigenvalues does the matrix contain?*
- [Scalar\\_T m\\_safe\\_arg](#)  
*Argument such that  $\exp(\pi \cdot m\_safe\_arg)$  lies between arguments of eigenvalues.*

### 6.11.1 Detailed Description

```
template<typename Matrix_T>
struct glucat::matrix::eig_genus< Matrix_T >
```

Structure containing classification of eigenvalues.

Definition at line 131 of file matrix.h.

### 6.11.2 Member Typedef Documentation

#### 6.11.2.1 Scalar\_T

```
template<typename Matrix_T>
typedef Matrix_T::value_type glucat::matrix::eig_genus< Matrix_T >::Scalar_T
```

Definition at line 133 of file matrix.h.

### 6.11.3 Member Data Documentation

#### 6.11.3.1 m\_eig\_case

```
template<typename Matrix_T>
eig_case_t glucat::matrix::eig_genus< Matrix_T >::m_eig_case
```

What kind of eigenvalues does the matrix contain?

Definition at line 135 of file matrix.h.

Referenced by glucat::matrix::classify\_eigenvalues(), glucat::matrix\_log(), and glucat::matrix\_sqrt().

#### 6.11.3.2 m\_safe\_arg

```
template<typename Matrix_T>
Scalar_T glucat::matrix::eig_genus< Matrix_T >::m_safe_arg
```

Argument such that  $\exp(\pi m\_safe\_arg)$  lies between arguments of eigenvalues.

Definition at line 137 of file matrix.h.

Referenced by glucat::matrix::classify\_eigenvalues(), glucat::matrix\_log(), and glucat::matrix\_sqrt().

The documentation for this struct was generated from the following file:

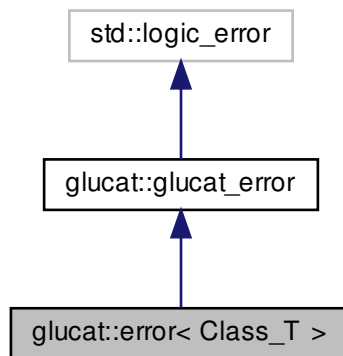
- glucat/matrix.h

## 6.12 glucat::error< Class\_T > Class Template Reference

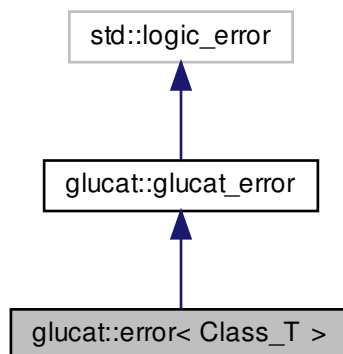
Specific exception class.

```
#include <errors.h>
```

Inheritance diagram for glucat::error< Class\_T >:



Collaboration diagram for glucat::error< Class\_T >:



### Public Member Functions

- [error](#) (const std::string &msg)  
*Specific exception class.*
- [error](#) (const std::string &context, const std::string &msg)
- virtual const std::string [heading](#) () const throw ()
- virtual const std::string [classname](#) () const throw ()
- virtual void [print\\_error\\_msg](#) () const

## Additional Inherited Members

### 6.12.1 Detailed Description

```
template<class Class_T>
class glucat::error< Class_T >
```

Specific exception class.

Definition at line 57 of file errors.h.

### 6.12.2 Constructor & Destructor Documentation

#### 6.12.2.1 error() [1/2]

```
template<class Class_T >
glucat::error< Class_T >::error (
    const std::string & msg )
```

Specific exception class.

Definition at line 39 of file errors\_imp.h.

#### 6.12.2.2 error() [2/2]

```
template<class Class_T >
glucat::error< Class_T >::error (
    const std::string & context,
    const std::string & msg )
```

Definition at line 45 of file errors\_imp.h.

### 6.12.3 Member Function Documentation

#### 6.12.3.1 classname()

```
template<class Class_T >
const std::string glucat::error< Class_T >::classname ( ) const throw ( ) [virtual]
```

Implements [glucat::glucat\\_error](#).

Definition at line 58 of file errors\_imp.h.

### 6.12.3.2 heading()

```
template<class Class_T >
const std::string glucat::error< Class_T >::heading ( ) const throw ( ) [virtual]
```

Implements [glucat::glucat\\_error](#).

Definition at line 52 of file errors\_imp.h.

### 6.12.3.3 print\_error\_msg()

```
template<class Class_T >
void glucat::error< Class_T >::print_error_msg ( ) const [virtual]
```

Implements [glucat::glucat\\_error](#).

Definition at line 64 of file errors\_imp.h.

The documentation for this class was generated from the following files:

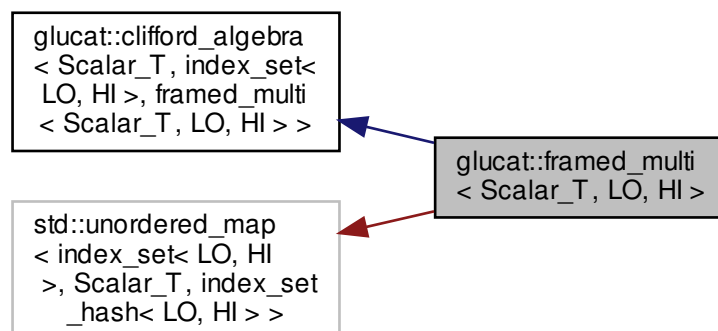
- [glucat/errors.h](#)
- [glucat/errors\\_imp.h](#)

## 6.13 glucat::framed\_multi< Scalar\_T, LO, HI > Class Template Reference

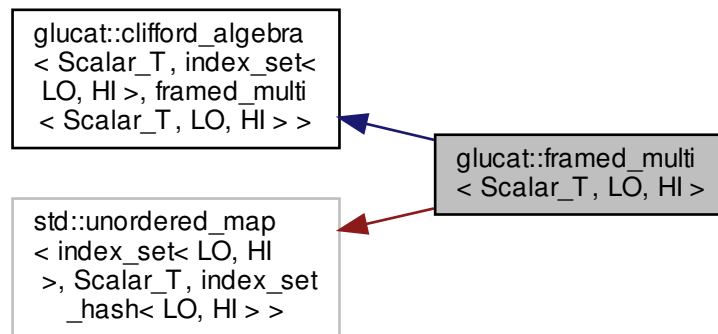
A framed\_multi<Scalar\_T,LO,HI> is a framed approximation to a multivector.

```
#include <framed_multi.h>
```

Inheritance diagram for glucat::framed\_multi< Scalar\_T, LO, HI >:



Collaboration diagram for glucat::framed\_multi< Scalar\_T, LO, HI >:



## Classes

- class [hash\\_size\\_t](#)
- class [var\\_term](#)

*Variable term.*

## Public Types

- typedef [framed\\_multi](#) [multivector\\_t](#)
- typedef [multivector\\_t](#) [framed\\_multi\\_t](#)
- typedef [Scalar\\_T](#) [scalar\\_t](#)
- typedef [index\\_set< LO, HI >](#) [index\\_set\\_t](#)
- typedef std::pair< const [index\\_set\\_t](#), [Scalar\\_T](#) > [term\\_t](#)
- typedef std::vector< [Scalar\\_T](#) > [vector\\_t](#)
- typedef [error< multivector\\_t >](#) [error\\_t](#)
- typedef [matrix\\_multi< Scalar\\_T, LO, HI >](#) [matrix\\_multi\\_t](#)

## Public Member Functions

- [~framed\\_multi](#) ()  
*Destructor.*
- [framed\\_multi](#) ()  
*Default constructor.*
- template<typename Other\_Scalar\_T >  
[framed\\_multi](#) (const [framed\\_multi](#)< Other\_Scalar\_T, LO, HI > &val)  
*Construct a multivector from a multivector with a different scalar type.*
- template<typename Other\_Scalar\_T >  
[framed\\_multi](#) (const [framed\\_multi](#)< Other\_Scalar\_T, LO, HI > &val, const [index\\_set\\_t](#) frm, const bool prechecked=false)  
*Construct a multivector, within a given frame, from a given multivector.*
- [framed\\_multi](#) (const [framed\\_multi\\_t](#) &val, const [index\\_set\\_t](#) frm, const bool prechecked=false)

- Construct a multivector, within a given frame, from a given multivector.*
- `framed_multi` (const `index_set_t` ist, const `Scalar_T` &crd=`Scalar_T`(1))  
*Construct a multivector from an index set and a scalar coordinate.*
- `framed_multi` (const `index_set_t` ist, const `Scalar_T` &crd, const `index_set_t` frm, const bool prechecked=false)  
*Construct a multivector, within a given frame, from an index set and a scalar coordinate.*
- `framed_multi` (const `Scalar_T` &scr, const `index_set_t` frm=`index_set_t`())  
*Construct a multivector from a scalar (within a frame, if given)*
- `framed_multi` (const int scr, const `index_set_t` frm=`index_set_t`())  
*Construct a multivector from an int (within a frame, if given)*
- `framed_multi` (const `vector_t` &vec, const `index_set_t` frm, const bool prechecked=false)  
*Construct a multivector, within a given frame, from a given vector.*
- `framed_multi` (const std::string &str)  
*Construct a multivector from a string: eg: "3+2{1,2}-6.1e-2{2,3}".*
- `framed_multi` (const std::string &str, const `index_set_t` frm, const bool prechecked=false)  
*Construct a multivector, within a given frame, from a string: eg: "3+2{1,2}-6.1e-2{2,3}".*
- `framed_multi` (const char \*str)  
*Construct a multivector from a char\*: eg: "3+2{1,2}-6.1e-2{2,3}".*
- `framed_multi` (const char \*str, const `index_set_t` frm, const bool prechecked=false)  
*Construct a multivector, within a given frame, from a char\*: eg: "3+2{1,2}-6.1e-2{2,3}".*
- template<typename Other\_Scalar\_T >  
`framed_multi` (const `matrix_multi`< Other\_Scalar\_T, LO, HI > &val)  
*Construct a multivector from a matrix\_multi\_t.*
- template<typename Other\_Scalar\_T >  
const `matrix_multi`< Other\_Scalar\_T, LO, HI > `fast_matrix_multi` (const `index_set_t` frm) const  
*Use generalized FFT to construct a matrix\_multi\_t.*
- const `framed_multi_t` `fast_framed_multi` () const  
*Use inverse generalized FFT to construct a framed\_multi\_t.*
- `_GLUCAT_CLIFFORD_ALGEBRA_OPERATIONS` unsigned long `nbr_terms` () const  
*Number of terms.*
- `multivector_t` & `operator+=` (const `term_t` &term)  
*Add a term, if non-zero.*

## Static Public Member Functions

- static const std::string `classname` ()  
*Class name used in messages.*
- static const `framed_multi_t` `random` (const `index_set_t` frm, `Scalar_T` fill=`Scalar_T`(1))  
*Random multivector within a frame.*

## Private Types

- typedef class `var_term` `var_term_t`
- typedef `matrix_multi_t::matrix_t` `matrix_t`
- typedef std::map< `index_set_t`, `Scalar_T`, std::less< const `index_set_t` > > `sorted_map_t`
- typedef std::unordered\_map< `index_set_t`, `Scalar_T`, `index_set_hash`< LO, HI > > `map_t`
- typedef std::pair< const `multivector_t`, const `multivector_t` > `framed_pair_t`
- typedef map\_t::size\_type `size_type`
- typedef map\_t::iterator `iterator`
- typedef map\_t::const\_iterator `const_iterator`

## Private Member Functions

- `framed_multi` (const `hash_size_t` &hash\_size)  
*Private constructor using hash\_size.*
- `multivector_t fold` (const `index_set_t` frm) const  
*Subalgebra isomorphism: fold each term within the given frame.*
- `multivector_t unfold` (const `index_set_t` frm) const  
*Subalgebra isomorphism: unfold each term within the given frame.*
- `multivector_t & centre_pm4_qp4` (`index_t` &p, `index_t` &q)  
*Subalgebra isomorphism:  $R_{\{p,q\}}$  to  $R_{\{p-4,q+4\}}$ .*
- `multivector_t & centre_pp4_qm4` (`index_t` &p, `index_t` &q)  
*Subalgebra isomorphism:  $R_{\{p,q\}}$  to  $R_{\{p+4,q-4\}}$ .*
- `multivector_t & centre_qp1_pm1` (`index_t` &p, `index_t` &q)  
*Subalgebra isomorphism:  $R_{\{p,q\}}$  to  $R_{\{q+1,p-1\}}$ .*
- const `framed_pair_t divide` (const `index_set_t` ist) const  
*Divide multivector into part divisible by `index_set` and remainder.*
- const `matrix_t fast` (const `index_t` level, const bool odd) const  
*Generalized FFT from framed\_multi\_t to matrix\_t.*

## Friends

- template<typename Other\_Scalar\_T , const `index_t` Other\_LO, const `index_t` Other\_HI>  
class `matrix_multi`
- template<typename Other\_Scalar\_T , const `index_t` Other\_LO, const `index_t` Other\_HI>  
class `framed_multi`
- const `framed_multi_t operator*` (const `framed_multi_t` &lhs, const `framed_multi_t` &rhs)
- const `framed_multi_t operator^` (const `framed_multi_t` &lhs, const `framed_multi_t` &rhs)
- const `framed_multi_t operator &` (const `framed_multi_t` &lhs, const `framed_multi_t` &rhs)
- const `framed_multi_t operator%` (const `framed_multi_t` &lhs, const `framed_multi_t` &rhs)
- `Scalar_T star` (const `framed_multi_t` &lhs, const `framed_multi_t` &rhs)
- const `framed_multi_t operator/` (const `framed_multi_t` &lhs, const `framed_multi_t` &rhs)
- const `framed_multi_t operator|` (const `framed_multi_t` &lhs, const `framed_multi_t` &rhs)
- std::istream & `operator>>` (std::istream &s, `multivector_t` &val)
- std::ostream & `operator<<` (std::ostream &os, const `multivector_t` &val)
- std::ostream & `operator<<` (std::ostream &os, const `term_t` &term)
- const `framed_multi_t exp` (const `framed_multi_t` &val)

### 6.13.1 Detailed Description

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
class glucat::framed_multi< Scalar_T, LO, HI >
```

A `framed_multi<Scalar_T,LO,HI>` is a framed approximation to a multivector.

Definition at line 65 of file `framed_multi.h`.

### 6.13.2 Member Typedef Documentation

### 6.13.2.1 const\_iterator

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
typedef map_t::const_iterator glucat::framed_multi< Scalar_T, LO, HI >::const_iterator [private]
```

Definition at line 196 of file framed\_multi.h.

### 6.13.2.2 error\_t

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
typedef error<multivector_t> glucat::framed_multi< Scalar_T, LO, HI >::error_t
```

Definition at line 155 of file framed\_multi.h.

### 6.13.2.3 framed\_multi\_t

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
typedef multivector_t glucat::framed_multi< Scalar_T, LO, HI >::framed_multi_t
```

Definition at line 150 of file framed\_multi.h.

### 6.13.2.4 framed\_pair\_t

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
typedef std::pair< const multivector_t, const multivector_t > glucat::framed_multi< Scalar_T,
LO, HI >::framed_pair_t [private]
```

Definition at line 193 of file framed\_multi.h.

### 6.13.2.5 index\_set\_t

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
typedef index_set<LO,HI> glucat::framed_multi< Scalar_T, LO, HI >::index_set_t
```

Definition at line 152 of file framed\_multi.h.

#### 6.13.2.6 iterator

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
typedef map_t::iterator glucat::framed_multi< Scalar_T, LO, HI >::iterator [private]
```

Definition at line 195 of file framed\_multi.h.

#### 6.13.2.7 map\_t

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
typedef std::unordered_map< index_set_t, Scalar_T, index_set_hash<LO,HI> > glucat::framed_multi<
Scalar_T, LO, HI >::map_t [private]
```

Definition at line 175 of file framed\_multi.h.

#### 6.13.2.8 matrix\_multi\_t

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
typedef matrix_multi<Scalar_T,LO,HI> glucat::framed_multi< Scalar_T, LO, HI >::matrix_multi_t
```

Definition at line 156 of file framed\_multi.h.

#### 6.13.2.9 matrix\_t

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
typedef matrix_multi_t::matrix_t glucat::framed_multi< Scalar_T, LO, HI >::matrix_t [private]
```

Definition at line 165 of file framed\_multi.h.

#### 6.13.2.10 multivector\_t

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
typedef framed_multi glucat::framed_multi< Scalar_T, LO, HI >::multivector_t
```

Definition at line 149 of file framed\_multi.h.

**6.13.2.11 scalar\_t**

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAU↵
LT_HI>
typedef Scalar_T glucat::framed_multi< Scalar_T, LO, HI >::scalar_t
```

Definition at line 151 of file framed\_multi.h.

**6.13.2.12 size\_type**

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAU↵
LT_HI>
typedef map_t::size_type glucat::framed_multi< Scalar_T, LO, HI >::size_type [private]
```

Definition at line 194 of file framed\_multi.h.

**6.13.2.13 sorted\_map\_t**

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAU↵
LT_HI>
typedef std::map< index_set_t, Scalar_T, std::less<const index_set_t> > glucat::framed_multi<
Scalar_T, LO, HI >::sorted_map_t [private]
```

Definition at line 172 of file framed\_multi.h.

**6.13.2.14 term\_t**

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAU↵
LT_HI>
typedef std::pair<const index_set_t, Scalar_T> glucat::framed_multi< Scalar_T, LO, HI >↵
::term_t
```

Definition at line 153 of file framed\_multi.h.

**6.13.2.15 var\_term\_t**

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAU↵
LT_HI>
typedef class var_term glucat::framed_multi< Scalar_T, LO, HI >::var_term_t [private]
```

Definition at line 164 of file framed\_multi.h.

## 6.13.2.16 vector\_t

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
typedef std::vector<Scalar_T> glucat::framed_multi< Scalar_T, LO, HI >::vector_t
```

Definition at line 154 of file framed\_multi.h.

## 6.13.3 Constructor &amp; Destructor Documentation

## 6.13.3.1 ~framed\_multi()

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
glucat::framed_multi< Scalar_T, LO, HI >::~~framed_multi ( ) [inline]
```

Destructor.

Definition at line 202 of file framed\_multi.h.

## 6.13.3.2 framed\_multi() [1/15]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
glucat::framed_multi< Scalar_T, LO, HI >::framed_multi ( )
```

Default constructor.

Definition at line 67 of file framed\_multi\_imp.h.

Referenced by glucat::framed\_multi< Scalar\_T, LO, HI >::framed\_multi().

## 6.13.3.3 framed\_multi() [2/15]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
glucat::framed_multi< Scalar_T, LO, HI >::framed_multi (
    const hash_size_t & hash_size ) [private]
```

Private constructor using hash\_size.

Definition at line 74 of file framed\_multi\_imp.h.

**6.13.3.4 framed\_multi()** [3/15]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
template<typename Other_Scalar_T >
glucat::framed_multi< Scalar_T, LO, HI >::framed_multi (
    const framed_multi< Other_Scalar_T, LO, HI > & val )
```

Construct a multivector from a multivector with a different scalar type.

Definition at line 82 of file framed\_multi\_imp.h.

**6.13.3.5 framed\_multi()** [4/15]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
template<typename Other_Scalar_T >
glucat::framed_multi< Scalar_T, LO, HI >::framed_multi (
    const framed_multi< Other_Scalar_T, LO, HI > & val,
    const index_set_t frm,
    const bool prechecked = false )
```

Construct a multivector, within a given frame, from a given multivector.

Definition at line 97 of file framed\_multi\_imp.h.

**6.13.3.6 framed\_multi()** [5/15]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
glucat::framed_multi< Scalar_T, LO, HI >::framed_multi (
    const framed_multi_t & val,
    const index_set_t frm,
    const bool prechecked = false )
```

Construct a multivector, within a given frame, from a given multivector.

Definition at line 112 of file framed\_multi\_imp.h.

**6.13.3.7 framed\_multi()** [6/15]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
glucat::framed_multi< Scalar_T, LO, HI >::framed_multi (
    const index_set_t ist,
    const Scalar_T & crd = Scalar_T(1) )
```

Construct a multivector from an index set and a scalar coordinate.

Definition at line 120 of file framed\_multi\_imp.h.

References PyClical::ist.

**6.13.3.8 framed\_multi()** [7/15]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
glucat::framed_multi< Scalar_T, LO, HI >::framed_multi (
    const index_set_t ist,
    const Scalar_T & crd,
    const index_set_t frm,
    const bool prechecked = false )
```

Construct a multivector, within a given frame, from an index set and a scalar coordinate.

Definition at line 130 of file framed\_multi\_imp.h.

References PyClical::ist.

**6.13.3.9 framed\_multi()** [8/15]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
glucat::framed_multi< Scalar_T, LO, HI >::framed_multi (
    const Scalar_T & scr,
    const index_set_t frm = index_set_t() )
```

Construct a multivector from a scalar (within a frame, if given)

Definition at line 143 of file framed\_multi\_imp.h.

**6.13.3.10 framed\_multi()** [9/15]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
glucat::framed_multi< Scalar_T, LO, HI >::framed_multi (
    const int scr,
    const index_set_t frm = index_set_t() )
```

Construct a multivector from an int (within a frame, if given)

Definition at line 153 of file framed\_multi\_imp.h.

**6.13.3.11 framed\_multi()** [10/15]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
glucat::framed_multi< Scalar_T, LO, HI >::framed_multi (
    const vector_t & vec,
    const index_set_t frm,
    const bool prechecked = false )
```

Construct a multivector, within a given frame, from a given vector.

Definition at line 163 of file framed\_multi\_imp.h.

References glucat::index\_set< LO, HI >::count(), glucat::index\_set< LO, HI >::max(), and glucat::index\_set< LO, HI >::min().

**6.13.3.12 framed\_multi()** [11/15]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
glucat::framed_multi< Scalar_T, LO, HI >::framed_multi (
    const std::string & str )
```

Construct a multivector from a string: eg: "3+2{1,2}-6.1e-2{2,3}".

Definition at line 186 of file framed\_multi\_imp.h.

**6.13.3.13 framed\_multi()** [12/15]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
glucat::framed_multi< Scalar_T, LO, HI >::framed_multi (
    const std::string & str,
    const index_set_t frm,
    const bool prechecked = false )
```

Construct a multivector, within a given frame, from a string: eg: "3+2{1,2}-6.1e-2{2,3}".

Definition at line 202 of file framed\_multi\_imp.h.

**6.13.3.14 framed\_multi()** [13/15]

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAU↵
LT_HI>
glucat::framed_multi< Scalar_T, LO, HI >::framed_multi (
    const char * str ) [inline]
```

Construct a multivector from a char\*: eg: "3+2{1,2}-6.1e-2{2,3}".

Definition at line 238 of file framed\_multi.h.

References glucat::framed\_multi< Scalar\_T, LO, HI >::framed\_multi().

**6.13.3.15 framed\_multi()** [14/15]

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAU↵
LT_HI>
glucat::framed_multi< Scalar_T, LO, HI >::framed_multi (
    const char * str,
    const index_set_t frm,
    const bool prechecked = false ) [inline]
```

Construct a multivector, within a given frame, from a char\*: eg: "3+2{1,2}-6.1e-2{2,3}".

Definition at line 241 of file framed\_multi.h.

References glucat::framed\_multi< Scalar\_T, LO, HI >::framed\_multi().

## 6.13.3.16 framed\_multi() [15/15]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
template<typename Other_Scalar_T >
glucat::framed_multi< Scalar_T, LO, HI >::framed_multi (
    const matrix_multi< Other_Scalar_T, LO, HI > & val )
```

Construct a multivector from a matrix\_multi\_t.

Definition at line 215 of file framed\_multi\_imp.h.

References \_GLUCAT\_HASH\_SIZE\_T, glucat::abs(), glucat::matrix\_multi< Scalar\_T, LO, HI >::basis\_element(), glucat::index\_set< LO, HI >::count(), PyClical::e(), glucat::clifford\_algebra< Scalar\_T, index\_set< LO, HI >, matrix\_multi< Scalar\_T, LO, HI > >::frame(), glucat::tuning< Mult\_Matrix\_Threshold, Div\_Max\_Steps, Sqrt\_Max\_Steps, Log\_Max\_Outer\_Steps, Log\_Max\_Inner\_Steps, Basis\_Max\_Count, Fast\_Size\_Threshold, Inv\_Fast\_Dim\_Threshold, Products\_Size\_Threshold, Function\_Precision >::inv\_fast\_dim\_threshold, PyClical::ist, glucat::matrix\_multi< Scalar\_T, LO, HI >::m\_matrix, glucat::matrix::nnz(), and glucat::clifford\_algebra< Scalar\_T, index\_set< LO, HI >, matrix\_multi< Scalar\_T, LO, HI > >::norm().

## 6.13.4 Member Function Documentation

## 6.13.4.1 centre\_pm4\_qp4()

```
template<typename Scalar_T , const index_t LO, const index_t HI>
framed_multi< Scalar_T, LO, HI > & glucat::framed_multi< Scalar_T, LO, HI >::centre_pm4_qp4 (
    index_t & p,
    index_t & q ) [private]
```

Subalgebra isomorphism:  $R_{\{p,q\}}$  to  $R_{\{p-4,q+4\}}$ .

Definition at line 1655 of file framed\_multi\_imp.h.

References PyClical::ist.

Referenced by glucat::matrix\_multi< Scalar\_T, LO, HI >::fast\_framed\_multi(), and glucat::framed\_multi< Scalar\_T, LO, HI >::fast\_matrix\_multi().

## 6.13.4.2 centre\_pp4\_qm4()

```
template<typename Scalar_T , const index_t LO, const index_t HI>
framed_multi< Scalar_T, LO, HI > & glucat::framed_multi< Scalar_T, LO, HI >::centre_pp4_qm4 (
    index_t & p,
    index_t & q ) [private]
```

Subalgebra isomorphism:  $R_{\{p,q\}}$  to  $R_{\{p+4,q-4\}}$ .

Definition at line 1700 of file framed\_multi\_imp.h.

References PyClical::ist.

Referenced by glucat::matrix\_multi< Scalar\_T, LO, HI >::fast\_framed\_multi(), and glucat::framed\_multi< Scalar\_T, LO, HI >::fast\_matrix\_multi().

#### 6.13.4.3 centre\_qp1\_pm1()

```
template<typename Scalar_T , const index_t LO, const index_t HI>
framed_multi< Scalar_T, LO, HI > & glucat::framed_multi< Scalar_T, LO, HI >::centre_qp1_pm1 (
    index_t & p,
    index_t & q ) [private]
```

Subalgebra isomorphism:  $R_{\{p,q\}}$  to  $R_{\{q+1,p-1\}}$ .

Definition at line 1745 of file framed\_multi\_imp.h.

References PyClical::ist.

Referenced by glucat::matrix\_multi< Scalar\_T, LO, HI >::fast\_framed\_multi(), and glucat::framed\_multi< Scalar\_T, LO, HI >::fast\_matrix\_multi().

#### 6.13.4.4 classname()

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const std::string glucat::framed_multi< Scalar_T, LO, HI >::classname ( ) [static]
```

Class name used in messages.

Definition at line 53 of file framed\_multi\_imp.h.

#### 6.13.4.5 divide()

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const std::pair< const framed_multi< Scalar_T, LO, HI >, const framed_multi< Scalar_T, LO, HI > >
glucat::framed_multi< Scalar_T, LO, HI >::divide (
    const index_set_t ist ) const [private]
```

Divide multivector into part divisible by [index\\_set](#) and remainder.

Divide multivector into quotient with terms divisible by index set, and remainder.

Definition at line 1781 of file framed\_multi\_imp.h.

References PyClical::ist.

Referenced by glucat::framed\_multi< Scalar\_T, LO, HI >::fast().

## 6.13.4.6 fast()

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const framed_multi< Scalar_T, LO, HI >::matrix_t glucat::framed_multi< Scalar_T, LO, HI >↵
::fast (
    const index_t level,
    const bool odd ) const [private]
```

Generalized FFT from framed\_multi\_t to matrix\_t.

Definition at line 1800 of file framed\_multi\_imp.h.

References glucat::framed\_multi< Scalar\_T, LO, HI >::divide(), glucat::framed\_multi< Scalar\_T, LO, HI >::fast(), glucat::matrix::kron(), glucat::odd(), and glucat::scalar().

Referenced by glucat::framed\_multi< Scalar\_T, LO, HI >::fast(), and glucat::framed\_multi< Scalar\_T, LO, HI >↵::fast\_matrix\_multi().

## 6.13.4.7 fast\_framed\_multi()

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const framed_multi< Scalar_T, LO, HI > glucat::framed_multi< Scalar_T, LO, HI >::fast_↵
framed_multi ( ) const [inline]
```

Use inverse generalized FFT to construct a framed\_multi\_t.

Definition at line 1898 of file framed\_multi\_imp.h.

## 6.13.4.8 fast\_matrix\_multi()

```
template<typename Scalar_T , const index_t LO, const index_t HI>
template<typename Other_Scalar_T >
const matrix_multi< Other_Scalar_T, LO, HI > glucat::framed_multi< Scalar_T, LO, HI >::fast_↵
_matrix_multi (
    const index_set_t frm ) const
```

Use generalized FFT to construct a matrix\_multi\_t.

Definition at line 1866 of file framed\_multi\_imp.h.

References glucat::framed\_multi< Scalar\_T, LO, HI >::centre\_pm4\_qp4(), glucat::framed\_multi< Scalar\_T, LO, HI >::centre\_pp4\_qm4(), glucat::framed\_multi< Scalar\_T, LO, HI >::centre\_qp1\_pm1(), glucat::index\_set< L↵O, HI >::count\_neg(), glucat::index\_set< LO, HI >::count\_pos(), glucat::clifford\_algebra< Scalar\_T, Index\_Set↵\_T, Multivector\_T >::even(), glucat::framed\_multi< Scalar\_T, LO, HI >::fast(), glucat::clifford\_algebra< Scalar\_T, Index\_Set\_T, Multivector\_T >::odd(), glucat::gen::offset\_to\_super, and glucat::pos\_mod().

#### 6.13.4.9 fold()

```
template<typename Scalar_T , const index_t LO, const index_t HI>
framed_multi< Scalar_T, LO, HI > glucat::framed_multi< Scalar_T, LO, HI >::fold (
    const index_set_t frm ) const [private]
```

Subalgebra isomorphism: fold each term within the given frame.

Definition at line 1614 of file framed\_multi\_imp.h.

References glucat::index\_set< LO, HI >::is\_contiguous().

#### 6.13.4.10 nbr\_terms()

```
template<typename Scalar_T , const index_t LO, const index_t HI>
unsigned long glucat::framed_multi< Scalar_T, LO, HI >::nbr_terms ( ) const
```

Number of terms.

Definition at line 1545 of file framed\_multi\_imp.h.

#### 6.13.4.11 operator+=( )

```
template<typename Scalar_T , const index_t LO, const index_t HI>
framed_multi< Scalar_T, LO, HI > & glucat::framed_multi< Scalar_T, LO, HI >::operator+= (
    const term_t & term ) [inline]
```

Add a term, if non-zero.

Insert a term into a multivector, add terms with same index set.

Geometric sum.

Geometric sum of multivector and scalar.

Definition at line 329 of file framed\_multi\_imp.h.

#### 6.13.4.12 random()

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const framed_multi< Scalar_T, LO, HI > glucat::framed_multi< Scalar_T, LO, HI >::random (
    const index_set_t frm,
    Scalar_T fill = Scalar_T(1) ) [static]
```

Random multivector within a frame.

Definition at line 1273 of file framed\_multi\_imp.h.

References glucat::index\_set< LO, HI >::count(), PyClical::fill, and glucat::sqrt().

Referenced by glucat::matrix\_multi< Scalar\_T, LO, HI >::random().

6.13.4.13 `unfold()`

```
template<typename Scalar_T , const index_t LO, const index_t HI>
framed_multi< Scalar_T, LO, HI > glucat::framed_multi< Scalar_T, LO, HI >::unfold (
    const index_set_t frm ) const [private]
```

Subalgebra isomorphism: unfold each term within the given frame.

Definition at line 1634 of file framed\_multi\_imp.h.

References `glucat::index_set< LO, HI >::is_contiguous()`.

Referenced by `glucat::matrix_multi< Scalar_T, LO, HI >::fast_framed_multi()`.

## 6.13.5 Friends And Related Function Documentation

6.13.5.1 `exp`

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
const framed_multi_t exp (
    const framed_multi_t & val ) [friend]
```

6.13.5.2 `framed_multi`

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
template<typename Other_Scalar_T , const index_t Other_LO, const index_t Other_HI>
friend class framed_multi [friend]
```

Definition at line 160 of file framed\_multi.h.

6.13.5.3 `matrix_multi`

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
template<typename Other_Scalar_T , const index_t Other_LO, const index_t Other_HI>
friend class matrix_multi [friend]
```

Definition at line 158 of file framed\_multi.h.

#### 6.13.5.4 operator &

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
const framed_multi_t operator& (
    const framed_multi_t & lhs,
    const framed_multi_t & rhs ) [friend]
```

#### 6.13.5.5 operator%

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
const framed_multi_t operator% (
    const framed_multi_t & lhs,
    const framed_multi_t & rhs ) [friend]
```

#### 6.13.5.6 operator\*

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
const framed_multi_t operator* (
    const framed_multi_t & lhs,
    const framed_multi_t & rhs ) [friend]
```

#### 6.13.5.7 operator/

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
const framed_multi_t operator/ (
    const framed_multi_t & lhs,
    const framed_multi_t & rhs ) [friend]
```

#### 6.13.5.8 operator<< [1/2]

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
std::ostream& operator<< (
    std::ostream & os,
    const multivector_t & val ) [friend]
```

## 6.13.5.9 operator&lt;&lt; [2/2]

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
std::ostream& operator<< (
    std::ostream & os,
    const term\_t & term ) [friend]
```

## 6.13.5.10 operator&gt;&gt;

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
std::istream& operator>> (
    std::istream & s,
    multivector\_t & val ) [friend]
```

## 6.13.5.11 operator^

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
const framed\_multi\_t operator^ (
    const framed\_multi\_t & lhs,
    const framed\_multi\_t & rhs ) [friend]
```

## 6.13.5.12 operator" |

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
const framed\_multi\_t operator| (
    const framed\_multi\_t & lhs,
    const framed\_multi\_t & rhs ) [friend]
```

## 6.13.5.13 star

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
Scalar_T star (
    const framed\_multi\_t & lhs,
    const framed\_multi\_t & rhs ) [friend]
```

The documentation for this class was generated from the following files:

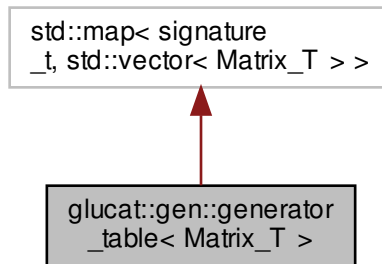
- [glucat/framed\\_multi.h](#)
- [glucat/framed\\_multi\\_imp.h](#)

## 6.14 glucat::gen::generator\_table< Matrix\_T > Class Template Reference

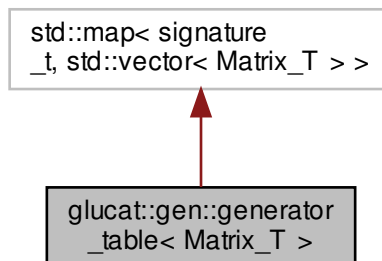
Table of generators for specific signatures.

```
#include <generation.h>
```

Inheritance diagram for glucat::gen::generator\_table< Matrix\_T >:



Collaboration diagram for glucat::gen::generator\_table< Matrix\_T >:



### Public Member Functions

- `const Matrix_T * operator()` (const `index_t` p, const `index_t` q)  
*Pointer to generators for a specific signature.*

### Static Public Member Functions

- static `generator_table< Matrix_T > & generator` ()  
*Single instance of generator table.*

## Private Member Functions

- `const std::vector< Matrix_T > & gen_vector` (const `index_t` p, const `index_t` q)  
*Construct a vector of generators for a specific signature.*
- `void gen_from_pm1_qm1` (const std::vector< Matrix\_T > &old, const `signature_t` sig)  
*Construct generators for p,q given generators for p-1,q-1.*
- `void gen_from_pm4_qp4` (const std::vector< Matrix\_T > &old, const `signature_t` sig)  
*Construct generators for p,q given generators for p-4,q+4.*
- `void gen_from_pp4_qm4` (const std::vector< Matrix\_T > &old, const `signature_t` sig)  
*Construct generators for p,q given generators for p+4,q-4.*
- `void gen_from_qp1_pm1` (const std::vector< Matrix\_T > &old, const `signature_t` sig)  
*Construct generators for p,q given generators for q+1,p-1.*
- `generator_table` ()
- `~generator_table` ()
- `generator_table` (const `generator_table` &)
- `generator_table & operator=` (const `generator_table` &)

## Friends

- class `friend_for_private_destructor`

### 6.14.1 Detailed Description

```
template<class Matrix_T>
class glucat::gen::generator_table< Matrix_T >
```

Table of generators for specific signatures.

Definition at line 47 of file generation.h.

### 6.14.2 Constructor & Destructor Documentation

#### 6.14.2.1 `generator_table()` [1/2]

```
template<class Matrix_T>
glucat::gen::generator_table< Matrix_T >::generator_table ( ) [inline], [private]
```

Definition at line 69 of file generation.h.

#### 6.14.2.2 `~generator_table()`

```
template<class Matrix_T>
glucat::gen::generator_table< Matrix_T >::~~generator_table ( ) [inline], [private]
```

Definition at line 70 of file generation.h.

### 6.14.2.3 generator\_table() [2/2]

```
template<class Matrix_T>
glucat::gen::generator_table< Matrix_T >::generator_table (
    const generator_table< Matrix_T > & ) [private]
```

## 6.14.3 Member Function Documentation

### 6.14.3.1 gen\_from\_pm1\_qm1()

```
template<class Matrix_T >
void glucat::gen::generator_table< Matrix_T >::gen_from_pm1_qm1 (
    const std::vector< Matrix_T > & old,
    const signature_t sig ) [private]
```

Construct generators for p,q given generators for p-1,q-1.

Definition at line 127 of file generation\_imp.h.

References glucat::matrix::mono\_kron().

### 6.14.3.2 gen\_from\_pm4\_qp4()

```
template<class Matrix_T >
void glucat::gen::generator_table< Matrix_T >::gen_from_pm4_qp4 (
    const std::vector< Matrix_T > & old,
    const signature_t sig ) [private]
```

Construct generators for p,q given generators for p-4,q+4.

Definition at line 164 of file generation\_imp.h.

References glucat::matrix::mono\_prod().

### 6.14.3.3 gen\_from\_pp4\_qm4()

```
template<class Matrix_T >
void glucat::gen::generator_table< Matrix_T >::gen_from_pp4_qm4 (
    const std::vector< Matrix_T > & old,
    const signature_t sig ) [private]
```

Construct generators for p,q given generators for p+4,q-4.

Definition at line 195 of file generation\_imp.h.

References glucat::matrix::mono\_prod().

## 6.14.3.4 gen\_from\_qp1\_pm1()

```
template<class Matrix_T >
void glucat::gen::generator_table< Matrix_T >::gen_from_qp1_pm1 (
    const std::vector< Matrix_T > & old,
    const signature_t sig ) [private]
```

Construct generators for p,q given generators for q+1,p-1.

Definition at line 225 of file generation\_imp.h.

References glucat::matrix::mono\_prod().

## 6.14.3.5 gen\_vector()

```
template<class Matrix_T >
const std::vector< Matrix_T > & glucat::gen::generator_table< Matrix_T >::gen_vector (
    const index_t p,
    const index_t q ) [private]
```

Construct a vector of generators for a specific signature.

Definition at line 80 of file generation\_imp.h.

References glucat::pos\_mod().

## 6.14.3.6 generator()

```
template<class Matrix_T >
generator_table< Matrix_T > & glucat::gen::generator_table< Matrix_T >::generator ( ) [static]
```

Single instance of generator table.

Definition at line 50 of file generation\_imp.h.

Referenced by glucat::matrix\_multi< Scalar\_T, LO, HI >::basis\_element().

## 6.14.3.7 operator&gt;()()

```
template<class Matrix_T >
const Matrix_T * glucat::gen::generator_table< Matrix_T >::operator() (
    const index_t p,
    const index_t q ) [inline]
```

Pointer to generators for a specific signature.

Definition at line 59 of file generation\_imp.h.

References glucat::gen::offset\_to\_super, and glucat::pos\_mod().

### 6.14.3.8 operator=()

```
template<class Matrix_T>
generator_table& glucat::gen::generator_table< Matrix_T >::operator= (
    const generator_table< Matrix_T > & ) [private]
```

## 6.14.4 Friends And Related Function Documentation

### 6.14.4.1 friend\_for\_private\_destructor

```
template<class Matrix_T>
friend class friend_for_private_destructor [friend]
```

Friend declaration to avoid compiler warning: "... only defines a private destructor and has no friends" Ref: Carlos O'Ryan, ACE <http://doc.ece.uci.edu>

Definition at line 77 of file generation.h.

The documentation for this class was generated from the following files:

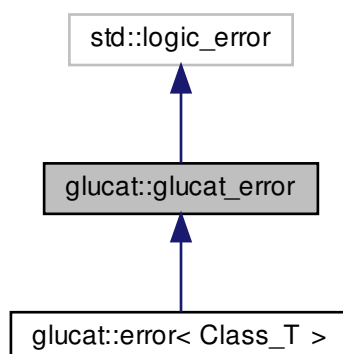
- [glucat/generation.h](#)
- [glucat/generation\\_imp.h](#)

## 6.15 glucat::glucat\_error Class Reference

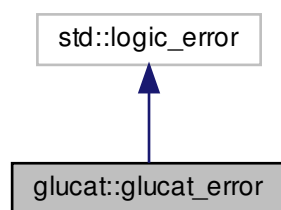
Abstract exception class.

```
#include <errors.h>
```

Inheritance diagram for glucat::glucat\_error:



Collaboration diagram for glucat::glucat\_error:



### Public Member Functions

- [glucat\\_error](#) (const std::string &context, const std::string &msg)
- [~glucat\\_error](#) () throw ()
- virtual const std::string [heading](#) () const =0 throw ()
- virtual const std::string [classname](#) () const =0 throw ()
- virtual void [print\\_error\\_msg](#) () const =0

### Public Attributes

- std::string [name](#)

#### 6.15.1 Detailed Description

Abstract exception class.

Definition at line 41 of file errors.h.

#### 6.15.2 Constructor & Destructor Documentation

##### 6.15.2.1 glucat\_error()

```
glucat::glucat_error::glucat_error (  
    const std::string & context,  
    const std::string & msg ) [inline]
```

Definition at line 44 of file errors.h.

#### 6.15.2.2 ~glucat\_error()

```
glucat::glucat_error::~~glucat_error ( ) throw )    [inline]
```

Definition at line 47 of file errors.h.

### 6.15.3 Member Function Documentation

#### 6.15.3.1 classname()

```
virtual const std::string glucat::glucat_error::classname ( ) const throw )    [pure virtual]
```

Implemented in [glucat::error< Class\\_T >](#).

#### 6.15.3.2 heading()

```
virtual const std::string glucat::glucat_error::heading ( ) const throw )    [pure virtual]
```

Implemented in [glucat::error< Class\\_T >](#).

#### 6.15.3.3 print\_error\_msg()

```
virtual void glucat::glucat_error::print_error_msg ( ) const    [pure virtual]
```

Implemented in [glucat::error< Class\\_T >](#).

### 6.15.4 Member Data Documentation

#### 6.15.4.1 name

```
std::string glucat::glucat_error::name
```

Definition at line 52 of file errors.h.

The documentation for this class was generated from the following file:

- [glucat/errors.h](#)

## 6.16 glucat::framed\_multi< Scalar\_T, LO, HI >::hash\_size\_t Class Reference

### Public Member Functions

- [hash\\_size\\_t](#) (size\_t hash\_size)
- [size\\_t operator\(\)](#) () const

### Private Attributes

- [size\\_t n](#)

### 6.16.1 Detailed Description

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
class glucat::framed_multi< Scalar_T, LO, HI >::hash_size_t
```

Definition at line 180 of file framed\_multi.h.

### 6.16.2 Constructor & Destructor Documentation

#### 6.16.2.1 hash\_size\_t()

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
glucat::framed_multi< Scalar_T, LO, HI >::hash_size_t::hash_size_t (
    size_t hash_size ) [inline]
```

Definition at line 183 of file framed\_multi.h.

### 6.16.3 Member Function Documentation

#### 6.16.3.1 operator()()

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
size_t glucat::framed_multi< Scalar_T, LO, HI >::hash_size_t::operator() () const [inline]
```

Definition at line 186 of file framed\_multi.h.

References [glucat::framed\\_multi< Scalar\\_T, LO, HI >::hash\\_size\\_t::n](#).

## 6.16.4 Member Data Documentation

### 6.16.4.1 n

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
size_t glucat::framed_multi< Scalar_T, LO, HI >::hash_size_t::n [private]
```

Definition at line 189 of file framed\_multi.h.

Referenced by glucat::framed\_multi< Scalar\_T, LO, HI >::hash\_size\_t::operator()().

The documentation for this class was generated from the following file:

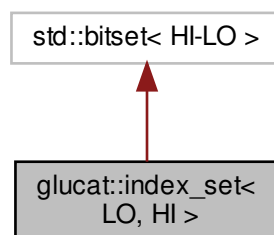
- glucat/framed\_multi.h

## 6.17 glucat::index\_set< LO, HI > Class Template Reference

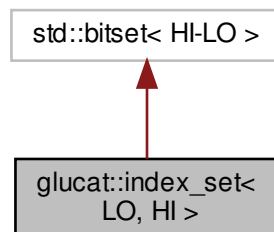
Index set class based on std::bitset<> in Gnu standard C++ library.

```
#include <index_set.h>
```

Inheritance diagram for glucat::index\_set< LO, HI >:



Collaboration diagram for glucat::index\_set< LO, HI >:



## Classes

- class [reference](#)  
*Index set member reference.*

## Public Types

- typedef [index\\_set](#) [index\\_set\\_t](#)
- typedef std::pair< [index\\_t](#), [index\\_t](#) > [index\\_pair\\_t](#)

## Public Member Functions

- [index\\_set](#) ()  
*Default constructor creates an empty set.*
- [index\\_set](#) (const [bitset\\_t](#) bst)  
*Constructor from [bitset\\_t](#).*
- [index\\_set](#) (const [index\\_t](#) idx)  
*Constructor from [index](#).*
- [index\\_set](#) (const [set\\_value\\_t](#) folded\_val, const [index\\_set\\_t](#) frm, const bool prechecked=false)  
*Constructor from set value of an index set folded within the given frame.*
- [index\\_set](#) (const [index\\_pair\\_t](#) &range, const bool prechecked=false)  
*Constructor from range of indices from *range.first* to *range.second*.*
- [index\\_set](#) (const std::string &str)  
*Constructor from string.*
- bool [operator==](#) (const [index\\_set\\_t](#) rhs) const  
*Equality.*
- bool [operator!=](#) (const [index\\_set\\_t](#) rhs) const  
*Inequality.*
- [index\\_set\\_t](#) [operator~](#) () const  
*Set complement: not.*
- [index\\_set\\_t](#) & [operator^](#) = (const [index\\_set\\_t](#) rhs)  
*Symmetric set difference: exclusive or.*
- [index\\_set\\_t](#) & [operator &=](#) (const [index\\_set\\_t](#) rhs)  
*Set intersection: and.*
- [index\\_set\\_t](#) & [operator|=](#) (const [index\\_set\\_t](#) rhs)  
*Set union: or.*
- bool [operator\[\]](#) (const [index\\_t](#) idx) const  
*Subscripting: Test *idx* for membership: test value of bit *idx*.*
- bool [test](#) (const [index\\_t](#) idx) const  
*Test *idx* for membership: test value of bit *idx*.*
- [index\\_set\\_t](#) & [set](#) ()  
*Include all indices except 0: set all bits except 0.*
- [index\\_set\\_t](#) & [set](#) (const [index\\_t](#) idx)  
*Include *idx*: Set bit at *idx* if *idx* != 0.*
- [index\\_set\\_t](#) & [set](#) (const [index\\_t](#) idx, const int val)  
*Set membership of *idx* to *val* if *idx* != 0: Set bit at *idx* to *val* if *idx* != 0.*
- [index\\_set\\_t](#) & [reset](#) ()  
*Make set empty: Set all bits to 0.*
- [index\\_set\\_t](#) & [reset](#) (const [index\\_t](#) idx)  
*Exclude *idx*: Set bit at *idx* to 0.*

- `index_set_t & flip ()`  
*Set complement, except 0: flip all bits, except 0.*
- `index_set_t & flip (const index_t idx)`  
*Complement membership of idx if idx != 0: flip bit at idx if idx != 0.*
- `index_t count () const`  
*Cardinality: Number of indices included in set.*
- `index_t count_neg () const`  
*Number of negative indices included in set.*
- `index_t count_pos () const`  
*Number of positive indices included in set.*
- `index_t min () const`  
*Minimum member.*
- `index_t max () const`  
*Maximum member.*
- `bool operator< (const index_set_t rhs) const`  
*Less than operator used for comparisons, map, etc.*
- `bool is_contiguous () const`  
*Determine if the index set is contiguous, ie. has no gaps.*
- `const index_set_t fold () const`  
*Fold this index set within itself as a frame.*
- `const index_set_t fold (const index_set_t frm, const bool prechecked=false) const`  
*Fold this index set within the given frame.*
- `const index_set_t unfold (const index_set_t frm, const bool prechecked=false) const`  
*Unfold this index set within the given frame.*
- `set_value_t value_of_fold (const index_set_t frm) const`  
*The set value of the fold of this index set within the given frame.*
- `int sign_of_mult (const index_set_t ist) const`  
*Sign of geometric product of two Clifford basis elements.*
- `int sign_of_square () const`  
*Sign of geometric square of a Clifford basis element.*
- `size_t hash_fn () const`  
*Hash function.*
- `reference operator[] (index_t idx)`  
*Subscripting: Element access.*

## Static Public Member Functions

- `static const std::string classname ()`

## Static Public Attributes

- `static const index_t v_lo = LO`
- `static const index_t v_hi = HI`

## Private Types

- `typedef std::bitset< HI-LO > bitset_t`
- `typedef error< index_set > error_t`

## Private Member Functions

- `BOOST_STATIC_ASSERT` ((LO<=0) &&(0<=HI) &&(LO< HI) &&(-LO< \_GLUCAT\_BITS\_PER\_ULONG) &&(HI< \_GLUCAT\_BITS\_PER\_ULONG) &&(HI-LO<=\_GLUCAT\_BITS\_PER\_ULONG))
- `bool lex_less_than` (const `index_set_t` rhs) const  
*Lexicographic ordering of two sets: \*this < rhs.*

## Friends

- class `reference`
- const `index_set_t` `operator^` (const `index_set_t` &lhs, const `index_set_t` &rhs)
- const `index_set_t` `operator &` (const `index_set_t` &lhs, const `index_set_t` &rhs)
- const `index_set_t` `operator|` (const `index_set_t` &lhs, const `index_set_t` &rhs)
- int `compare` (const `index_set_t` &lhs, const `index_set_t` &rhs)

### 6.17.1 Detailed Description

```
template<const index_t LO, const index_t HI>
class glucat::index_set< LO, HI >
```

Index set class based on `std::bitset<>` in Gnu standard C++ library.

Definition at line 45 of file `index_set.h`.

### 6.17.2 Member Typedef Documentation

#### 6.17.2.1 `bitset_t`

```
template<const index_t LO, const index_t HI>
typedef std::bitset<HI-LO> glucat::index_set< LO, HI >::bitset_t [private]
```

Definition at line 81 of file `index_set.h`.

#### 6.17.2.2 `error_t`

```
template<const index_t LO, const index_t HI>
typedef error<index_set> glucat::index_set< LO, HI >::error_t [private]
```

Definition at line 82 of file `index_set.h`.

### 6.17.2.3 index\_pair\_t

```
template<const index_t LO, const index_t HI>
typedef std::pair<index_t, index_t> glucat::index_set< LO, HI >::index_pair_t
```

Definition at line 85 of file index\_set.h.

### 6.17.2.4 index\_set\_t

```
template<const index_t LO, const index_t HI>
typedef index_set glucat::index_set< LO, HI >::index_set_t
```

Definition at line 84 of file index\_set.h.

## 6.17.3 Constructor & Destructor Documentation

### 6.17.3.1 index\_set() [1/6]

```
template<const index_t LO, const index_t HI>
glucal::index_set< LO, HI >::index_set ( ) [inline]
```

Default constructor creates an empty set.

Definition at line 92 of file index\_set.h.

### 6.17.3.2 index\_set() [2/6]

```
template<const index_t LO, const index_t HI>
glucal::index_set< LO, HI >::index_set (
    const bitset_t bst )
```

Constructor from bitset\_t.

Definition at line 61 of file index\_set\_imp.h.

**6.17.3.3 index\_set()** [3/6]

```
template<const index_t LO, const index_t HI>
glucat::index_set< LO, HI >::index_set (
    const index_t idx )
```

Constructor from index.

Constructor from index value.

Definition at line 55 of file index\_set\_imp.h.

**6.17.3.4 index\_set()** [4/6]

```
template<const index_t LO, const index_t HI>
glucat::index_set< LO, HI >::index_set (
    const set_value_t folded_val,
    const index_set_t frm,
    const bool prechecked = false )
```

Constructor from set value of an index set folded within the given frame.

Definition at line 68 of file index\_set\_imp.h.

References glucat::index\_set< LO, HI >::count(), glucat::index\_set< LO, HI >::fold(), glucat::index\_set< LO, HI >::min(), and glucat::index\_set< LO, HI >::unfold().

**6.17.3.5 index\_set()** [5/6]

```
template<const index_t LO, const index_t HI>
glucat::index_set< LO, HI >::index_set (
    const index_pair_t & range,
    const bool prechecked = false )
```

Constructor from range of indices from range.first to range.second.

Definition at line 82 of file index\_set\_imp.h.

**6.17.3.6 index\_set()** [6/6]

```
template<const index_t LO, const index_t HI>
glucat::index_set< LO, HI >::index_set (
    const std::string & str )
```

Constructor from string.

Definition at line 102 of file index\_set\_imp.h.

## 6.17.4 Member Function Documentation

### 6.17.4.1 BOOST\_STATIC\_ASSERT()

```
template<const index_t LO, const index_t HI>
glucat::index_set< LO, HI >::BOOST_STATIC_ASSERT (
    (LO<=0) && (0<=HI) && (LO< HI) && (-LO< _GLUCAT_BITS_PER_ULONG) && (HI< _GLUCAT_BITS_PER_ULONG) && (HI-LO<=_GLUCAT_BITS_PER_ULONG) ) [private]
```

### 6.17.4.2 classname()

```
template<const index_t LO, const index_t HI>
const std::string glucat::index_set< LO, HI >::classname ( ) [inline], [static]
```

Definition at line 49 of file index\_set\_imp.h.

### 6.17.4.3 count()

```
template<const index_t LO, const index_t HI>
index_t glucat::index_set< LO, HI >::count ( ) const [inline]
```

Cardinality: Number of indices included in set.

Definition at line 344 of file index\_set\_imp.h.

Referenced by glucat::index\_set< LO, HI >::count\_neg(), glucat::index\_set< LO, HI >::count\_pos(), glucat::framed\_multi< Scalar\_T, LO, HI >::framed\_multi(), glucat::index\_set< LO, HI >::index\_set(), glucat::matrix\_multi< Scalar\_T, LO, HI >::matrix\_multi(), glucat::index\_set< LO, HI >::operator<(), and glucat::framed\_multi< Scalar\_T, LO, HI >::random().

### 6.17.4.4 count\_neg()

```
template<const index_t LO, const index_t HI>
index_t glucat::index_set< LO, HI >::count_neg ( ) const [inline]
```

Number of negative indices included in set.

Definition at line 364 of file index\_set\_imp.h.

References glucat::index\_set< LO, HI >::count().

Referenced by glucat::framed\_multi< Scalar\_T, LO, HI >::fast\_matrix\_multi(), and glucat::folded\_dim().

## 6.17.4.5 count\_pos()

```
template<const index_t LO, const index_t HI>
index_t glucat::index_set< LO, HI >::count_pos ( ) const [inline]
```

Number of positive indices included in set.

Definition at line 376 of file index\_set\_imp.h.

References glucat::index\_set< LO, HI >::count().

Referenced by glucat::framed\_multi< Scalar\_T, LO, HI >::fast\_matrix\_multi(), and glucat::folded\_dim().

## 6.17.4.6 flip() [1/2]

```
template<const index_t LO, const index_t HI>
index_set< LO, HI > & glucat::index_set< LO, HI >::flip ( ) [inline]
```

Set complement, except 0: flip all bits, except 0.

Definition at line 319 of file index\_set\_imp.h.

## 6.17.4.7 flip() [2/2]

```
template<const index_t LO, const index_t HI>
index_set< LO, HI > & glucat::index_set< LO, HI >::flip (
    const index_t idx ) [inline]
```

Complement membership of idx if idx != 0: flip bit at idx if idx != 0.

Definition at line 330 of file index\_set\_imp.h.

## 6.17.4.8 fold() [1/2]

```
template<const index_t LO, const index_t HI>
const index_set< LO, HI > glucat::index_set< LO, HI >::fold ( ) const [inline]
```

Fold this index set within itself as a frame.

Definition at line 748 of file index\_set\_imp.h.

Referenced by glucat::matrix\_multi< Scalar\_T, LO, HI >::basis\_element(), glucat::index\_set< LO, HI >::index\_set(), and glucat::index\_set< LO, HI >::value\_of\_fold().

**6.17.4.9 fold()** [2/2]

```
template<const index_t LO, const index_t HI>
const index_set< LO, HI > glucat::index_set< LO, HI >::fold (
    const index_set_t frm,
    const bool prechecked = false ) const
```

Fold this index set within the given frame.

Definition at line 756 of file index\_set\_imp.h.

References glucat::index\_set< LO, HI >::max(), glucat::index\_set< LO, HI >::min(), glucat::index\_set< LO, HI >::set(), and glucat::index\_set< LO, HI >::test().

**6.17.4.10 hash\_fn()**

```
template<const index_t LO, const index_t HI>
size_t glucat::index_set< LO, HI >::hash_fn ( ) const [inline]
```

Hash function.

Definition at line 948 of file index\_set\_imp.h.

Referenced by glucat::index\_set\_hash< LO, HI >::operator()().

**6.17.4.11 is\_contiguous()**

```
template<const index_t LO, const index_t HI>
bool glucat::index_set< LO, HI >::is_contiguous ( ) const [inline]
```

Determine if the index set is contiguous, ie. has no gaps.

Determine if the index set is contiguous, ie. has no gaps when 0 is included.

Definition at line 732 of file index\_set\_imp.h.

Referenced by glucat::framed\_multi< Scalar\_T, LO, HI >::fold(), and glucat::framed\_multi< Scalar\_T, LO, HI >::unfold().

**6.17.4.12 lex\_less\_than()**

```
template<const index_t LO, const index_t HI>
bool glucat::index_set< LO, HI >::lex_less_than (
    const index_set_t rhs ) const [inline], [private]
```

Lexicographic ordering of two sets: \*this < rhs.

Definition at line 588 of file index\_set\_imp.h.

Referenced by glucat::compare().

## 6.17.4.13 max()

```
template<const index_t LO, const index_t HI>
index_t glucat::index_set< LO, HI >::max ( ) const
```

Maximum member.

Maximum member, or 0 if none.

Definition at line 550 of file index\_set\_imp.h.

Referenced by PyClical.index\_set::\_\_iter\_\_(), glucat::matrix\_multi< Scalar\_T, LO, HI >::basis\_element(), glucat::index\_set< LO, HI >::fold(), glucat::framed\_multi< Scalar\_T, LO, HI >::framed\_multi(), glucat::matrix\_multi< Scalar\_T, LO, HI >::matrix\_multi(), and glucat::index\_set< LO, HI >::unfold().

## 6.17.4.14 min()

```
template<const index_t LO, const index_t HI>
index_t glucat::index_set< LO, HI >::min ( ) const
```

Minimum member.

Minimum member, or 0 if none.

Definition at line 461 of file index\_set\_imp.h.

Referenced by PyClical.index\_set::\_\_iter\_\_(), glucat::matrix\_multi< Scalar\_T, LO, HI >::basis\_element(), glucat::index\_set< LO, HI >::fold(), glucat::framed\_multi< Scalar\_T, LO, HI >::framed\_multi(), glucat::index\_set< LO, HI >::index\_set(), glucat::matrix\_multi< Scalar\_T, LO, HI >::matrix\_multi(), glucat::index\_set< LO, HI >::unfold(), and glucat::index\_set< LO, HI >::value\_of\_fold().

## 6.17.4.15 operator &amp;=()

```
template<const index_t LO, const index_t HI>
index_set_t& glucat::index_set< LO, HI >::operator&= (
    const index_set_t rhs )
```

Set intersection: and.

## 6.17.4.16 operator !=()

```
template<const index_t LO, const index_t HI>
bool glucat::index_set< LO, HI >::operator!= (
    const index_set_t rhs ) const [inline]
```

Inequality.

Definition at line 130 of file index\_set\_imp.h.

**6.17.4.17 operator<()**

```
template<const index_t LO, const index_t HI>
bool glucat::index_set< LO, HI >::operator< (
    const index_set_t rhs ) const [inline]
```

Less than operator used for comparisons, map, etc.

Definition at line 597 of file index\_set\_imp.h.

References glucat::index\_set< LO, HI >::count().

**6.17.4.18 operator==()**

```
template<const index_t LO, const index_t HI>
bool glucat::index_set< LO, HI >::operator== (
    const index_set_t rhs ) const [inline]
```

Equality.

Definition at line 119 of file index\_set\_imp.h.

**6.17.4.19 operator[]()** [1/2]

```
template<const index_t LO, const index_t HI>
bool glucat::index_set< LO, HI >::operator[] (
    const index_t idx ) const [inline]
```

Subscripting: Test idx for membership: test value of bit idx.

Definition at line 232 of file index\_set\_imp.h.

**6.17.4.20 operator[]()** [2/2]

```
template<const index_t LO, const index_t HI>
index_set< LO, HI >::reference glucat::index_set< LO, HI >::operator[] (
    index_t idx ) [inline]
```

Subscripting: Element access.

Definition at line 224 of file index\_set\_imp.h.

**6.17.4.21 operator^=()**

```
template<const index_t LO, const index_t HI>
index_set< LO, HI > & glucat::index_set< LO, HI >::operator^= (
    const index_set_t rhs ) [inline]
```

Symmetric set difference: exclusive or.

Definition at line 149 of file index\_set\_imp.h.

**6.17.4.22 operator" |=()**

```
template<const index_t LO, const index_t HI>
index_set< LO, HI > & glucat::index_set< LO, HI >::operator|= (
    const index_set_t rhs ) [inline]
```

Set union: or.

Definition at line 199 of file index\_set\_imp.h.

**6.17.4.23 operator~()**

```
template<const index_t LO, const index_t HI>
index_set< LO, HI > glucat::index_set< LO, HI >::operator~ ( ) const [inline]
```

Set complement: not.

Definition at line 141 of file index\_set\_imp.h.

**6.17.4.24 reset()** [1/2]

```
template<const index_t LO, const index_t HI>
index_set< LO, HI > & glucat::index_set< LO, HI >::reset ( ) [inline]
```

Make set empty: Set all bits to 0.

Definition at line 294 of file index\_set\_imp.h.

**6.17.4.25 reset()** [2/2]

```
template<const index_t LO, const index_t HI>
index_set< LO, HI > & glucat::index_set< LO, HI >::reset (
    const index_t idx ) [inline]
```

Exclude idx: Set bit at idx to 0.

Definition at line 305 of file index\_set\_imp.h.

**6.17.4.26 set()** [1/3]

```
template<const index_t LO, const index_t HI>
index_set< LO, HI > & glucat::index_set< LO, HI >::set ( ) [inline]
```

Include all indices except 0: set all bits except 0.

Definition at line 255 of file index\_set\_imp.h.

Referenced by glucat::index\_set< LO, HI >::fold(), glucat::operator>>(), and glucat::index\_set< LO, HI >↵::unfold().

**6.17.4.27 set()** [2/3]

```
template<const index_t LO, const index_t HI>
index_set< LO, HI > & glucat::index_set< LO, HI >::set (
    const index_t idx ) [inline]
```

Include idx: Set bit at idx if idx != 0.

Definition at line 266 of file index\_set\_imp.h.

**6.17.4.28 set()** [3/3]

```
template<const index_t LO, const index_t HI>
index_set< LO, HI > & glucat::index_set< LO, HI >::set (
    const index_t idx,
    const int val ) [inline]
```

Set membership of idx to val if idx != 0: Set bit at idx to val if idx != 0.

Definition at line 280 of file index\_set\_imp.h.

**6.17.4.29 sign\_of\_mult()**

```
template<const index_t LO, const index_t HI>
int glucat::index_set< LO, HI >::sign_of_mult (
    const index_set_t ist ) const
```

Sign of geometric product of two Clifford basis elements.

Definition at line 879 of file index\_set\_imp.h.

References glucat::inverse\_gray(), and glucat::inverse\_reversed\_gray().

**6.17.4.30 sign\_of\_square()**

```
template<const index_t LO, const index_t HI>
int glucat::index_set< LO, HI >::sign_of_square ( ) const [inline]
```

Sign of geometric square of a Clifford basis element.

Definition at line 928 of file index\_set\_imp.h.

**6.17.4.31 test()**

```
template<const index_t LO, const index_t HI>
bool glucat::index_set< LO, HI >::test (
    const index_t idx ) const [inline]
```

Test idx for membership: test value of bit idx.

Definition at line 240 of file index\_set\_imp.h.

Referenced by glucat::index\_set< LO, HI >::fold(), and glucat::index\_set< LO, HI >::unfold().

**6.17.4.32 unfold()**

```
template<const index_t LO, const index_t HI>
const index_set< LO, HI > glucat::index_set< LO, HI >::unfold (
    const index_set_t frm,
    const bool prechecked = false ) const
```

Unfold this index set within the given frame.

Definition at line 794 of file index\_set\_imp.h.

References glucat::index\_set< LO, HI >::max(), glucat::index\_set< LO, HI >::min(), glucat::index\_set< LO, HI >::set(), and glucat::index\_set< LO, HI >::test().

Referenced by glucat::index\_set< LO, HI >::index\_set().

#### 6.17.4.33 value\_of\_fold()

```
template<const index_t LO, const index_t HI>
set_value_t glucat::index_set< LO, HI >::value_of_fold (
    const index_set_t frm ) const [inline]
```

The set value of the fold of this index set within the given frame.

Definition at line 828 of file index\_set\_imp.h.

References glucat::index\_set< LO, HI >::fold(), and glucat::index\_set< LO, HI >::min().

### 6.17.5 Friends And Related Function Documentation

#### 6.17.5.1 compare

```
template<const index_t LO, const index_t HI>
int compare (
    const index_set_t & lhs,
    const index_set_t & rhs ) [friend]
```

#### 6.17.5.2 operator &

```
template<const index_t LO, const index_t HI>
const index_set_t operator& (
    const index_set_t & lhs,
    const index_set_t & rhs ) [friend]
```

#### 6.17.5.3 operator^

```
template<const index_t LO, const index_t HI>
const index_set_t operator^ (
    const index_set_t & lhs,
    const index_set_t & rhs ) [friend]
```

#### 6.17.5.4 operator" |

```
template<const index_t LO, const index_t HI>
const index_set_t operator| (
    const index_set_t & lhs,
    const index_set_t & rhs ) [friend]
```

#### 6.17.5.5 reference

```
template<const index_t LO, const index_t HI>  
friend class reference [friend]
```

Definition at line 173 of file index\_set.h.

### 6.17.6 Member Data Documentation

#### 6.17.6.1 v\_hi

```
template<const index_t LO, const index_t HI>  
const index_t glucat::index_set< LO, HI >::v_hi = HI [static]
```

Definition at line 88 of file index\_set.h.

#### 6.17.6.2 v\_lo

```
template<const index_t LO, const index_t HI>  
const index_t glucat::index_set< LO, HI >::v_lo = LO [static]
```

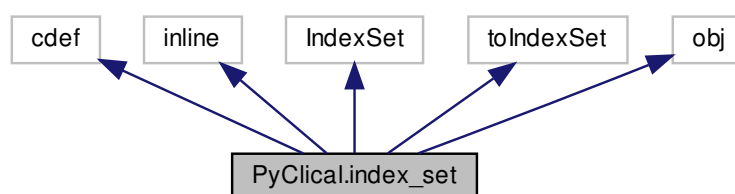
Definition at line 87 of file index\_set.h.

The documentation for this class was generated from the following files:

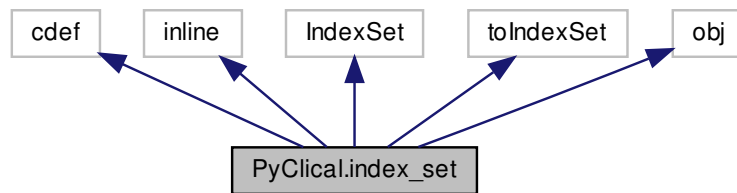
- glucat/index\_set.h
- glucat/index\_set\_imp.h

## 6.18 PyClical.index\_set Class Reference

Inheritance diagram for PyClical.index\_set:



Collaboration diagram for PyClical.index\_set:



## Public Member Functions

- `def __cinit__(self, other=0)`
- `def __dealloc__(self)`
- `def __richcmp__(lhs, rhs, int, op)`
- `def __setitem__(self, idx, val)`
- `def __getitem__(self, idx)`
- `def __contains__(self, idx)`
- `def __iter__(self)`
- `def __invert__(self)`
- `def __xor__(lhs, rhs)`
- `def __ixor__(self, rhs)`
- `def __and__(lhs, rhs)`
- `def __iand__(self, rhs)`
- `def __or__(lhs, rhs)`
- `def __ior__(self, rhs)`
- `def count(self)`
- `def count_neg(self)`
- `def count_pos(self)`
- `def min(self)`
- `def max(self)`
- `def hash_fn(self)`
- `def sign_of_mult(self, rhs)`
- `def sign_of_square(self)`
- `def __repr__(self)`
- `def __str__(self)`

## Public Attributes

- `instance`

## 6.18.1 Detailed Description

Return the C++ `IndexSet` instance wrapped by `index_set(obj)`.

Python class `index_set` wraps C++ class `IndexSet`.

Definition at line 39 of file `PyClical.pyx`.

## 6.18.2 Member Function Documentation

### 6.18.2.1 \_\_and\_\_()

```
def PyClical.index_set.__and__ (
    lhs,
    rhs )
```

Set intersection: and.

```
>>> print index_set({1}) & index_set({2})
{}
>>> print index_set({1,2}) & index_set({2})
{2}
```

Definition at line 269 of file PyClical.pyx.

### 6.18.2.2 \_\_cinit\_\_()

```
def PyClical.index_set.__cinit__ (
    self,
    other = 0 )
```

Construct an object of type index\_set.

```
>>> print index_set(1)
{1}
>>> print index_set({1,2})
{1,2}
>>> print index_set(index_set({1,2}))
{1,2}
>>> print index_set({1,2})
{1,2}
>>> print index_set({1,2,1})
{1,2}
>>> print index_set("{1,2,1}")
{1,2}
>>> print index_set("")
{}
```

Definition at line 73 of file PyClical.pyx.

### 6.18.2.3 `__contains__()`

```
def PyClical.index_set.__contains__ (
    self,
    idx )
```

Check that an `index_set` object contains the index `idx`: `idx` in `self`.

```
>>> 1 in index_set({1})
True
>>> 2 in index_set({1})
False
>>> -1 in index_set({2})
False
>>> 1 in index_set({2})
False
>>> 2 in index_set({2})
True
>>> 33 in index_set({2})
False
```

Definition at line 208 of file `PyClical.pyx`.

References `PyClical.index_set.instance`.

### 6.18.2.4 `__dealloc__()`

```
def PyClical.index_set.__dealloc__ (
    self )
```

Clean up by deallocating the instance of C++ class `IndexSet`.

Definition at line 114 of file `PyClical.pyx`.

References `PyClical.index_set.instance`.

### 6.18.2.5 `__getitem__()`

```
def PyClical.index_set.__getitem__ (
    self,
    idx )
```

Get the value of an `index_set` object at an index.

```
>>> index_set({1})[1]
True
>>> index_set({1})[2]
False
>>> index_set({2})[-1]
False
>>> index_set({2})[1]
False
>>> index_set({2})[2]
True
>>> index_set({2})[33]
False
```

Definition at line 189 of file `PyClical.pyx`.

References `PyClical.index_set.instance`.

#### 6.18.2.6 \_\_iand\_\_()

```
def PyClical.index_set.__iand__ (
    self,
    rhs )

Set intersection: and.

>>> x = index_set({1}); x &= index_set({2}); print x
{}
>>> x = index_set({1,2}); x &= index_set({2}); print x
{2}
```

Definition at line 280 of file PyClical.pyx.

#### 6.18.2.7 \_\_invert\_\_()

```
def PyClical.index_set.__invert__ (
    self )

Set complement: not.

>>> print ~index_set({-16,-15,-14,-13,-12,-11,-10,-9,-8,-7,-6,-5,-4,-3,-2,-1,1,2,3,4,5,6,7,8,9,10,11,12,13,14,
{-32,-31,-30,-29,-28,-27,-26,-25,-24,-23,-22,-21,-20,-19,-18,-17,17,18,19,20,21,22,23,24,25,26,27,28,29,30,31,
```

Definition at line 238 of file PyClical.pyx.

References PyClical.index\_set.instance.

#### 6.18.2.8 \_\_ior\_\_()

```
def PyClical.index_set.__ior__ (
    self,
    rhs )

Set union: or.

>>> x = index_set({1}); x |= index_set({2}); print x
{1,2}
>>> x = index_set({1,2}); x |= index_set({2}); print x
{1,2}
```

Definition at line 302 of file PyClical.pyx.

#### 6.18.2.9 `__iter__()`

```
def PyClical.index_set.__iter__ (
    self )
```

Iterate over the indices of an `index_set`.

```
>>> for i in index_set({-3,4,7}): print i,
-3 4 7
```

Definition at line 227 of file `PyClical.pyx`.

References `glucat::index_set< LO, HI >.max()`, `PyClical.index_set.max()`, `glucat::index_set< LO, HI >.min()`, and `PyClical.index_set.min()`.

#### 6.18.2.10 `__ixor__()`

```
def PyClical.index_set.__ixor__ (
    self,
    rhs )
```

Symmetric set difference: exclusive or.

```
>>> x = index_set({1}); x ^= index_set({2}); print x
{1,2}
>>> x = index_set({1,2}); x ^= index_set({2}); print x
{1}
```

Definition at line 258 of file `PyClical.pyx`.

#### 6.18.2.11 `__or__()`

```
def PyClical.index_set.__or__ (
    lhs,
    rhs )
```

Set union: or.

```
>>> print index_set({1}) | index_set({2})
{1,2}
>>> print index_set({1,2}) | index_set({2})
{1,2}
```

Definition at line 291 of file `PyClical.pyx`.

**6.18.2.12 `__repr__()`**

```
def PyClical.index_set.__repr__ (
    self )
```

The “official” string representation of self.

```
>>> index_set({1,2}).__repr__()
'index_set({1,2})'
>>> repr(index_set({1,2}))
'index_set({1,2})'
```

Definition at line 382 of file PyClical.pyx.

References `index_set_to_repr()`.

**6.18.2.13 `__richcmp__()`**

```
def PyClical.index_set.__richcmp__ (
    lhs,
    rhs,
    int,
    op )
```

Compare two objects of class `index_set`.

```
>>> index_set(1) == index_set({1})
True
>>> index_set({1}) != index_set({1})
False
>>> index_set({1}) != index_set({2})
True
>>> index_set({1}) == index_set({2})
False
>>> index_set({1}) < index_set({2})
True
>>> index_set({1}) <= index_set({2})
True
>>> index_set({1}) > index_set({2})
False
>>> index_set({1}) >= index_set({2})
False
```

Definition at line 120 of file PyClical.pyx.

**6.18.2.14 `__setitem__()`**

```
def PyClical.index_set.__setitem__ (
    self,
    idx,
    val )
```

Set the value of an `index_set` object at index `idx` to value `val`.

```
>>> s=index_set({1}); s[2] = True; print s
{1,2}
>>> s=index_set({1,2}); s[1] = False; print s
{2}
```

Definition at line 177 of file PyClical.pyx.

References `PyClical.index_set.instance`.

#### 6.18.2.15 `__str__()`

```
def PyClical.index_set.__str__ (
    self )
```

The “informal” string representation of self.

```
>>> index_set({1,2}).__str__()
' {1,2} '
>>> str(index_set({1,2}))
' {1,2} '
```

Definition at line 393 of file `PyClical.pyx`.

References `index_set_to_str()`.

#### 6.18.2.16 `__xor__()`

```
def PyClical.index_set.__xor__ (
    lhs,
    rhs )
```

Symmetric set difference: exclusive or.

```
>>> print index_set({1}) ^ index_set({2})
{1,2}
>>> print index_set({1,2}) ^ index_set({2})
{1}
```

Definition at line 247 of file `PyClical.pyx`.

#### 6.18.2.17 `count()`

```
def PyClical.index_set.count (
    self )
```

Cardinality: Number of indices included in set.

```
>>> index_set({-1,1,2}).count()
3
```

Definition at line 313 of file `PyClical.pyx`.

References `PyClical.index_set.instance`.

#### 6.18.2.18 count\_neg()

```
def PyClical.index_set.count_neg (
    self )
```

Number of negative indices included in set.

```
>>> index_set({-1,1,2}).count_neg()
1
```

Definition at line 322 of file PyClical.pyx.

References `PyClical.index_set.instance`.

#### 6.18.2.19 count\_pos()

```
def PyClical.index_set.count_pos (
    self )
```

Number of positive indices included in set.

```
>>> index_set({-1,1,2}).count_pos()
2
```

Definition at line 331 of file PyClical.pyx.

References `PyClical.index_set.instance`.

#### 6.18.2.20 hash\_fn()

```
def PyClical.index_set.hash_fn (
    self )
```

Hash function.

Definition at line 358 of file PyClical.pyx.

References `PyClical.index_set.instance`.

#### 6.18.2.21 max()

```
def PyClical.index_set.max (
    self )
```

Maximum member.

```
>>> index_set({-1,1,2}).max()
2
```

Definition at line 349 of file PyClical.pyx.

References PyClical.index\_set.instance.

Referenced by PyClical.index\_set.\_\_iter\_\_().

#### 6.18.2.22 min()

```
def PyClical.index_set.min (
    self )
```

Minimum member.

```
>>> index_set({-1,1,2}).min()
-1
```

Definition at line 340 of file PyClical.pyx.

References PyClical.index\_set.instance.

Referenced by PyClical.index\_set.\_\_iter\_\_().

#### 6.18.2.23 sign\_of\_mult()

```
def PyClical.index_set.sign_of_mult (
    self,
    rhs )
```

Sign of geometric product of two Clifford basis elements.

```
>>> s = index_set({1,2}); t=index_set({-1}); s.sign_of_mult(t)
1
```

Definition at line 364 of file PyClical.pyx.

References PyClical.index\_set.instance.

## 6.18.2.24 sign\_of\_square()

```
def PyClical.index_set.sign_of_square (
    self )
```

Sign of geometric square of a Clifford basis element.

```
>>> s = index_set({1,2}); s.sign_of_square()
-1
```

Definition at line 373 of file PyClical.pyx.

References PyClical.index\_set.instance.

## 6.18.3 Member Data Documentation

## 6.18.3.1 instance

PyClical.index\_set.instance

Definition at line 94 of file PyClical.pyx.

Referenced by PyClical.clifford.\_\_call\_\_(), PyClical.index\_set.\_\_contains\_\_(), PyClical.index\_set.\_\_dealloc\_\_(), PyClical.clifford.\_\_dealloc\_\_(), PyClical.index\_set.\_\_getitem\_\_(), PyClical.clifford.\_\_getitem\_\_(), PyClical.index\_set.\_\_invert\_\_(), PyClical.clifford.\_\_neg\_\_(), PyClical.index\_set.\_\_setitem\_\_(), PyClical.clifford.conj(), PyClical.index\_set.count(), PyClical.index\_set.count\_neg(), PyClical.index\_set.count\_pos(), PyClical.clifford.even(), PyClical.clifford.frame(), PyClical.index\_set.hash\_fn(), PyClical.clifford.inv(), PyClical.clifford.involute(), PyClical.clifford.isnan(), PyClical.index\_set.max(), PyClical.clifford.max\_abs(), PyClical.index\_set.min(), PyClical.clifford.norm(), PyClical.clifford.odd(), PyClical.clifford.outer\_pow(), PyClical.clifford.pow(), PyClical.clifford.pure(), PyClical.clifford.quad(), PyClical.clifford.reverse(), PyClical.clifford.scalar(), PyClical.index\_set.sign\_of\_mult(), PyClical.index\_set.sign\_of\_square(), PyClical.clifford.truncated(), and PyClical.clifford.vector\_part().

The documentation for this class was generated from the following file:

- [pyclical/PyClical.pyx](#)

## 6.19 glucat::index\_set\_hash&lt; LO, HI &gt; Class Template Reference

```
#include <framed_multi.h>
```

## Public Types

- typedef [index\\_set](#)< LO, HI > [index\\_set\\_t](#)

## Public Member Functions

- `size_t operator() (index_set_t val) const`

### 6.19.1 Detailed Description

```
template<const index_t LO, const index_t HI>
class glucat::index_set_hash< LO, HI >
```

Definition at line 126 of file framed\_multi.h.

### 6.19.2 Member Typedef Documentation

#### 6.19.2.1 index\_set\_t

```
template<const index_t LO, const index_t HI>
typedef index_set<LO,HI> glucat::index_set_hash< LO, HI >::index_set_t
```

Definition at line 129 of file framed\_multi.h.

### 6.19.3 Member Function Documentation

#### 6.19.3.1 operator()()

```
template<const index_t LO, const index_t HI>
size_t glucat::index_set_hash< LO, HI >::operator() (
    index_set_t val ) const [inline]
```

Definition at line 130 of file framed\_multi.h.

References `glucat::index_set< LO, HI >::hash_fn()`.

The documentation for this class was generated from the following file:

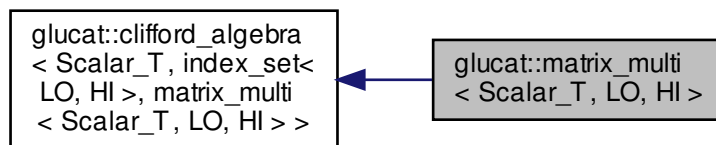
- `glucat/framed_multi.h`

## 6.20 glucat::matrix\_multi< Scalar\_T, LO, HI > Class Template Reference

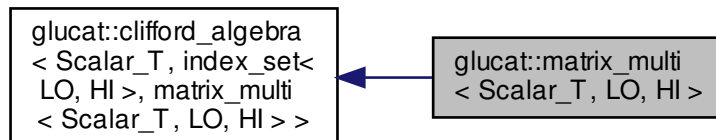
A matrix\_multi<Scalar\_T,LO,HI> is a matrix approximation to a multivector.

```
#include <framed_multi.h>
```

Inheritance diagram for glucat::matrix\_multi< Scalar\_T, LO, HI >:



Collaboration diagram for glucat::matrix\_multi< Scalar\_T, LO, HI >:



### Public Types

- typedef [matrix\\_multi](#) [multivector\\_t](#)
- typedef [multivector\\_t](#) [matrix\\_multi\\_t](#)
- typedef [Scalar\\_T](#) [scalar\\_t](#)
- typedef [index\\_set< LO, HI >](#) [index\\_set\\_t](#)
- typedef std::pair< const [index\\_set\\_t](#), [Scalar\\_T](#) > [term\\_t](#)
- typedef std::vector< [Scalar\\_T](#) > [vector\\_t](#)
- typedef [error< multivector\\_t >](#) [error\\_t](#)
- typedef [framed\\_multi< Scalar\\_T, LO, HI >](#) [framed\\_multi\\_t](#)

## Public Member Functions

- [~matrix\\_multi](#) ()  
*Destructor.*
- [matrix\\_multi](#) ()  
*Default constructor.*
- `template<typename Other_Scalar_T >`  
[matrix\\_multi](#) (const [matrix\\_multi](#)< Other\_Scalar\_T, LO, HI > &val)  
*Construct a multivector from a multivector with a different scalar type.*
- `template<typename Other_Scalar_T >`  
[matrix\\_multi](#) (const [matrix\\_multi](#)< Other\_Scalar\_T, LO, HI > &val, const [index\\_set\\_t](#) frm, const bool prechecked=false)  
*Construct a multivector, within a given frame, from a given multivector.*
- [matrix\\_multi](#) (const [multivector\\_t](#) &val, const [index\\_set\\_t](#) frm, const bool prechecked=false)  
*Construct a multivector, within a given frame, from a given multivector.*
- [matrix\\_multi](#) (const [index\\_set\\_t](#) ist, const Scalar\_T &crd=Scalar\_T(1))  
*Construct a multivector from an index set and a scalar coordinate.*
- [matrix\\_multi](#) (const [index\\_set\\_t](#) ist, const Scalar\_T &crd, const [index\\_set\\_t](#) frm, const bool prechecked=false)  
*Construct a multivector, within a given frame, from an index set and a scalar coordinate.*
- [matrix\\_multi](#) (const Scalar\_T &scr, const [index\\_set\\_t](#) frm=[index\\_set\\_t](#)())  
*Construct a multivector from a scalar (within a frame, if given)*
- [matrix\\_multi](#) (const int scr, const [index\\_set\\_t](#) frm=[index\\_set\\_t](#)())  
*Construct a multivector from an int (within a frame, if given)*
- [matrix\\_multi](#) (const [vector\\_t](#) &vec, const [index\\_set\\_t](#) frm, const bool prechecked=false)  
*Construct a multivector, within a given frame, from a given vector.*
- [matrix\\_multi](#) (const std::string &str)  
*Construct a multivector from a string: eg: "3+2{1,2}-6.1e-2{2,3}".*
- [matrix\\_multi](#) (const std::string &str, const [index\\_set\\_t](#) frm, const bool prechecked=false)  
*Construct a multivector, within a given frame, from a string: eg: "3+2{1,2}-6.1e-2{2,3}".*
- [matrix\\_multi](#) (const char \*str)  
*Construct a multivector from a char\*: eg: "3+2{1,2}-6.1e-2{2,3}".*
- [matrix\\_multi](#) (const char \*str, const [index\\_set\\_t](#) frm, const bool prechecked=false)  
*Construct a multivector, within a given frame, from a char\*: eg: "3+2{1,2}-6.1e-2{2,3}".*
- `template<typename Other_Scalar_T >`  
[matrix\\_multi](#) (const [framed\\_multi](#)< Other\_Scalar\_T, LO, HI > &val)  
*Construct a multivector from a framed\_multi\_t.*
- `template<typename Other_Scalar_T >`  
[matrix\\_multi](#) (const [framed\\_multi](#)< Other\_Scalar\_T, LO, HI > &val, const [index\\_set\\_t](#) frm, const bool prechecked=false)  
*Construct a multivector, within a given frame, from a framed\_multi\_t.*
- const [matrix\\_multi\\_t](#) [fast\\_matrix\\_multi](#) (const [index\\_set\\_t](#) frm) const  
*Use generalized FFT to construct a matrix\_multi\_t.*
- `template<typename Other_Scalar_T >`  
const [framed\\_multi](#)< Other\_Scalar\_T, LO, HI > [fast\\_framed\\_multi](#) () const  
*Use inverse generalized FFT to construct a framed\_multi\_t.*
- [\\_GLUCAT\\_CLIFFORD\\_ALGEBRA\\_OPERATIONS](#) [multivector\\_t](#) & [operator=](#) (const [multivector\\_t](#) &rhs)  
*Assignment operator.*
- [multivector\\_t](#) & [operator+=](#) (const [term\\_t](#) &rhs)  
*Add a term, if non-zero.*

## Static Public Member Functions

- static const std::string [classname](#) ()  
*Class name used in messages.*
- static const [matrix\\_multi\\_t](#) [random](#) (const [index\\_set\\_t](#) frm, Scalar\_T fill=Scalar\_T(1))  
*Random multivector within a frame.*

## Private Types

- typedef ublas::row\_major [orientation\\_t](#)
- typedef ublas::compressed\_matrix< int, [orientation\\_t](#) > [basis\\_matrix\\_t](#)
- typedef ublas::compressed\_matrix< Scalar\_T, [orientation\\_t](#) > [matrix\\_t](#)
- typedef matrix\_t::size\_type [matrix\\_index\\_t](#)

## Private Member Functions

- template<typename Matrix\_T >  
[matrix\\_multi](#) (const Matrix\_T &mtx, const [index\\_set\\_t](#) frm)  
*Construct a multivector within a given frame from a given matrix.*
- [matrix\\_multi](#) (const [matrix\\_t](#) &mtx, const [index\\_set\\_t](#) frm)  
*Construct a multivector within a given frame from a given matrix.*
- const [basis\\_matrix\\_t](#) [basis\\_element](#) (const [index\\_set](#)< LO, HI > &ist) const  
*Create a basis element matrix within the current frame.*

## Private Attributes

- [index\\_set\\_t](#) [m\\_frame](#)  
*Index set representing the frame for the subalgebra which contains the multivector.*
- [matrix\\_t](#) [m\\_matrix](#)  
*Matrix value representing the multivector within the folded frame.*

## Friends

- template<typename Other\_Scalar\_T , const index\_t Other\_LO, const index\_t Other\_HI>  
class [framed\\_multi](#)
- template<typename Other\_Scalar\_T , const index\_t Other\_LO, const index\_t Other\_HI>  
class [matrix\\_multi](#)
- const [matrix\\_multi\\_t](#) operator\* (const [matrix\\_multi\\_t](#) &lhs, const [matrix\\_multi\\_t](#) &rhs)
- const [matrix\\_multi\\_t](#) operator^ (const [matrix\\_multi\\_t](#) &lhs, const [matrix\\_multi\\_t](#) &rhs)
- const [matrix\\_multi\\_t](#) operator & (const [matrix\\_multi\\_t](#) &lhs, const [matrix\\_multi\\_t](#) &rhs)
- const [matrix\\_multi\\_t](#) operator% (const [matrix\\_multi\\_t](#) &lhs, const [matrix\\_multi\\_t](#) &rhs)
- Scalar\_T star (const [matrix\\_multi\\_t](#) &lhs, const [matrix\\_multi\\_t](#) &rhs)
- const [matrix\\_multi\\_t](#) operator/ (const [matrix\\_multi\\_t](#) &lhs, const [matrix\\_multi\\_t](#) &rhs)
- const [matrix\\_multi\\_t](#) operator| (const [matrix\\_multi\\_t](#) &lhs, const [matrix\\_multi\\_t](#) &rhs)
- std::istream & operator>> (std::istream &s, [multivector\\_t](#) &val)
- std::ostream & operator<< (std::ostream &os, const [multivector\\_t](#) &val)
- std::ostream & operator<< (std::ostream &os, const [term\\_t](#) &term)

- `template<typename Other_Scalar_T, const index_t Other_LO, const index_t Other_HI>`  
`const index\_set< Other_LO, Other_HI > reframe (const matrix\_multi< Other_Scalar_T, Other_LO, Other_HI`  
`> &lhs, const matrix\_multi< Other_Scalar_T, Other_LO, Other_HI > &rhs, matrix\_multi< Other_Scalar_↵`  
`T, Other_LO, Other_HI > &lhs_reframed, matrix\_multi< Other_Scalar_T, Other_LO, Other_HI > &rhs_↵`  
`reframed)`
- `template<typename Other_Scalar_T, const index_t Other_LO, const index_t Other_HI>`  
`const matrix\_multi< Other_Scalar_T, Other_LO, Other_HI > matrix\_sqrt (const matrix\_multi< Other_↵`  
`Scalar_T, Other_LO, Other_HI > &val, const matrix\_multi< Other_Scalar_T, Other_LO, Other_HI > &i)`
- `template<typename Other_Scalar_T, const index_t Other_LO, const index_t Other_HI>`  
`const matrix\_multi< Other_Scalar_T, Other_LO, Other_HI > matrix\_log (const matrix\_multi< Other_↵`  
`Scalar_T, Other_LO, Other_HI > &val, const matrix\_multi< Other_Scalar_T, Other_LO, Other_HI > &i)`

### 6.20.1 Detailed Description

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
class glucat::matrix_multi< Scalar_T, LO, HI >
```

A `matrix_multi<Scalar_T,LO,HI>` is a matrix approximation to a multivector.

Definition at line 68 of file `framed_multi.h`.

### 6.20.2 Member Typedef Documentation

#### 6.20.2.1 `basis_matrix_t`

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAU↵
LT_HI>
typedef ublas::compressed_matrix< int, orientation\_t > glucat::matrix\_multi< Scalar_T, LO, HI
>::basis_matrix_t [private]
```

Definition at line 152 of file `matrix_multi.h`.

#### 6.20.2.2 `error_t`

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAU↵
LT_HI>
typedef error<multivector\_t> glucat::matrix\_multi< Scalar_T, LO, HI >::error_t
```

Definition at line 142 of file `matrix_multi.h`.

### 6.20.2.3 framed\_multi\_t

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
typedef framed_multi<Scalar_T,LO,HI> glucat::matrix_multi< Scalar_T, LO, HI >::framed_multi_t
```

Definition at line 143 of file matrix\_multi.h.

### 6.20.2.4 index\_set\_t

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
typedef index_set<LO,HI> glucat::matrix_multi< Scalar_T, LO, HI >::index_set_t
```

Definition at line 139 of file matrix\_multi.h.

### 6.20.2.5 matrix\_index\_t

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
typedef matrix_t::size_type glucat::matrix_multi< Scalar_T, LO, HI >::matrix_index_t [private]
```

Definition at line 159 of file matrix\_multi.h.

### 6.20.2.6 matrix\_multi\_t

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
typedef multivector_t glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi_t
```

Definition at line 137 of file matrix\_multi.h.

### 6.20.2.7 matrix\_t

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
typedef ublas::compressed_matrix< Scalar_T, orientation_t > glucat::matrix_multi< Scalar_T,
LO, HI >::matrix_t [private]
```

Definition at line 157 of file matrix\_multi.h.

### 6.20.2.8 multivector\_t

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAU↵
LT_HI>
typedef matrix_multi glucat::matrix_multi< Scalar_T, LO, HI >::multivector_t
```

Definition at line 136 of file matrix\_multi.h.

### 6.20.2.9 orientation\_t

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAU↵
LT_HI>
typedef ublas::row_major glucat::matrix_multi< Scalar_T, LO, HI >::orientation_t [private]
```

Definition at line 150 of file matrix\_multi.h.

### 6.20.2.10 scalar\_t

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAU↵
LT_HI>
typedef Scalar_T glucat::matrix_multi< Scalar_T, LO, HI >::scalar_t
```

Definition at line 138 of file matrix\_multi.h.

### 6.20.2.11 term\_t

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAU↵
LT_HI>
typedef std::pair<const index_set_t, Scalar_T> glucat::matrix_multi< Scalar_T, LO, HI >↵
::term_t
```

Definition at line 140 of file matrix\_multi.h.

### 6.20.2.12 vector\_t

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAU↵
LT_HI>
typedef std::vector<Scalar_T> glucat::matrix_multi< Scalar_T, LO, HI >::vector_t
```

Definition at line 141 of file matrix\_multi.h.

### 6.20.3 Constructor & Destructor Documentation

#### 6.20.3.1 ~matrix\_multi()

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
glucat::matrix_multi< Scalar_T, LO, HI >::~~matrix_multi ( ) [inline]
```

Destructor.

Definition at line 165 of file matrix\_multi.h.

#### 6.20.3.2 matrix\_multi() [1/17]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi ( )
```

Default constructor.

Definition at line 97 of file matrix\_multi\_imp.h.

References glucat::matrix\_multi< Scalar\_T, LO, HI >::m\_matrix.

Referenced by glucat::matrix\_multi< Scalar\_T, LO, HI >::matrix\_multi().

#### 6.20.3.3 matrix\_multi() [2/17]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
template<typename Other_Scalar_T >
glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi (
    const matrix_multi< Other_Scalar_T, LO, HI > & val )
```

Construct a multivector from a multivector with a different scalar type.

Definition at line 106 of file matrix\_multi\_imp.h.

References glucat::matrix\_multi< Scalar\_T, LO, HI >::m\_matrix.

#### 6.20.3.4 `matrix_multi()` [3/17]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
template<typename Other_Scalar_T >
glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi (
    const matrix_multi< Other_Scalar_T, LO, HI > & val,
    const index_set_t frm,
    const bool prechecked = false )
```

Construct a multivector, within a given frame, from a given multivector.

Definition at line 128 of file `matrix_multi_imp.h`.

References `glucat::matrix_multi< Scalar_T, LO, HI >::m_frame`, and `glucat::matrix_multi< Scalar_T, LO, HI >::m_matrix`.

#### 6.20.3.5 `matrix_multi()` [4/17]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi (
    const multivector_t & val,
    const index_set_t frm,
    const bool prechecked = false )
```

Construct a multivector, within a given frame, from a given multivector.

Definition at line 156 of file `matrix_multi_imp.h`.

References `glucat::matrix_multi< Scalar_T, LO, HI >::m_frame`, and `glucat::matrix_multi< Scalar_T, LO, HI >::m_matrix`.

#### 6.20.3.6 `matrix_multi()` [5/17]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi (
    const index_set_t ist,
    const Scalar_T & crd = Scalar_T(1) )
```

Construct a multivector from an index set and a scalar coordinate.

Definition at line 168 of file `matrix_multi_imp.h`.

References `glucat::matrix_multi< Scalar_T, LO, HI >::m_frame`, and `glucat::matrix_multi< Scalar_T, LO, HI >::m_matrix`.

**6.20.3.7 matrix\_multi()** [6/17]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi (
    const index_set_t ist,
    const Scalar_T & crd,
    const index_set_t frm,
    const bool prechecked = false )
```

Construct a multivector, within a given frame, from an index set and a scalar coordinate.

Definition at line 180 of file matrix\_multi\_imp.h.

References PyClical::ist, and glucat::matrix\_multi< Scalar\_T, LO, HI >::m\_matrix.

**6.20.3.8 matrix\_multi()** [7/17]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi (
    const Scalar_T & scr,
    const index_set_t frm = index_set_t() )
```

Construct a multivector from a scalar (within a frame, if given)

Definition at line 194 of file matrix\_multi\_imp.h.

References glucat::matrix\_multi< Scalar\_T, LO, HI >::m\_matrix.

**6.20.3.9 matrix\_multi()** [8/17]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi (
    const int scr,
    const index_set_t frm = index_set_t() )
```

Construct a multivector from an int (within a frame, if given)

Definition at line 206 of file matrix\_multi\_imp.h.

**6.20.3.10 matrix\_multi()** [9/17]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi (
    const vector_t & vec,
    const index_set_t frm,
    const bool prechecked = false )
```

Construct a multivector, within a given frame, from a given vector.

Definition at line 212 of file matrix\_multi\_imp.h.

References glucat::index\_set< LO, HI >::count(), glucat::matrix\_multi< Scalar\_T, LO, HI >::m\_matrix, glucat::index\_set< LO, HI >::max(), and glucat::index\_set< LO, HI >::min().

**6.20.3.11** `matrix_multi()` [10/17]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi (
    const std::string & str )
```

Construct a multivector from a string: eg: "3+2{1,2}-6.1e-2{2,3}".

Definition at line 239 of file `matrix_multi_imp.h`.

**6.20.3.12** `matrix_multi()` [11/17]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi (
    const std::string & str,
    const index_set_t frm,
    const bool prechecked = false )
```

Construct a multivector, within a given frame, from a string: eg: "3+2{1,2}-6.1e-2{2,3}".

Definition at line 245 of file `matrix_multi_imp.h`.

**6.20.3.13** `matrix_multi()` [12/17]

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi (
    const char * str ) [inline]
```

Construct a multivector from a char\*: eg: "3+2{1,2}-6.1e-2{2,3}".

Definition at line 196 of file `matrix_multi.h`.

References `glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi()`.

**6.20.3.14** `matrix_multi()` [13/17]

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi (
    const char * str,
    const index_set_t frm,
    const bool prechecked = false ) [inline]
```

Construct a multivector, within a given frame, from a char\*: eg: "3+2{1,2}-6.1e-2{2,3}".

Definition at line 199 of file `matrix_multi.h`.

References `glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi()`.

## 6.20.3.15 matrix\_multi() [14/17]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
template<typename Other_Scalar_T >
glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi (
    const framed_multi< Other_Scalar_T, LO, HI > & val )
```

Construct a multivector from a framed\_multi\_t.

Definition at line 252 of file matrix\_multi\_imp.h.

References PyClical::e(), glucat::tuning< Mult\_Matrix\_Threshold, Div\_Max\_Steps, Sqrt\_Max\_Steps, Log\_Max\_Outer\_Steps, Log\_Max\_Inner\_Steps, Basis\_Max\_Count, Fast\_Size\_Threshold, Inv\_Fast\_Dim\_Threshold, Products\_Size\_Threshold, Function\_Precision >::fast\_size\_threshold, glucat::matrix\_multi< Scalar\_T, LO, HI >::m\_frame, and glucat::matrix\_multi< Scalar\_T, LO, HI >::m\_matrix.

## 6.20.3.16 matrix\_multi() [15/17]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
template<typename Other_Scalar_T >
glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi (
    const framed_multi< Other_Scalar_T, LO, HI > & val,
    const index_set_t frm,
    const bool prechecked = false )
```

Construct a multivector, within a given frame, from a framed\_multi\_t.

Definition at line 279 of file matrix\_multi\_imp.h.

References PyClical::e(), glucat::tuning< Mult\_Matrix\_Threshold, Div\_Max\_Steps, Sqrt\_Max\_Steps, Log\_Max\_Outer\_Steps, Log\_Max\_Inner\_Steps, Basis\_Max\_Count, Fast\_Size\_Threshold, Inv\_Fast\_Dim\_Threshold, Products\_Size\_Threshold, Function\_Precision >::fast\_size\_threshold, and glucat::clifford\_algebra< Scalar\_T, index\_set< LO, HI >, framed\_multi< Scalar\_T, LO, HI > >::frame().

## 6.20.3.17 matrix\_multi() [16/17]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
template<typename Matrix_T >
glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi (
    const Matrix_T & mtx,
    const index_set_t frm ) [private]
```

Construct a multivector within a given frame from a given matrix.

Definition at line 307 of file matrix\_multi\_imp.h.

References glucat::matrix\_multi< Scalar\_T, LO, HI >::m\_matrix.

**6.20.3.18 matrix\_multi()** [17/17]

```
template<typename Scalar_T , const index_t LO, const index_t HI>
glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi (
    const matrix_t & mtx,
    const index_set_t frm ) [private]
```

Construct a multivector within a given frame from a given matrix.

Definition at line 328 of file matrix\_multi\_imp.h.

**6.20.4 Member Function Documentation****6.20.4.1 basis\_element()**

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const matrix_multi< Scalar_T, LO, HI >::basis_matrix_t glucat::matrix_multi< Scalar_T, LO, HI
>::basis_element (
    const index_set< LO, HI > & ist ) const [private]
```

Create a basis element matrix within the current frame.

Definition at line 1243 of file matrix\_multi\_imp.h.

References glucat::tuning< Mult\_Matrix\_Threshold, Div\_Max\_Steps, Sqrt\_Max\_Steps, Log\_Max\_Outer\_Steps, Log\_Max\_Inner\_Steps, Basis\_Max\_Count, Fast\_Size\_Threshold, Inv\_Fast\_Dim\_Threshold, Products\_Size\_Threshold, Function\_Precision >::basis\_max\_count, PyClical::e(), glucat::index\_set< LO, HI >::fold(), glucat::gen::generator\_table< Matrix\_T >::generator(), PyClical::ist, glucat::index\_set< LO, HI >::max(), glucat::index\_set< LO, HI >::min(), glucat::matrix::mono\_prod(), and glucat::offset\_level().

Referenced by glucat::framed\_multi< Scalar\_T, LO, HI >::framed\_multi().

**6.20.4.2 classname()**

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const std::string glucat::matrix_multi< Scalar_T, LO, HI >::classname ( ) [static]
```

Class name used in messages.

Definition at line 69 of file matrix\_multi\_imp.h.

## 6.20.4.3 fast\_framed\_multi()

```
template<typename Scalar_T , const index_t LO, const index_t HI>
template<typename Other_Scalar_T >
const framed_multi< Other_Scalar_T, LO, HI > glucat::matrix_multi< Scalar_T, LO, HI >::fast↵
_framed_multi ( ) const
```

Use inverse generalized FFT to construct a framed\_multi\_t.

Definition at line 1166 of file matrix\_multi\_imp.h.

References glucat::framed\_multi< Scalar\_T, LO, HI >::centre\_pm4\_qp4(), glucat::framed\_multi< Scalar\_T, LO, HI >::centre\_pp4\_qm4(), glucat::framed\_multi< Scalar\_T, LO, HI >::centre\_qp1\_pm1(), glucat::gen::offset\_to\_↵super, glucat::pos\_mod(), and glucat::framed\_multi< Scalar\_T, LO, HI >::unfold().

## 6.20.4.4 fast\_matrix\_multi()

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const matrix_multi< Scalar_T, LO, HI > glucat::matrix_multi< Scalar_T, LO, HI >::fast_↵
matrix_multi (
    const index_set_t frm ) const [inline]
```

Use generalized FFT to construct a matrix\_multi\_t.

Definition at line 1153 of file matrix\_multi\_imp.h.

## 6.20.4.5 operator+=( )

```
template<typename Scalar_T , const index_t LO, const index_t HI>
matrix_multi< Scalar_T, LO, HI > & glucat::matrix_multi< Scalar_T, LO, HI >::operator+= (
    const term_t & rhs ) [inline]
```

Add a term, if non-zero.

Geometric sum.

Geometric sum of multivector and scalar.

Definition at line 470 of file matrix\_multi\_imp.h.

## 6.20.4.6 operator=( )

```
template<typename Scalar_T , const index_t LO, const index_t HI>
matrix_multi< Scalar_T, LO, HI > & glucat::matrix_multi< Scalar_T, LO, HI >::operator= (
    const multivector_t & rhs )
```

Assignment operator.

Definition at line 336 of file matrix\_multi\_imp.h.

References glucat::matrix\_multi< Scalar\_T, LO, HI >::m\_frame, and glucat::matrix\_multi< Scalar\_T, LO, HI >↵::m\_matrix.

#### 6.20.4.7 random()

```
template<typename Scalar_T , const index_t LO, const index_t HI>
const matrix_multi< Scalar_T, LO, HI > glucat::matrix_multi< Scalar_T, LO, HI >::random (
    const index_set_t frm,
    Scalar_T fill = Scalar_T(1) ) [static]
```

Random multivector within a frame.

Definition at line 996 of file matrix\_multi\_imp.h.

References PyClical::fill, and glucat::framed\_multi< Scalar\_T, LO, HI >::random().

### 6.20.5 Friends And Related Function Documentation

#### 6.20.5.1 framed\_multi

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
template<typename Other_Scalar_T , const index_t Other_LO, const index_t Other_HI>
friend class framed_multi [friend]
```

Definition at line 145 of file matrix\_multi.h.

#### 6.20.5.2 matrix\_log

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
template<typename Other_Scalar_T , const index_t Other_LO, const index_t Other_HI>
const matrix_multi<Other_Scalar_T,Other_LO,Other_HI> matrix_log (
    const matrix_multi< Other_Scalar_T, Other_LO, Other_HI > & val,
    const matrix_multi< Other_Scalar_T, Other_LO, Other_HI > & i ) [friend]
```

#### 6.20.5.3 matrix\_multi

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
template<typename Other_Scalar_T , const index_t Other_LO, const index_t Other_HI>
friend class matrix_multi [friend]
```

Definition at line 147 of file matrix\_multi.h.

## 6.20.5.4 matrix\_sqrt

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
template<typename Other_Scalar_T , const index_t Other_LO, const index_t Other_HI>
const matrix_multi<Other_Scalar_T,Other_LO,Other_HI> matrix_sqrt (
    const matrix_multi< Other_Scalar_T, Other_LO, Other_HI > & val,
    const matrix_multi< Other_Scalar_T, Other_LO, Other_HI > & i ) [friend]
```

## 6.20.5.5 operator &amp;

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
const matrix_multi_t operator& (
    const matrix_multi_t & lhs,
    const matrix_multi_t & rhs ) [friend]
```

## 6.20.5.6 operator%

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
const matrix_multi_t operator% (
    const matrix_multi_t & lhs,
    const matrix_multi_t & rhs ) [friend]
```

## 6.20.5.7 operator\*

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
const matrix_multi_t operator* (
    const matrix_multi_t & lhs,
    const matrix_multi_t & rhs ) [friend]
```

## 6.20.5.8 operator/

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
const matrix_multi_t operator/ (
    const matrix_multi_t & lhs,
    const matrix_multi_t & rhs ) [friend]
```

**6.20.5.9 operator<< [1/2]**

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
std::ostream& operator<< (
    std::ostream & os,
    const multivector_t & val ) [friend]
```

**6.20.5.10 operator<< [2/2]**

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
std::ostream& operator<< (
    std::ostream & os,
    const term_t & term ) [friend]
```

**6.20.5.11 operator>>**

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
std::istream& operator>> (
    std::istream & s,
    multivector_t & val ) [friend]
```

**6.20.5.12 operator^**

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
const matrix_multi_t operator^ (
    const matrix_multi_t & lhs,
    const matrix_multi_t & rhs ) [friend]
```

**6.20.5.13 operator" |**

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
const matrix_multi_t operator| (
    const matrix_multi_t & lhs,
    const matrix_multi_t & rhs ) [friend]
```

6.20.5.14 `reframe`

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
template<typename Other_Scalar_T , const index_t Other_LO, const index_t Other_HI>
const index_set<Other_LO,Other_HI> reframe (
    const matrix_multi< Other_Scalar_T, Other_LO, Other_HI > & lhs,
    const matrix_multi< Other_Scalar_T, Other_LO, Other_HI > & rhs,
    matrix_multi< Other_Scalar_T, Other_LO, Other_HI > & lhs_reframed,
    matrix_multi< Other_Scalar_T, Other_LO, Other_HI > & rhs_reframed ) [friend]
```

6.20.5.15 `star`

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
Scalar_T star (
    const matrix_multi_t & lhs,
    const matrix_multi_t & rhs ) [friend]
```

## 6.20.6 Member Data Documentation

6.20.6.1 `m_frame`

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
index_set_t glucat::matrix_multi< Scalar_T, LO, HI >::m_frame [private]
```

Index set representing the frame for the subalgebra which contains the multivector.

Definition at line 275 of file `matrix_multi.h`.

Referenced by `glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi()`, `glucat::operator*()`, `glucat::operator/()`, `glucat::matrix_multi< Scalar_T, LO, HI >::operator=()`, and `glucat::reframe()`.

6.20.6.2 `m_matrix`

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
matrix_t glucat::matrix_multi< Scalar_T, LO, HI >::m_matrix [private]
```

Matrix value representing the multivector within the folded frame.

Definition at line 277 of file `matrix_multi.h`.

Referenced by `glucat::framed_multi< Scalar_T, LO, HI >::framed_multi()`, `glucat::matrix_multi< Scalar_T, LO, HI >::matrix_multi()`, `glucat::operator*()`, and `glucat::matrix_multi< Scalar_T, LO, HI >::operator=()`.

The documentation for this class was generated from the following files:

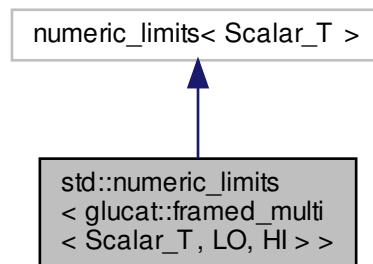
- `glucat/framed_multi.h`
- `glucat/matrix_multi.h`
- `glucat/matrix_multi_imp.h`

## 6.21 `std::numeric_limits< glucat::framed_multi< Scalar_T, LO, HI > >` Struct Template Reference

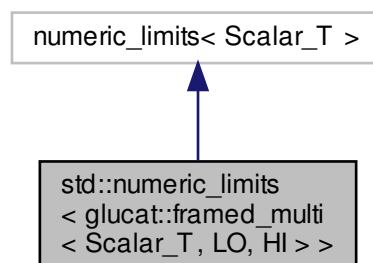
Numeric limits for `framed_multi` inherit limits for the corresponding scalar type.

```
#include <framed_multi.h>
```

Inheritance diagram for `std::numeric_limits< glucat::framed_multi< Scalar_T, LO, HI > >`:



Collaboration diagram for `std::numeric_limits< glucat::framed_multi< Scalar_T, LO, HI > >`:



### 6.21.1 Detailed Description

```
template<typename Scalar_T, const glucat::index_t LO, const glucat::index_t HI>
struct std::numeric_limits< glucat::framed_multi< Scalar_T, LO, HI > >
```

Numeric limits for `framed_multi` inherit limits for the corresponding scalar type.

Definition at line 374 of file `framed_multi.h`.

The documentation for this struct was generated from the following file:

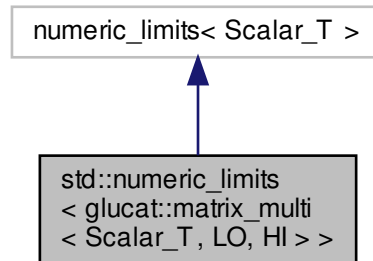
- [glucat/framed\\_multi.h](#)

## 6.22 std::numeric\_limits< glucat::matrix\_multi< Scalar\_T, LO, HI > > Struct Template Reference

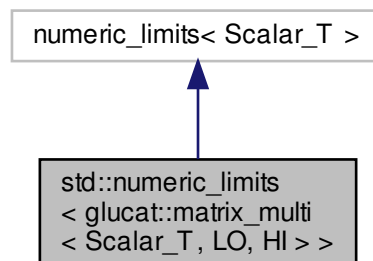
Numeric limits for matrix\_multi inherit limits for the corresponding scalar type.

```
#include <matrix_multi.h>
```

Inheritance diagram for std::numeric\_limits< glucat::matrix\_multi< Scalar\_T, LO, HI > >:



Collaboration diagram for std::numeric\_limits< glucat::matrix\_multi< Scalar\_T, LO, HI > >:



### 6.22.1 Detailed Description

```
template<typename Scalar_T, const glucat::index_t LO, const glucat::index_t HI>
struct std::numeric_limits< glucat::matrix_multi< Scalar_T, LO, HI > >
```

Numeric limits for matrix\_multi inherit limits for the corresponding scalar type.

Definition at line 293 of file matrix\_multi.h.

The documentation for this struct was generated from the following file:

- glucat/[matrix\\_multi.h](#)

## 6.23 glucat::numeric\_traits< Scalar\_T > Class Template Reference

Extra traits which extend numeric limits.

```
#include <scalar.h>
```

### Classes

- struct [demoted](#)  
*Demoted type for long double.*
- struct [promoted](#)  
*Promoted type.*

### Public Member Functions

- `template<>`  
`long double pi ()`  
*Pi for long double.*
- `template<>`  
`long double ln\_2 ()`  
*log(2) for long double*
- `template<>`  
`float to\_scalar\_t (const Other_Scalar_T &val)`  
*Extra traits which extend numeric limits.*
- `template<>`  
`double to\_scalar\_t (const Other_Scalar_T &val)`  
*Cast to double.*
- `template<>`  
`long double to\_scalar\_t (const dd_real &val)`  
*Cast to long double.*
- `template<>`  
`long double to\_scalar\_t (const qd_real &val)`  
*Cast to long double.*
- `template<>`  
`dd_real to\_scalar\_t (const long double &val)`  
*Cast to dd\_real.*
- `template<>`  
`dd_real to\_scalar\_t (const qd_real &val)`  
*Cast to dd\_real.*
- `template<>`  
`qd_real to\_scalar\_t (const long double &val)`  
*Cast to qd\_real.*
- `template<>`  
`qd_real to\_scalar\_t (const dd_real &val)`  
*Cast to qd\_real.*

## Static Public Member Functions

- static bool [isInf](#) (const Scalar\_T &val)  
*Smart isinf.*
- static bool [isNaN](#) (const Scalar\_T &val)  
*Smart isnan.*
- static bool [isNaN\\_or\\_isInf](#) (const Scalar\_T &val)  
*Smart isnan or isinf.*
- static Scalar\_T [NaN](#) ()  
*Smart NaN.*
- static int [to\\_int](#) (const Scalar\_T &val)  
*Cast to int.*
- static double [to\\_double](#) (const Scalar\_T &val)  
*Cast to double.*
- template<typename Other\_Scalar\_T >  
static Scalar\_T [to\\_scalar\\_t](#) (const Other\_Scalar\_T &val)  
*Cast to Scalar\_T.*
- static Scalar\_T [fmod](#) (const Scalar\_T &lhs, const Scalar\_T &rhs)  
*Modulo function for scalar.*
- static Scalar\_T [conj](#) (const Scalar\_T &val)  
*Complex conjugate of scalar.*
- static Scalar\_T [real](#) (const Scalar\_T &val)  
*Real part of scalar.*
- static Scalar\_T [imag](#) (const Scalar\_T &val)  
*Imaginary part of scalar.*
- static Scalar\_T [abs](#) (const Scalar\_T &val)  
*Absolute value of scalar.*
- static Scalar\_T [pi](#) ()  
*Pi.*
- static Scalar\_T [ln\\_2](#) ()  
*log(2)*
- static Scalar\_T [pow](#) (const Scalar\_T &val, int n)  
*Integer power.*
- static Scalar\_T [sqrt](#) (const Scalar\_T &val)  
*Square root of scalar.*
- static Scalar\_T [exp](#) (const Scalar\_T &val)  
*Exponential.*
- static Scalar\_T [log](#) (const Scalar\_T &val)  
*Logarithm of scalar.*
- static Scalar\_T [log2](#) (const Scalar\_T &val)  
*Log base 2.*
- static Scalar\_T [cos](#) (const Scalar\_T &val)  
*Cosine of scalar.*
- static Scalar\_T [acos](#) (const Scalar\_T &val)  
*Inverse cosine of scalar.*
- static Scalar\_T [cosh](#) (const Scalar\_T &val)  
*Hyperbolic cosine of scalar.*
- static Scalar\_T [sin](#) (const Scalar\_T &val)  
*Sine of scalar.*
- static Scalar\_T [asin](#) (const Scalar\_T &val)  
*Inverse sine of scalar.*

- static Scalar\_T [sinh](#) (const Scalar\_T &val)  
*Hyperbolic sine of scalar.*
- static Scalar\_T [tan](#) (const Scalar\_T &val)  
*Tangent of scalar.*
- static Scalar\_T [atan](#) (const Scalar\_T &val)  
*Inverse tangent of scalar.*
- static Scalar\_T [tanh](#) (const Scalar\_T &val)  
*Hyperbolic tangent of scalar.*

### Static Private Member Functions

- static bool [isInf](#) (const Scalar\_T &val, [bool\\_to\\_type](#)< false >)  
*Smart isinf specialised for Scalar\_T without infinity.*
- static bool [isInf](#) (const Scalar\_T &val, [bool\\_to\\_type](#)< true >)  
*Smart isinf specialised for Scalar\_T with infinity.*
- static bool [isNaN](#) (const Scalar\_T &val, [bool\\_to\\_type](#)< false >)  
*Smart isnan specialised for Scalar\_T without quiet NaN.*
- static bool [isNaN](#) (const Scalar\_T &val, [bool\\_to\\_type](#)< true >)  
*Smart isnan specialised for Scalar\_T with quiet NaN.*

### 6.23.1 Detailed Description

```
template<typename Scalar_T>
class glucat::numeric_traits< Scalar_T >
```

Extra traits which extend numeric limits.

Definition at line 46 of file scalar.h.

### 6.23.2 Member Function Documentation

#### 6.23.2.1 [abs\(\)](#)

```
template<typename Scalar_T >
static Scalar_T glucat::numeric\_traits< Scalar_T >::abs (
    const Scalar_T & val ) [inline], [static]
```

Absolute value of scalar.

Definition at line 181 of file scalar.h.

References [UBLAS\\_ABS](#).

#### 6.23.2.2 acos()

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::acos (
    const Scalar_T & val ) [inline], [static]
```

Inverse cosine of scalar.

Definition at line 244 of file scalar.h.

References glucat::acos().

#### 6.23.2.3 asin()

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::asin (
    const Scalar_T & val ) [inline], [static]
```

Inverse sine of scalar.

Definition at line 265 of file scalar.h.

References glucat::asin().

#### 6.23.2.4 atan()

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::atan (
    const Scalar_T & val ) [inline], [static]
```

Inverse tangent of scalar.

Definition at line 286 of file scalar.h.

References glucat::atan().

#### 6.23.2.5 conj()

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::conj (
    const Scalar_T & val ) [inline], [static]
```

Complex conjugate of scalar.

Definition at line 160 of file scalar.h.

#### 6.23.2.6 cos()

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::cos (
    const Scalar_T & val ) [inline], [static]
```

Cosine of scalar.

Definition at line 237 of file scalar.h.

References glucat::cos().

#### 6.23.2.7 cosh()

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::cosh (
    const Scalar_T & val ) [inline], [static]
```

Hyperbolic cosine of scalar.

Definition at line 251 of file scalar.h.

References glucat::cosh().

#### 6.23.2.8 exp()

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::exp (
    const Scalar_T & val ) [inline], [static]
```

Exponential.

Definition at line 216 of file scalar.h.

References glucat::exp().

#### 6.23.2.9 fmod()

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::fmod (
    const Scalar_T & lhs,
    const Scalar_T & rhs ) [inline], [static]
```

Modulo function for scalar.

Definition at line 153 of file scalar.h.

**6.23.2.10** `imag()`

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::imag (
    const Scalar_T & val ) [inline], [static]
```

Imaginary part of scalar.

Definition at line 174 of file scalar.h.

**6.23.2.11** `isInf()` [1/3]

```
template<typename Scalar_T >
static bool glucat::numeric_traits< Scalar_T >::isInf (
    const Scalar_T & val,
    bool_to_type< false > ) [inline], [static], [private]
```

Smart isinf specialised for Scalar\_T without infinity.

Definition at line 53 of file scalar.h.

Referenced by `glucat::numeric_traits< Scalar_T >::isInf()`, and `glucat::numeric_traits< Scalar_T >::isNaN_or_isInf()`.

**6.23.2.12** `isInf()` [2/3]

```
template<typename Scalar_T >
static bool glucat::numeric_traits< Scalar_T >::isInf (
    const Scalar_T & val,
    bool_to_type< true > ) [inline], [static], [private]
```

Smart isinf specialised for Scalar\_T with infinity.

Definition at line 60 of file scalar.h.

References `_GLUCAT_ISINF`.

**6.23.2.13** `isInf()` [3/3]

```
template<typename Scalar_T >
static bool glucat::numeric_traits< Scalar_T >::isInf (
    const Scalar_T & val ) [inline], [static]
```

Smart isinf.

Definition at line 82 of file scalar.h.

References `glucat::numeric_traits< Scalar_T >::isInf()`.

**6.23.2.14 isNaN()** [1/3]

```
template<typename Scalar_T >
static bool glucat::numeric_traits< Scalar_T >::isNaN (
    const Scalar_T & val,
    bool_to_type< false > ) [inline], [static], [private]
```

Smart isnan specialised for Scalar\_T without quiet NaN.

Definition at line 67 of file scalar.h.

Referenced by glucat::numeric\_traits< Scalar\_T >::isNaN(), and glucat::numeric\_traits< Scalar\_T >::isNaN\_or\_isInf().

**6.23.2.15 isNaN()** [2/3]

```
template<typename Scalar_T >
static bool glucat::numeric_traits< Scalar_T >::isNaN (
    const Scalar_T & val,
    bool_to_type< true > ) [inline], [static], [private]
```

Smart isnan specialised for Scalar\_T with quiet NaN.

Definition at line 74 of file scalar.h.

References \_GLUCAT\_ISNAN.

**6.23.2.16 isNaN()** [3/3]

```
template<typename Scalar_T >
static bool glucat::numeric_traits< Scalar_T >::isNaN (
    const Scalar_T & val ) [inline], [static]
```

Smart isnan.

Definition at line 92 of file scalar.h.

References glucat::numeric\_traits< Scalar\_T >::isNaN().

**6.23.2.17 isNaN\_or\_isInf()**

```
template<typename Scalar_T >
static bool glucat::numeric_traits< Scalar_T >::isNaN_or_isInf (
    const Scalar_T & val ) [inline], [static]
```

Smart isnan or isinf.

Definition at line 102 of file scalar.h.

References glucat::numeric\_traits< Scalar\_T >::isInf(), and glucat::numeric\_traits< Scalar\_T >::isNaN().

**6.23.2.18** `ln_2()` [1/2]

```
template<>
long double glucat::numeric_traits< long double >::ln_2 ( ) [inline]
```

`log(2)` for long double

Definition at line 83 of file `long_double.h`.

References `glucat::l_ln2`.

**6.23.2.19** `ln_2()` [2/2]

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::ln_2 ( ) [inline], [static]
```

`log(2)`

Definition at line 195 of file `scalar.h`.

Referenced by `glucat::numeric_traits< Scalar_T >::log2()`.

**6.23.2.20** `log()`

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::log (
    const Scalar_T & val ) [inline], [static]
```

Logarithm of scalar.

Definition at line 223 of file `scalar.h`.

References `glucat::log()`.

Referenced by `glucat::numeric_traits< Scalar_T >::log2()`.

**6.23.2.21** `log2()`

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::log2 (
    const Scalar_T & val ) [inline], [static]
```

Log base 2.

Definition at line 230 of file `scalar.h`.

References `glucat::numeric_traits< Scalar_T >::ln_2()`, and `glucat::numeric_traits< Scalar_T >::log()`.

Referenced by `glucat::log2()`.

#### 6.23.2.22 NaN()

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::NaN ( ) [inline], [static]
```

Smart NaN.

Definition at line 114 of file scalar.h.

References glucat::log().

Referenced by glucat::matrix::trace().

#### 6.23.2.23 pi() [1/2]

```
template<>
long double glucat::numeric_traits< long double >::pi ( ) [inline]
```

Pi for long double.

Definition at line 75 of file long\_double.h.

References glucat::l\_pi.

#### 6.23.2.24 pi() [2/2]

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::pi ( ) [inline], [static]
```

Pi.

Definition at line 188 of file scalar.h.

Referenced by glucat::matrix::classify\_eigenvalues().

#### 6.23.2.25 pow()

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::pow (
    const Scalar_T & val,
    int n ) [inline], [static]
```

Integer power.

Definition at line 202 of file scalar.h.

References glucat::pow().

#### 6.23.2.26 real()

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::real (
    const Scalar_T & val ) [inline], [static]
```

Real part of scalar.

Definition at line 167 of file scalar.h.

#### 6.23.2.27 sin()

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::sin (
    const Scalar_T & val ) [inline], [static]
```

Sine of scalar.

Definition at line 258 of file scalar.h.

References glucat::sin().

#### 6.23.2.28 sinh()

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::sinh (
    const Scalar_T & val ) [inline], [static]
```

Hyperbolic sine of scalar.

Definition at line 272 of file scalar.h.

References glucat::sinh().

#### 6.23.2.29 sqrt()

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::sqrt (
    const Scalar_T & val ) [inline], [static]
```

Square root of scalar.

Definition at line 209 of file scalar.h.

References UBLAS\_SQRT.

Referenced by glucat::abs().

#### 6.23.2.30 tan()

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::tan (
    const Scalar_T & val ) [inline], [static]
```

Tangent of scalar.

Definition at line 279 of file scalar.h.

References glucat::tan().

#### 6.23.2.31 tanh()

```
template<typename Scalar_T >
static Scalar_T glucat::numeric_traits< Scalar_T >::tanh (
    const Scalar_T & val ) [inline], [static]
```

Hyperbolic tangent of scalar.

Definition at line 293 of file scalar.h.

References glucat::tanh().

#### 6.23.2.32 to\_double()

```
template<typename Scalar_T >
static double glucat::numeric_traits< Scalar_T >::to_double (
    const Scalar_T & val ) [inline], [static]
```

Cast to double.

Definition at line 132 of file scalar.h.

Referenced by glucat::operator<<(), and glucat::numeric\_traits< Scalar\_T >::to\_scalar\_t().

#### 6.23.2.33 to\_int()

```
template<typename Scalar_T >
static int glucat::numeric_traits< Scalar_T >::to_int (
    const Scalar_T & val ) [inline], [static]
```

Cast to int.

Definition at line 125 of file scalar.h.

**6.23.2.34 to\_scalar\_t()** [1/9]

```
template<>
float glucat::numeric_traits< float >::to_scalar_t (
    const Other_Scalar_T & val ) [inline]
```

Extra traits which extend numeric limits.

Cast to float

Definition at line 52 of file scalar\_imp.h.

References glucat::numeric\_traits< Scalar\_T >::to\_double().

**6.23.2.35 to\_scalar\_t()** [2/9]

```
template<>
double glucat::numeric_traits< double >::to_scalar_t (
    const Other_Scalar_T & val ) [inline]
```

Cast to double.

Definition at line 61 of file scalar\_imp.h.

References glucat::numeric\_traits< Scalar\_T >::to\_double().

**6.23.2.36 to\_scalar\_t()** [3/9]

```
template<>
long double glucat::numeric_traits< long double >::to_scalar_t (
    const dd_real & val ) [inline]
```

Cast to long double.

Definition at line 71 of file scalar\_imp.h.

**6.23.2.37 to\_scalar\_t()** [4/9]

```
template<>
long double glucat::numeric_traits< long double >::to_scalar_t (
    const qd_real & val ) [inline]
```

Cast to long double.

Definition at line 80 of file scalar\_imp.h.

**6.23.2.38 to\_scalar\_t()** [ 5/9]

```
template<>
dd_real glucat::numeric_traits< dd_real >::to_scalar_t (
    const long double & val ) [inline]
```

Cast to dd\_real.

Definition at line 89 of file scalar\_imp.h.

**6.23.2.39 to\_scalar\_t()** [ 6/9]

```
template<>
dd_real glucat::numeric_traits< dd_real >::to_scalar_t (
    const qd_real & val ) [inline]
```

Cast to dd\_real.

Definition at line 98 of file scalar\_imp.h.

**6.23.2.40 to\_scalar\_t()** [ 7/9]

```
template<>
qd_real glucat::numeric_traits< qd_real >::to_scalar_t (
    const long double & val ) [inline]
```

Cast to qd\_real.

Definition at line 107 of file scalar\_imp.h.

**6.23.2.41 to\_scalar\_t()** [ 8/9]

```
template<>
qd_real glucat::numeric_traits< qd_real >::to_scalar_t (
    const dd_real & val ) [inline]
```

Cast to qd\_real.

Definition at line 116 of file scalar\_imp.h.

6.23.2.42 `to_scalar_t()` [ 9/9 ]

```
template<typename Scalar_T >
template<typename Other_Scalar_T >
static Scalar_T glucat::numeric\_traits< Scalar\_T >::to\_scalar\_t (
    const Other_Scalar_T & val ) [inline], [static]
```

Cast to `Scalar_T`.

Definition at line 140 of file `scalar.h`.

Referenced by `glucat::matrix::nork_range()`, `glucat::to_demote()`, and `glucat::to_promote()`.

The documentation for this class was generated from the following file:

- [glucat/scalar.h](#)

6.24 `glucat::numeric_traits< Scalar_T >::promoted` Struct Reference

Promoted type.

```
#include <scalar.h>
```

## Public Types

- typedef double [type](#)

## 6.24.1 Detailed Description

```
template<typename Scalar_T>
struct glucat::numeric_traits< Scalar_T >::promoted
```

Promoted type.

Definition at line 144 of file `scalar.h`.

## 6.24.2 Member Typedef Documentation

6.24.2.1 `type`

```
template<typename Scalar_T >
typedef double glucat::numeric\_traits< Scalar\_T >::promoted::type
```

Definition at line 144 of file `scalar.h`.

The documentation for this struct was generated from the following file:

- [glucat/scalar.h](#)

## 6.25 glucat::random\_generator< Scalar\_T > Class Template Reference

Random number generator with single instance per Scalar\_T.

```
#include <random.h>
```

### Public Member Functions

- Scalar\_T [uniform](#) ()
- Scalar\_T [normal](#) ()

### Static Public Member Functions

- static [random\\_generator](#) & [generator](#) ()  
*Single instance of Random number generator.*

### Private Member Functions

- [random\\_generator](#) (const [random\\_generator](#) &)
- [random\\_generator](#) & [operator=](#) (const [random\\_generator](#) &)
- [random\\_generator](#) ()
- [~random\\_generator](#) ()

### Private Attributes

- std::mt19937 [uint\\_gen](#)
- std::uniform\_real\_distribution< double > [uniform\\_dist](#)
- std::normal\_distribution< double > [normal\\_dist](#)

### Static Private Attributes

- static const unsigned long [seed](#) = 19590921UL

### Friends

- class [friend\\_for\\_private\\_destructor](#)

#### 6.25.1 Detailed Description

```
template<typename Scalar_T>  
class glucat::random_generator< Scalar_T >
```

Random number generator with single instance per Scalar\_T.

Definition at line 47 of file random.h.

## 6.25.2 Constructor & Destructor Documentation

### 6.25.2.1 random\_generator() [1/2]

```
template<typename Scalar_T >
glucat::random_generator< Scalar_T >::random_generator (
    const random_generator< Scalar_T > & ) [private]
```

### 6.25.2.2 random\_generator() [2/2]

```
template<typename Scalar_T >
glucat::random_generator< Scalar_T >::random_generator ( ) [inline], [private]
```

Definition at line 83 of file random.h.

References glucat::random\_generator< Scalar\_T >::seed.

### 6.25.2.3 ~random\_generator()

```
template<typename Scalar_T >
glucat::random_generator< Scalar_T >::~~random_generator ( ) [inline], [private]
```

Definition at line 87 of file random.h.

## 6.25.3 Member Function Documentation

### 6.25.3.1 generator()

```
template<typename Scalar_T >
static random_generator& glucat::random_generator< Scalar_T >::generator ( ) [inline], [static]
```

Single instance of Random number generator.

Definition at line 51 of file random.h.

#### 6.25.3.2 normal()

```
template<typename Scalar_T >
Scalar_T glucat::random_generator< Scalar_T >::normal ( ) [inline]
```

Definition at line 93 of file random.h.

References glucat::random\_generator< Scalar\_T >::normal\_dist.

#### 6.25.3.3 operator=()

```
template<typename Scalar_T >
random_generator& glucat::random_generator< Scalar_T >::operator= (
    const random_generator< Scalar_T > & ) [private]
```

#### 6.25.3.4 uniform()

```
template<typename Scalar_T >
Scalar_T glucat::random_generator< Scalar_T >::uniform ( ) [inline]
```

Definition at line 91 of file random.h.

References glucat::random\_generator< Scalar\_T >::uniform\_dist.

### 6.25.4 Friends And Related Function Documentation

#### 6.25.4.1 friend\_for\_private\_destructor

```
template<typename Scalar_T >
friend class friend_for_private_destructor [friend]
```

Friend declaration to avoid compiler warning: "... only defines a private destructor and has no friends" Ref: Carlos O'Ryan, ACE <http://doc.ece.uci.edu>

Definition at line 56 of file random.h.

### 6.25.5 Member Data Documentation

#### 6.25.5.1 normal\_dist

```
template<typename Scalar_T >
std::normal_distribution<double> glucat::random_generator< Scalar_T >::normal_dist [private]
```

Definition at line 81 of file random.h.

Referenced by glucat::random\_generator< Scalar\_T >::normal().

#### 6.25.5.2 seed

```
template<typename Scalar_T >
const unsigned long glucat::random_generator< Scalar_T >::seed = 19590921UL [static], [private]
```

Definition at line 59 of file random.h.

Referenced by glucat::random\_generator< Scalar\_T >::random\_generator().

#### 6.25.5.3 uint\_gen

```
template<typename Scalar_T >
std::mt19937 glucat::random_generator< Scalar_T >::uint_gen [private]
```

Definition at line 79 of file random.h.

#### 6.25.5.4 uniform\_dist

```
template<typename Scalar_T >
std::uniform_real_distribution<double> glucat::random_generator< Scalar_T >::uniform_dist
[private]
```

Definition at line 80 of file random.h.

Referenced by glucat::random\_generator< Scalar\_T >::uniform().

The documentation for this class was generated from the following file:

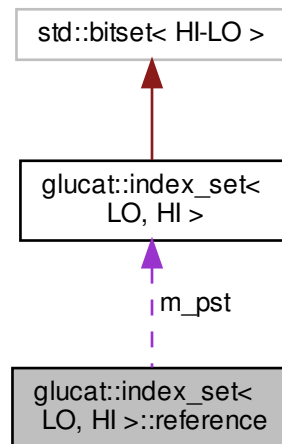
- glucat/[random.h](#)

## 6.26 glucat::index\_set< LO, HI >::reference Class Reference

Index set member reference.

```
#include <index_set.h>
```

Collaboration diagram for glucat::index\_set< LO, HI >::reference:



### Public Member Functions

- [reference](#) ([index\\_set\\_t](#) &ist, [index\\_t](#) idx)  
*index\_set reference*
- [~reference](#) ()
- [reference](#) & [operator=](#) (const bool x)  
*for b[i] = x;*
- [reference](#) & [operator=](#) (const [reference](#) &j)  
*for b[i] = b[j];*
- bool [operator~](#) () const  
*Flips a bit.*
- [operator bool](#) () const  
*for x = b[i];*
- [reference](#) & [flip](#) ()  
*for b[i].flip();*

### Private Member Functions

- [reference](#) ()  
*Private default constructor is left undefined.*

## Private Attributes

- [index\\_set\\_t](#) \* m\_pst
- [index\\_t](#) m\_idx

## Friends

- class [index\\_set](#)

### 6.26.1 Detailed Description

```
template<const index_t LO, const index_t HI>
class glucat::index_set< LO, HI >::reference
```

Index set member reference.

Definition at line 177 of file [index\\_set.h](#).

### 6.26.2 Constructor & Destructor Documentation

#### 6.26.2.1 [reference\(\)](#) [1/2]

```
template<const index_t LO, const index_t HI>
glucat::index_set< LO, HI >::reference::reference ( ) [private]
```

Private default constructor is left undefined.

#### 6.26.2.2 [reference\(\)](#) [2/2]

```
template<const index_t LO, const index_t HI>
glucat::index_set< LO, HI >::reference::reference (
    index_set_t & ist,
    index_t idx ) [inline]
```

[index\\_set](#) reference

Definition at line 983 of file [index\\_set\\_imp.h](#).

### 6.26.2.3 ~reference()

```
template<const index_t LO, const index_t HI>
glucat::index_set< LO, HI >::reference::~reference ( ) [inline]
```

Definition at line 184 of file index\_set.h.

## 6.26.3 Member Function Documentation

### 6.26.3.1 flip()

```
template<const index_t LO, const index_t HI>
index_set< LO, HI >::reference & glucat::index_set< LO, HI >::reference::flip ( ) [inline]
```

for b[i].flip();

Definition at line 1036 of file index\_set\_imp.h.

References glucat::index\_set< LO, HI >::reference::flip().

Referenced by glucat::index\_set< LO, HI >::reference::flip().

### 6.26.3.2 operator bool()

```
template<const index_t LO, const index_t HI>
glucat::index_set< LO, HI >::reference::operator bool ( ) const [inline]
```

for x = b[i];

Definition at line 1028 of file index\_set\_imp.h.

### 6.26.3.3 operator=() [1/2]

```
template<const index_t LO, const index_t HI>
index_set< LO, HI >::reference & glucat::index_set< LO, HI >::reference::operator= (
    const bool x ) [inline]
```

for b[i] = x;

Definition at line 993 of file index\_set\_imp.h.

**6.26.3.4 operator=()** [2/2]

```
template<const index_t LO, const index_t HI>
index_set< LO, HI >::reference & glucat::index_set< LO, HI >::reference::operator= (
    const reference & j ) [inline]
```

for b[i] = b[j];

Definition at line 1007 of file index\_set\_imp.h.

References glucat::index\_set< LO, HI >::reference::m\_idx, and glucat::index\_set< LO, HI >::reference::m\_pst.

**6.26.3.5 operator~()**

```
template<const index_t LO, const index_t HI>
bool glucat::index_set< LO, HI >::reference::operator~ ( ) const [inline]
```

Flips a bit.

flips the bit

Definition at line 1021 of file index\_set\_imp.h.

**6.26.4 Friends And Related Function Documentation****6.26.4.1 index\_set**

```
template<const index_t LO, const index_t HI>
friend class index_set [friend]
```

Definition at line 178 of file index\_set.h.

**6.26.5 Member Data Documentation****6.26.5.1 m\_idx**

```
template<const index_t LO, const index_t HI>
index_t glucat::index_set< LO, HI >::reference::m_idx [private]
```

Definition at line 198 of file index\_set.h.

Referenced by glucat::index\_set< LO, HI >::reference::operator=().

### 6.26.5.2 m\_pst

```
template<const index_t LO, const index_t HI>
index_set_t* glucat::index_set< LO, HI >::reference::m_pst [private]
```

Definition at line 197 of file index\_set.h.

Referenced by glucat::index\_set< LO, HI >::reference::operator=().

The documentation for this class was generated from the following files:

- glucat/index\_set.h
- glucat/index\_set\_imp.h

## 6.27 glucat::sorted\_range< Map\_T, Sorted\_Map\_T > Class Template Reference

Sorted range for use with output.

```
#include <framed_multi_imp.h>
```

### Public Types

- typedef Map\_T [map\\_t](#)
- typedef Sorted\_Map\_T [sorted\\_map\\_t](#)
- typedef Sorted\_Map\_T::const\_iterator [sorted\\_iterator](#)

### Public Member Functions

- [sorted\\_range](#) (Sorted\_Map\_T &sorted\_val, const Map\_T &val)

### Public Attributes

- [sorted\\_iterator](#) [sorted\\_begin](#)
- [sorted\\_iterator](#) [sorted\\_end](#)

### 6.27.1 Detailed Description

```
template<typename Map_T, typename Sorted_Map_T>
class glucat::sorted_range< Map_T, Sorted_Map_T >
```

Sorted range for use with output.

Definition at line 1326 of file framed\_multi\_imp.h.

### 6.27.2 Member Typedef Documentation

### 6.27.2.1 map\_t

```
template<typename Map_T, typename Sorted_Map_T>
typedef Map_T glucat::sorted_range< Map_T, Sorted_Map_T >::map_t
```

Definition at line 1329 of file framed\_multi\_imp.h.

### 6.27.2.2 sorted\_iterator

```
template<typename Map_T, typename Sorted_Map_T>
typedef Sorted_Map_T::const_iterator glucat::sorted_range< Map_T, Sorted_Map_T >::sorted_iterator
```

Definition at line 1331 of file framed\_multi\_imp.h.

### 6.27.2.3 sorted\_map\_t

```
template<typename Map_T, typename Sorted_Map_T>
typedef Sorted_Map_T glucat::sorted_range< Map_T, Sorted_Map_T >::sorted_map_t
```

Definition at line 1330 of file framed\_multi\_imp.h.

## 6.27.3 Constructor & Destructor Documentation

### 6.27.3.1 sorted\_range()

```
template<typename Map_T, typename Sorted_Map_T>
glucat::sorted_range< Map_T, Sorted_Map_T >::sorted_range (
    Sorted_Map_T & sorted_val,
    const Map_T & val ) [inline]
```

Definition at line 1333 of file framed\_multi\_imp.h.

References glucat::sorted\_range< Map\_T, Sorted\_Map\_T >::sorted\_begin, and glucat::sorted\_range< Map\_T, Sorted\_Map\_T >::sorted\_end.

## 6.27.4 Member Data Documentation

#### 6.27.4.1 sorted\_begin

```
template<typename Map_T, typename Sorted_Map_T>
sorted_iterator glucat::sorted_range< Map_T, Sorted_Map_T >::sorted_begin
```

Definition at line 1343 of file framed\_multi\_imp.h.

Referenced by glucat::operator<<(), and glucat::sorted\_range< Map\_T, Sorted\_Map\_T >::sorted\_range().

#### 6.27.4.2 sorted\_end

```
template<typename Map_T, typename Sorted_Map_T>
sorted_iterator glucat::sorted_range< Map_T, Sorted_Map_T >::sorted_end
```

Definition at line 1344 of file framed\_multi\_imp.h.

Referenced by glucat::operator<<(), and glucat::sorted\_range< Map\_T, Sorted\_Map\_T >::sorted\_range().

The documentation for this class was generated from the following file:

- glucat/framed\_multi\_imp.h

## 6.28 glucat::sorted\_range< Sorted\_Map\_T, Sorted\_Map\_T > Class Template Reference

```
#include <framed_multi_imp.h>
```

### Public Types

- typedef Sorted\_Map\_T [map\\_t](#)
- typedef Sorted\_Map\_T [sorted\\_map\\_t](#)
- typedef Sorted\_Map\_T::const\_iterator [sorted\\_iterator](#)

### Public Member Functions

- [sorted\\_range](#) (Sorted\_Map\_T &sorted\_val, const Sorted\_Map\_T &val)

### Public Attributes

- [sorted\\_iterator](#) [sorted\\_begin](#)
- [sorted\\_iterator](#) [sorted\\_end](#)

#### 6.28.1 Detailed Description

```
template<typename Sorted_Map_T>
class glucat::sorted_range< Sorted_Map_T, Sorted_Map_T >
```

Definition at line 1348 of file framed\_multi\_imp.h.

## 6.28.2 Member Typedef Documentation

### 6.28.2.1 map\_t

```
template<typename Sorted_Map_T >
typedef Sorted_Map_T glucat::sorted_range< Sorted_Map_T, Sorted_Map_T >::map_t
```

Definition at line 1351 of file framed\_multi\_imp.h.

### 6.28.2.2 sorted\_iterator

```
template<typename Sorted_Map_T >
typedef Sorted_Map_T::const_iterator glucat::sorted_range< Sorted_Map_T, Sorted_Map_T >↔
::sorted_iterator
```

Definition at line 1353 of file framed\_multi\_imp.h.

### 6.28.2.3 sorted\_map\_t

```
template<typename Sorted_Map_T >
typedef Sorted_Map_T glucat::sorted_range< Sorted_Map_T, Sorted_Map_T >::sorted_map_t
```

Definition at line 1352 of file framed\_multi\_imp.h.

## 6.28.3 Constructor & Destructor Documentation

### 6.28.3.1 sorted\_range()

```
template<typename Sorted_Map_T >
glucat::sorted_range< Sorted_Map_T, Sorted_Map_T >::sorted_range (
    Sorted_Map_T & sorted_val,
    const Sorted_Map_T & val ) [inline]
```

Definition at line 1355 of file framed\_multi\_imp.h.

## 6.28.4 Member Data Documentation

#### 6.28.4.1 sorted\_begin

```
template<typename Sorted_Map_T >
sorted_iterator glucat::sorted_range< Sorted_Map_T, Sorted_Map_T >::sorted_begin
```

Definition at line 1359 of file framed\_multi\_imp.h.

#### 6.28.4.2 sorted\_end

```
template<typename Sorted_Map_T >
sorted_iterator glucat::sorted_range< Sorted_Map_T, Sorted_Map_T >::sorted_end
```

Definition at line 1360 of file framed\_multi\_imp.h.

The documentation for this class was generated from the following file:

- [glucat/framed\\_multi\\_imp.h](#)

### 6.29 glucat::tuning< Mult\_Matrix\_Threshold, Div\_Max\_Steps, Sqrt\_Max\_Steps, Log\_Max\_Outer\_Steps, Log\_Max\_Inner\_Steps, Basis\_Max\_Count, Fast\_Size\_Threshold, Inv\_Fast\_Dim\_Threshold, Products\_Size\_Threshold, Function\_Precision > Struct Template Reference

Tuning policy.

```
#include <global.h>
```

#### Public Types

- enum { [mult\\_matrix\\_threshold](#) = Mult\_Matrix\_Threshold }  
*Minimum index count needed to invoke matrix multiplication algorithm.*
- enum { [div\\_max\\_steps](#) = Div\_Max\_Steps }  
*Maximum steps of iterative refinement in division algorithm.*
- enum { [sqrt\\_max\\_steps](#) = Sqrt\_Max\_Steps }  
*Maximum number of steps in square root iteration.*
- enum { [log\\_max\\_outer\\_steps](#) = Log\_Max\_Outer\_Steps }  
*Maximum number of incomplete square roots in cascade log algorithm.*
- enum { [log\\_max\\_inner\\_steps](#) = Log\_Max\_Inner\_Steps }  
*Maximum number of steps in incomplete square root within cascade log algorithm.*
- enum { [basis\\_max\\_count](#) = Basis\_Max\_Count }  
*Maximum index count of folded frames in basis cache.*
- enum { [fast\\_size\\_threshold](#) = Fast\_Size\_Threshold }  
*Minimum map size needed to invoke generalized FFT.*
- enum { [inv\\_fast\\_dim\\_threshold](#) = Inv\_Fast\_Dim\_Threshold }  
*Minimum matrix dimension needed to invoke inverse generalized FFT.*
- enum { [products\\_size\\_threshold](#) = Products\_Size\_Threshold }  
*Minimum size needed for to invoke faster products algorithms.*

- static const [precision\\_t function\\_precision](#) = Function\_Precision  
*Precision used for exp, log and sqrt functions.*

### 6.29.1 Detailed Description

```
template<unsigned int Mult_Matrix_Threshold = DEFAULT_Mult_Matrix_Threshold, unsigned int Div_Max_Steps = DEFAULT_↵
Div_Max_Steps, unsigned int Sqrt_Max_Steps = DEFAULT_Sqrt_Max_Steps, unsigned int Log_Max_Outer_Steps = DEFAULT_↵
Log_Max_Outer_Steps, unsigned int Log_Max_Inner_Steps = DEFAULT_Log_Max_Inner_Steps, unsigned int Basis_Max_Count =
DEFAULT_Basis_Max_Count, unsigned int Fast_Size_Threshold = DEFAULT_Fast_Size_Threshold, unsigned int Inv_Fast_Dim_↵
_Threshold = DEFAULT_Inv_Fast_Dim_Threshold, unsigned int Products_Size_Threshold = DEFAULT_Products_Size_Threshold,
precision_t Function_Precision = DEFAULT_Function_Precision>
struct glucat::tuning< Mult_Matrix_Threshold, Div_Max_Steps, Sqrt_Max_Steps, Log_Max_Outer_Steps, Log_Max_Inner_Steps,
Basis_Max_Count, Fast_Size_Threshold, Inv_Fast_Dim_Threshold, Products_Size_Threshold, Function_Precision >
```

Tuning policy.

Definition at line 151 of file global.h.

### 6.29.2 Member Enumeration Documentation

#### 6.29.2.1 anonymous enum

```
template<unsigned int Mult_Matrix_Threshold = DEFAULT_Mult_Matrix_Threshold, unsigned int
Div_Max_Steps = DEFAULT_Div_Max_Steps, unsigned int Sqrt_Max_Steps = DEFAULT_Sqrt_Max_Steps,
unsigned int Log_Max_Outer_Steps = DEFAULT_Log_Max_Outer_Steps, unsigned int Log_Max_Inner_↵
Steps = DEFAULT_Log_Max_Inner_Steps, unsigned int Basis_Max_Count = DEFAULT_Basis_Max_Count,
unsigned int Fast_Size_Threshold = DEFAULT_Fast_Size_Threshold, unsigned int Inv_Fast_Dim_↵
Threshold = DEFAULT_Inv_Fast_Dim_Threshold, unsigned int Products_Size_Threshold = DEFAULT_↵
Products_Size_Threshold, precision_t Function_Precision = DEFAULT_Function_Precision>
anonymous enum
```

Minimum matrix dimension needed to invoke inverse generalized FFT.

Enumerator

inv_fast_dim_threshold	
------------------------	--

Definition at line 174 of file global.h.

#### 6.29.2.2 anonymous enum

```
template<unsigned int Mult_Matrix_Threshold = DEFAULT_Mult_Matrix_Threshold, unsigned int
Div_Max_Steps = DEFAULT_Div_Max_Steps, unsigned int Sqrt_Max_Steps = DEFAULT_Sqrt_Max_Steps,
```

```

unsigned int Log_Max_Outer_Steps = DEFAULT_Log_Max_Outer_Steps, unsigned int Log_Max_Inner_↵
Steps = DEFAULT_Log_Max_Inner_Steps, unsigned int Basis_Max_Count = DEFAULT_Basis_Max_Count,
unsigned int Fast_Size_Threshold = DEFAULT_Fast_Size_Threshold, unsigned int Inv_Fast_Dim_↵
Threshold = DEFAULT_Inv_Fast_Dim_Threshold, unsigned int Products_Size_Threshold = DEFAULT_↵
Products_Size_Threshold, precision_t Function_Precision = DEFAULT_Function_Precision>
anonymous enum

```

Minimum size needed for to invoke faster products algorithms.

#### Enumerator

products_size_threshold	
-------------------------	--

Definition at line 177 of file global.h.

#### 6.29.2.3 anonymous enum

```

template<unsigned int Mult_Matrix_Threshold = DEFAULT_Mult_Matrix_Threshold, unsigned int
Div_Max_Steps = DEFAULT_Div_Max_Steps, unsigned int Sqrt_Max_Steps = DEFAULT_Sqrt_Max_Steps,
unsigned int Log_Max_Outer_Steps = DEFAULT_Log_Max_Outer_Steps, unsigned int Log_Max_Inner_↵
Steps = DEFAULT_Log_Max_Inner_Steps, unsigned int Basis_Max_Count = DEFAULT_Basis_Max_Count,
unsigned int Fast_Size_Threshold = DEFAULT_Fast_Size_Threshold, unsigned int Inv_Fast_Dim_↵
Threshold = DEFAULT_Inv_Fast_Dim_Threshold, unsigned int Products_Size_Threshold = DEFAULT_↵
Products_Size_Threshold, precision_t Function_Precision = DEFAULT_Function_Precision>
anonymous enum

```

Minimum index count needed to invoke matrix multiplication algorithm.

#### Enumerator

mult_matrix_threshold	
-----------------------	--

Definition at line 155 of file global.h.

#### 6.29.2.4 anonymous enum

```

template<unsigned int Mult_Matrix_Threshold = DEFAULT_Mult_Matrix_Threshold, unsigned int
Div_Max_Steps = DEFAULT_Div_Max_Steps, unsigned int Sqrt_Max_Steps = DEFAULT_Sqrt_Max_Steps,
unsigned int Log_Max_Outer_Steps = DEFAULT_Log_Max_Outer_Steps, unsigned int Log_Max_Inner_↵
Steps = DEFAULT_Log_Max_Inner_Steps, unsigned int Basis_Max_Count = DEFAULT_Basis_Max_Count,
unsigned int Fast_Size_Threshold = DEFAULT_Fast_Size_Threshold, unsigned int Inv_Fast_Dim_↵
Threshold = DEFAULT_Inv_Fast_Dim_Threshold, unsigned int Products_Size_Threshold = DEFAULT_↵
Products_Size_Threshold, precision_t Function_Precision = DEFAULT_Function_Precision>
anonymous enum

```

Maximum steps of iterative refinement in division algorithm.

Enumerator

div_max_steps	
---------------	--

Definition at line 158 of file global.h.

6.29.2.5 anonymous enum

```
template<unsigned int Mult_Matrix_Threshold = DEFAULT_Mult_Matrix_Threshold, unsigned int Div_Max_Steps = DEFAULT_Div_Max_Steps, unsigned int Sqrt_Max_Steps = DEFAULT_Sqrt_Max_Steps, unsigned int Log_Max_Outer_Steps = DEFAULT_Log_Max_Outer_Steps, unsigned int Log_Max_Inner_Steps = DEFAULT_Log_Max_Inner_Steps, unsigned int Basis_Max_Count = DEFAULT_Basis_Max_Count, unsigned int Fast_Size_Threshold = DEFAULT_Fast_Size_Threshold, unsigned int Inv_Fast_Dim_Threshold = DEFAULT_Inv_Fast_Dim_Threshold, unsigned int Products_Size_Threshold = DEFAULT_Products_Size_Threshold, precision_t Function_Precision = DEFAULT_Function_Precision>
anonymous enum
```

Maximum number of steps in square root iteration.

Enumerator

sqrt_max_steps	
----------------	--

Definition at line 161 of file global.h.

6.29.2.6 anonymous enum

```
template<unsigned int Mult_Matrix_Threshold = DEFAULT_Mult_Matrix_Threshold, unsigned int Div_Max_Steps = DEFAULT_Div_Max_Steps, unsigned int Sqrt_Max_Steps = DEFAULT_Sqrt_Max_Steps, unsigned int Log_Max_Outer_Steps = DEFAULT_Log_Max_Outer_Steps, unsigned int Log_Max_Inner_Steps = DEFAULT_Log_Max_Inner_Steps, unsigned int Basis_Max_Count = DEFAULT_Basis_Max_Count, unsigned int Fast_Size_Threshold = DEFAULT_Fast_Size_Threshold, unsigned int Inv_Fast_Dim_Threshold = DEFAULT_Inv_Fast_Dim_Threshold, unsigned int Products_Size_Threshold = DEFAULT_Products_Size_Threshold, precision_t Function_Precision = DEFAULT_Function_Precision>
anonymous enum
```

Maximum number of incomplete square roots in cascade log algorithm.

Enumerator

log_max_outer_steps	
---------------------	--

Definition at line 164 of file global.h.

### 6.29.2.7 anonymous enum

```
template<unsigned int Mult_Matrix_Threshold = DEFAULT_Mult_Matrix_Threshold, unsigned int
Div_Max_Steps = DEFAULT_Div_Max_Steps, unsigned int Sqrt_Max_Steps = DEFAULT_Sqrt_Max_Steps,
unsigned int Log_Max_Outer_Steps = DEFAULT_Log_Max_Outer_Steps, unsigned int Log_Max_Inner_↵
Steps = DEFAULT_Log_Max_Inner_Steps, unsigned int Basis_Max_Count = DEFAULT_Basis_Max_Count,
unsigned int Fast_Size_Threshold = DEFAULT_Fast_Size_Threshold, unsigned int Inv_Fast_Dim_↵
Threshold = DEFAULT_Inv_Fast_Dim_Threshold, unsigned int Products_Size_Threshold = DEFAULT_↵
Products_Size_Threshold, precision_t Function_Precision = DEFAULT_Function_Precision>
anonymous enum
```

Maximum number of steps in incomplete square root within cascade log algorithm.

#### Enumerator

log_max_inner_steps	
---------------------	--

Definition at line 166 of file global.h.

### 6.29.2.8 anonymous enum

```
template<unsigned int Mult_Matrix_Threshold = DEFAULT_Mult_Matrix_Threshold, unsigned int
Div_Max_Steps = DEFAULT_Div_Max_Steps, unsigned int Sqrt_Max_Steps = DEFAULT_Sqrt_Max_Steps,
unsigned int Log_Max_Outer_Steps = DEFAULT_Log_Max_Outer_Steps, unsigned int Log_Max_Inner_↵
Steps = DEFAULT_Log_Max_Inner_Steps, unsigned int Basis_Max_Count = DEFAULT_Basis_Max_Count,
unsigned int Fast_Size_Threshold = DEFAULT_Fast_Size_Threshold, unsigned int Inv_Fast_Dim_↵
Threshold = DEFAULT_Inv_Fast_Dim_Threshold, unsigned int Products_Size_Threshold = DEFAULT_↵
Products_Size_Threshold, precision_t Function_Precision = DEFAULT_Function_Precision>
anonymous enum
```

Maximum index count of folded frames in basis cache.

#### Enumerator

basis_max_count	
-----------------	--

Definition at line 169 of file global.h.

### 6.29.2.9 anonymous enum

```
template<unsigned int Mult_Matrix_Threshold = DEFAULT_Mult_Matrix_Threshold, unsigned int
Div_Max_Steps = DEFAULT_Div_Max_Steps, unsigned int Sqrt_Max_Steps = DEFAULT_Sqrt_Max_Steps,
unsigned int Log_Max_Outer_Steps = DEFAULT_Log_Max_Outer_Steps, unsigned int Log_Max_Inner_↵
Steps = DEFAULT_Log_Max_Inner_Steps, unsigned int Basis_Max_Count = DEFAULT_Basis_Max_Count,
unsigned int Fast_Size_Threshold = DEFAULT_Fast_Size_Threshold, unsigned int Inv_Fast_Dim_↵
Threshold = DEFAULT_Inv_Fast_Dim_Threshold, unsigned int Products_Size_Threshold = DEFAULT_↵
Products_Size_Threshold, precision_t Function_Precision = DEFAULT_Function_Precision>
anonymous enum
```

Minimum map size needed to invoke generalized FFT.

## Enumerator

fast_size_threshold	
---------------------	--

Definition at line 172 of file global.h.

### 6.29.3 Member Data Documentation

#### 6.29.3.1 function\_precision

```
template<unsigned int Mult_Matrix_Threshold = DEFAULT_Mult_Matrix_Threshold, unsigned int
Div_Max_Steps = DEFAULT_Div_Max_Steps, unsigned int Sqrt_Max_Steps = DEFAULT_Sqrt_Max_Steps,
unsigned int Log_Max_Outer_Steps = DEFAULT_Log_Max_Outer_Steps, unsigned int Log_Max_Inner_↵
Steps = DEFAULT_Log_Max_Inner_Steps, unsigned int Basis_Max_Count = DEFAULT_Basis_Max_Count,
unsigned int Fast_Size_Threshold = DEFAULT_Fast_Size_Threshold, unsigned int Inv_Fast_Dim_↵
Threshold = DEFAULT_Inv_Fast_Dim_Threshold, unsigned int Products_Size_Threshold = DEFAULT_↵
Products_Size_Threshold, precision_t Function_Precision = DEFAULT_Function_Precision>
const precision\_t glucat::tuning< Mult_Matrix_Threshold, Div_Max_Steps, Sqrt_Max_Steps, Log_↵
_Max_Outer_Steps, Log_Max_Inner_Steps, Basis_Max_Count, Fast_Size_Threshold, Inv_Fast_Dim_↵
_Threshold, Products_Size_Threshold, Function_Precision >::function_precision = Function_↵
Precision [static]
```

Precision used for exp, log and sqrt functions.

Definition at line 180 of file global.h.

Referenced by `glucat::exp()`, `glucat::log()`, and `glucat::sqrt()`.

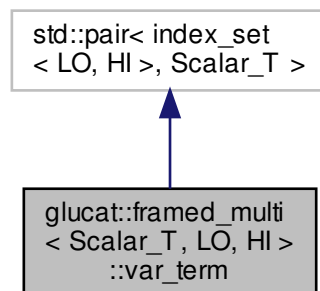
The documentation for this struct was generated from the following file:

- [glucat/global.h](#)

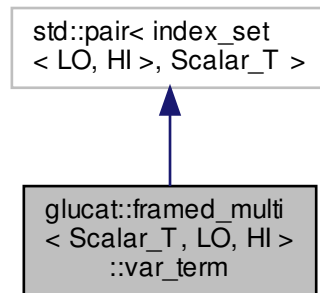
## 6.30 glucat::framed\_multi< Scalar\_T, LO, HI >::var\_term Class Reference

Variable term.

Inheritance diagram for `glucat::framed_multi< Scalar_T, LO, HI >::var_term`:



Collaboration diagram for `glucat::framed_multi< Scalar_T, LO, HI >::var_term`:



## Public Types

- typedef `std::pair< index\_set< LO, HI >, Scalar\_T >` `var_pair_t`

## Public Member Functions

- `~var\_term ()`  
*Destructor.*
- `var\_term ()`  
*Default constructor.*
- `var\_term (const index\_set\_t ist, const Scalar\_T &crd=Scalar\_T(1))`  
*Construct a variable term from an index set and a scalar coordinate.*
- `var\_term\_t & operator\*= (const term\_t &rhs)`  
*Product of variable term and term.*

## Static Public Member Functions

- static const `std::string classname ()`  
*Class name used in messages.*

### 6.30.1 Detailed Description

```
template<typename Scalar\_T = double, const index\_t LO = DEFAULT\_LO, const index\_t HI = DEFAULT\_HI>
class glucat::framed_multi< Scalar\_T, LO, HI >::var_term
```

Variable term.

Definition at line 308 of file `framed_multi.h`.

## 6.30.2 Member Typedef Documentation

### 6.30.2.1 var\_pair\_t

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
typedef std::pair<index_set<LO,HI>, Scalar_T> glucat::framed_multi< Scalar_T, LO, HI >::var_term::var_pair_t
```

Definition at line 312 of file framed\_multi.h.

## 6.30.3 Constructor & Destructor Documentation

### 6.30.3.1 ~var\_term()

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
glucat::framed_multi< Scalar_T, LO, HI >::var_term::~~var_term ( ) [inline]
```

Destructor.

Definition at line 318 of file framed\_multi.h.

### 6.30.3.2 var\_term() [1/2]

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
glucat::framed_multi< Scalar_T, LO, HI >::var_term::var_term ( ) [inline]
```

Default constructor.

Definition at line 320 of file framed\_multi.h.

### 6.30.3.3 var\_term() [2/2]

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
glucat::framed_multi< Scalar_T, LO, HI >::var_term::var_term (
    const index_set_t ist,
    const Scalar_T & crd = Scalar_T(1) ) [inline]
```

Construct a variable term from an index set and a scalar coordinate.

Definition at line 324 of file framed\_multi.h.

## 6.30.4 Member Function Documentation

### 6.30.4.1 `classname()`

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
static const std::string glucat::framed\_multi< Scalar_T, LO, HI >::var_term::classname ( )
[inline], [static]
```

Class name used in messages.

Definition at line 315 of file `framed_multi.h`.

### 6.30.4.2 `operator*=( )`

```
template<typename Scalar_T = double, const index_t LO = DEFAULT_LO, const index_t HI = DEFAULT_HI>
LT_HI>
var\_term\_t& glucat::framed\_multi< Scalar_T, LO, HI >::var_term::operator*= (
    const term\_t & rhs ) [inline]
```

Product of variable term and term.

Definition at line 328 of file `framed_multi.h`.

The documentation for this class was generated from the following file:

- [glucat/framed\\_multi.h](#)

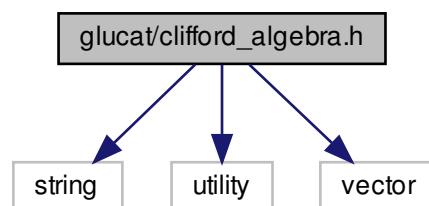
## Chapter 7

# File Documentation

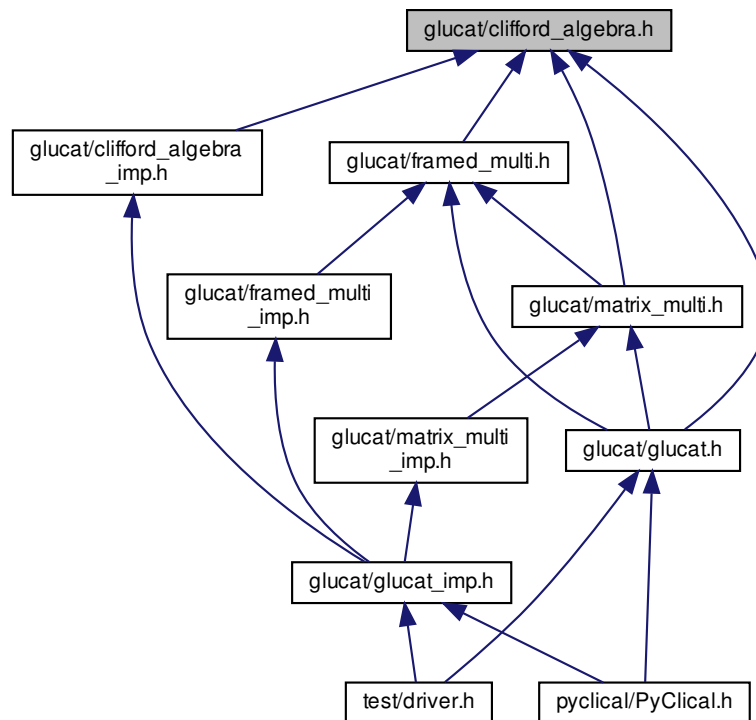
### 7.1 glucat/clifford\_algebra.h File Reference

```
#include <string>
#include <utility>
#include <vector>
```

Include dependency graph for clifford\_algebra.h:



This graph shows which files directly or indirectly include this file:



## Classes

- class [glucat::clifford\\_algebra< Scalar\\_T, Index\\_Set\\_T, Multivector\\_T >](#)  
*clifford\_algebra<> declares the operations of a Clifford algebra*

## Namespaces

- [glucat](#)

## Macros

- [#define \\_GLUCAT\\_CLIFFORD\\_ALGEBRA\\_OPERATIONS](#)

## Functions

- template<template< typename, const index\_t, const index\_t > class Multivector, template< typename, const index\_t, const index\_t > class RHS, typename Scalar\_T, const index\_t LO, const index\_t HI>  
 bool [glucat::operator!=](#) (const Multivector< Scalar\_T, LO, HI > &lhs, const RHS< Scalar\_T, LO, HI > &rhs)  
*Test for inequality of multivectors.*

- template<template< typename, const index\_t, const index\_t > class Multivector, typename Scalar\_T , const index\_t LO, const index\_t HI>  
 bool [glucat::operator!=](#) (const Multivector< Scalar\_T, LO, HI > &lhs, const Scalar\_T &scr)  
*Test for inequality of multivector and scalar.*
- template<template< typename, const index\_t, const index\_t > class Multivector, typename Scalar\_T , const index\_t LO, const index\_t HI>  
 bool [glucat::operator!=](#) (const Scalar\_T &scr, const Multivector< Scalar\_T, LO, HI > &rhs)  
*Test for inequality of scalar and multivector.*
- template<template< typename, const index\_t, const index\_t > class Multivector, typename Scalar\_T , const index\_t LO, const index\_t HI>  
 const Multivector< Scalar\_T, LO, HI > [glucat::operator+](#) (const Multivector< Scalar\_T, LO, HI > &lhs, const Scalar\_T &scr)  
*Geometric sum of multivector and scalar.*
- template<template< typename, const index\_t, const index\_t > class Multivector, typename Scalar\_T , const index\_t LO, const index\_t HI>  
 const Multivector< Scalar\_T, LO, HI > [glucat::operator+](#) (const Scalar\_T &scr, const Multivector< Scalar\_T, LO, HI > &rhs)  
*Geometric sum of scalar and multivector.*
- template<template< typename, const index\_t, const index\_t > class Multivector, template< typename, const index\_t, const index\_t > class RHS, typename Scalar\_T , const index\_t LO, const index\_t HI>  
 const Multivector< Scalar\_T, LO, HI > [glucat::operator+](#) (const Multivector< Scalar\_T, LO, HI > &lhs, const RHS< Scalar\_T, LO, HI > &rhs)  
*Geometric sum.*
- template<template< typename, const index\_t, const index\_t > class Multivector, typename Scalar\_T , const index\_t LO, const index\_t HI>  
 const Multivector< Scalar\_T, LO, HI > [glucat::operator-](#) (const Multivector< Scalar\_T, LO, HI > &lhs, const Scalar\_T &scr)  
*Geometric difference of multivector and scalar.*
- template<template< typename, const index\_t, const index\_t > class Multivector, typename Scalar\_T , const index\_t LO, const index\_t HI>  
 const Multivector< Scalar\_T, LO, HI > [glucat::operator-](#) (const Scalar\_T &scr, const Multivector< Scalar\_T, LO, HI > &rhs)  
*Geometric difference of scalar and multivector.*
- template<template< typename, const index\_t, const index\_t > class Multivector, template< typename, const index\_t, const index\_t > class RHS, typename Scalar\_T , const index\_t LO, const index\_t HI>  
 const Multivector< Scalar\_T, LO, HI > [glucat::operator-](#) (const Multivector< Scalar\_T, LO, HI > &lhs, const RHS< Scalar\_T, LO, HI > &rhs)  
*Geometric difference.*
- template<template< typename, const index\_t, const index\_t > class Multivector, typename Scalar\_T , const index\_t LO, const index\_t HI>  
 const Multivector< Scalar\_T, LO, HI > [glucat::operator\\*](#) (const Multivector< Scalar\_T, LO, HI > &lhs, const Scalar\_T &scr)  
*Product of multivector and scalar.*
- template<template< typename, const index\_t, const index\_t > class Multivector, typename Scalar\_T , const index\_t LO, const index\_t HI>  
 const Multivector< Scalar\_T, LO, HI > [glucat::operator\\*](#) (const Scalar\_T &scr, const Multivector< Scalar\_T, LO, HI > &rhs)  
*Product of scalar and multivector.*
- template<template< typename, const index\_t, const index\_t > class Multivector, template< typename, const index\_t, const index\_t > class RHS, typename Scalar\_T , const index\_t LO, const index\_t HI>  
 const Multivector< Scalar\_T, LO, HI > [glucat::operator\\*](#) (const Multivector< Scalar\_T, LO, HI > &lhs, const RHS< Scalar\_T, LO, HI > &rhs)  
*Geometric product.*

- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator^ (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`

*Outer product.*

- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator & (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`

*Inner product.*

- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator% (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`

*Left contraction.*

- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`Scalar_T glucat::star (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`

*Hestenes scalar product.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator/ (const Multivector< Scalar_T, LO, HI > &lhs, const Scalar_T &scr)`

*Quotient of multivector and scalar.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator/ (const Scalar_T &scr, const Multivector< Scalar_T, LO, HI > &rhs)`

*Quotient of scalar and multivector.*

- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator/ (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`

*Geometric quotient.*

- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator| (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`

*Transformation via twisted adjoint action.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::inv (const Multivector< Scalar_T, LO, HI > &val)`

*Geometric multiplicative inverse.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::pow (const Multivector< Scalar_T, LO, HI > &lhs, int rhs)`

*Integer power of multivector.*

- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::pow (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`

*Multivector power of multivector.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::outer\_pow (const Multivector< Scalar_T, LO, HI > &lhs, int rhs)`

*Outer product power of multivector.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`

`Scalar_T glucat::scalar (const Multivector< Scalar_T, LO, HI > &val)`

*Scalar part.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`

`Scalar_T glucat::real (const Multivector< Scalar_T, LO, HI > &val)`

*Real part: synonym for scalar part.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`

`Scalar_T glucat::imag (const Multivector< Scalar_T, LO, HI > &val)`

*Imaginary part: deprecated (always 0)*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`

`const Multivector< Scalar_T, LO, HI > glucat::pure (const Multivector< Scalar_T, LO, HI > &val)`

*Pure part.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`

`const Multivector< Scalar_T, LO, HI > glucat::even (const Multivector< Scalar_T, LO, HI > &val)`

*Even part.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`

`const Multivector< Scalar_T, LO, HI > glucat::odd (const Multivector< Scalar_T, LO, HI > &val)`

*Odd part.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`

`const std::vector< Scalar_T > glucat::vector_part (const Multivector< Scalar_T, LO, HI > &val)`

*Vector part of multivector, as a vector\_t with respect to frame()*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`

`const Multivector< Scalar_T, LO, HI > glucat::involute (const Multivector< Scalar_T, LO, HI > &val)`

*Main involution, each {i} is replaced by -{i} in each term, eg. {1}\*{2} -> (-{2})\*(-{1})*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`

`const Multivector< Scalar_T, LO, HI > glucat::reverse (const Multivector< Scalar_T, LO, HI > &val)`

*Reversion, eg. {1}\*{2} -> {2}\*{1}.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`

`const Multivector< Scalar_T, LO, HI > glucat::conj (const Multivector< Scalar_T, LO, HI > &val)`

*Conjugation, rev o invo == invo o rev.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`

`Scalar_T glucat::quad (const Multivector< Scalar_T, LO, HI > &val)`

*Scalar\_T quadratic form == (rev(x)\*x)(0)*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`

`Scalar_T glucat::norm (const Multivector< Scalar_T, LO, HI > &val)`

*Scalar\_T norm == sum of norm of coordinates.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`

`Scalar_T glucat::abs (const Multivector< Scalar_T, LO, HI > &val)`

*Absolute value == sqrt(norm)*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>  
 Scalar_T glucat::max\_abs (const Multivector< Scalar_T, LO, HI > &val)  
Maximum of absolute values of components of multivector: multivector infinity norm.`
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>  
 const Multivector< Scalar_T, LO, HI > glucat::complexifier (const Multivector< Scalar_T, LO, HI > &val)  
Square root of -1 which commutes with all members of the frame of the given multivector.`
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>  
 const Multivector< Scalar_T, LO, HI > glucat::elliptic (const Multivector< Scalar_T, LO, HI > &val)`
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>  
 const Multivector< Scalar_T, LO, HI > glucat::sqrt (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)  
Square root of multivector with specified complexifier.`
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>  
 const Multivector< Scalar_T, LO, HI > glucat::sqrt (const Multivector< Scalar_T, LO, HI > &val)  
Square root of multivector.`
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>  
 const Multivector< Scalar_T, LO, HI > glucat::clifford\_exp (const Multivector< Scalar_T, LO, HI > &val)  
Exponential of multivector.`
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>  
 const Multivector< Scalar_T, LO, HI > glucat::log (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)  
Natural logarithm of multivector with specified complexifier.`
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>  
 const Multivector< Scalar_T, LO, HI > glucat::log (const Multivector< Scalar_T, LO, HI > &val)  
Natural logarithm of multivector.`
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>  
 const Multivector< Scalar_T, LO, HI > glucat::cos (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)  
Cosine of multivector with specified complexifier.`
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>  
 const Multivector< Scalar_T, LO, HI > glucat::cos (const Multivector< Scalar_T, LO, HI > &val)  
Cosine of multivector.`
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>  
 const Multivector< Scalar_T, LO, HI > glucat::acos (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)  
Inverse cosine of multivector with specified complexifier.`
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>  
 const Multivector< Scalar_T, LO, HI > glucat::acos (const Multivector< Scalar_T, LO, HI > &val)  
Inverse cosine of multivector.`
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>  
 const Multivector< Scalar_T, LO, HI > glucat::cosh (const Multivector< Scalar_T, LO, HI > &val)  
Hyperbolic cosine of multivector.`



- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::atan (const Multivector< Scalar_T, LO, HI > &val)`  
*Inverse tangent of multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::tanh (const Multivector< Scalar_T, LO, HI > &val)`  
*Hyperbolic tangent of multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::atanh (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)`  
*Inverse hyperbolic tangent of multivector with specified complexifier.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::atanh (const Multivector< Scalar_T, LO, HI > &val)`  
*Inverse hyperbolic tangent of multivector.*

## 7.1.1 Macro Definition Documentation

### 7.1.1.1 \_GLUCAT\_CLIFFORD\_ALGEBRA\_OPERATIONS

```
#define _GLUCAT_CLIFFORD_ALGEBRA_OPERATIONS
```

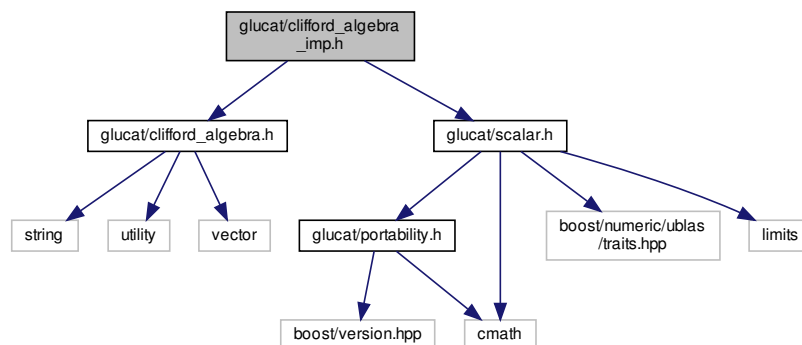
Definition at line 134 of file `clifford_algebra.h`.

## 7.2 `glucat/clifford_algebra_imp.h` File Reference

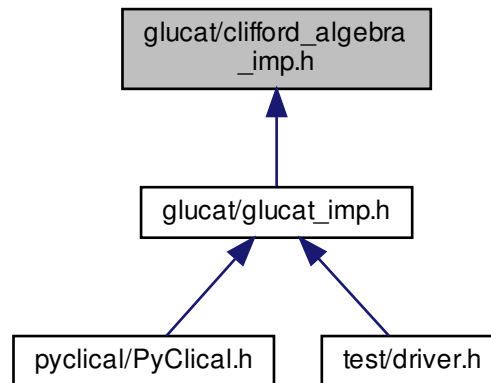
```
#include <glucat/clifford_algebra.h>
```

```
#include <glucat/scalar.h>
```

Include dependency graph for `clifford_algebra_imp.h`:



This graph shows which files directly or indirectly include this file:



## Namespaces

- [glucat](#)

## Functions

- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T, const index_t LO, const index_t HI>`  
`bool glucat::operator!= (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`  
*Test for inequality of multivectors.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T, const index_t LO, const index_t HI>`  
`bool glucat::operator!= (const Multivector< Scalar_T, LO, HI > &lhs, const Scalar_T &scr)`  
*Test for inequality of multivector and scalar.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T, const index_t LO, const index_t HI>`  
`bool glucat::operator!= (const Scalar_T &scr, const Multivector< Scalar_T, LO, HI > &rhs)`  
*Test for inequality of scalar and multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T, const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator+ (const Multivector< Scalar_T, LO, HI > &lhs, const Scalar_T &scr)`  
*Geometric sum of multivector and scalar.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T, const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator+ (const Scalar_T &scr, const Multivector< Scalar_T, LO, HI > &rhs)`  
*Geometric sum of scalar and multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T, const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator+ (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`

*Geometric sum.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator- (const Multivector< Scalar_T, LO, HI > &lhs, const Scalar_T &scr)`

*Geometric difference of multivector and scalar.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator- (const Scalar_T &scr, const Multivector< Scalar_T, LO, HI > &rhs)`

*Geometric difference of scalar and multivector.*

- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator- (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`

*Geometric difference.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator\* (const Multivector< Scalar_T, LO, HI > &lhs, const Scalar_T &scr)`

*Product of multivector and scalar.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator\* (const Scalar_T &scr, const Multivector< Scalar_T, LO, HI > &rhs)`

*Product of scalar and multivector.*

- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator\* (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`

*Geometric product.*

- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator^ (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`

*Outer product.*

- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator & (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`

*Inner product.*

- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator% (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`

*Left contraction.*

- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t > class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`Scalar_T glucat::star (const Multivector< Scalar_T, LO, HI > &lhs, const RHS< Scalar_T, LO, HI > &rhs)`

*Hestenes scalar product.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator/ (const Multivector< Scalar_T, LO, HI > &lhs, const Scalar_T &scr)`

*Quotient of multivector and scalar.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator/ (const Scalar_T &scr, const Multivector< Scalar_T,`  
`LO, HI > &rhs)`

*Quotient of scalar and multivector.*

- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t >`  
`class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator/ (const Multivector< Scalar_T, LO, HI > &lhs, const`  
`RHS< Scalar_T, LO, HI > &rhs)`

*Geometric quotient.*

- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t >`  
`class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::operator| (const Multivector< Scalar_T, LO, HI > &lhs, const`  
`RHS< Scalar_T, LO, HI > &rhs)`

*Transformation via twisted adjoint action.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t`  
`HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::inv (const Multivector< Scalar_T, LO, HI > &val)`

*Geometric multiplicative inverse.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t`  
`HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::pow (const Multivector< Scalar_T, LO, HI > &lhs, int rhs)`

*Integer power of multivector.*

- `template<template< typename, const index_t, const index_t > class Multivector, template< typename, const index_t, const index_t >`  
`class RHS, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::pow (const Multivector< Scalar_T, LO, HI > &lhs, const RHS<`  
`Scalar_T, LO, HI > &rhs)`

*Multivector power of multivector.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t`  
`HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::outer_pow (const Multivector< Scalar_T, LO, HI > &lhs, int`  
`rhs)`

*Outer product power of multivector.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t`  
`HI>`  
`Scalar_T glucat::scalar (const Multivector< Scalar_T, LO, HI > &val)`

*Scalar part.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t`  
`HI>`  
`Scalar_T glucat::real (const Multivector< Scalar_T, LO, HI > &val)`

*Real part: synonym for scalar part.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t`  
`HI>`  
`Scalar_T glucat::imag (const Multivector< Scalar_T, LO, HI > &val)`

*Imaginary part: deprecated (always 0)*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t`  
`HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::pure (const Multivector< Scalar_T, LO, HI > &val)`

*Pure part.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t`  
`HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::even (const Multivector< Scalar_T, LO, HI > &val)`

*Even part.*

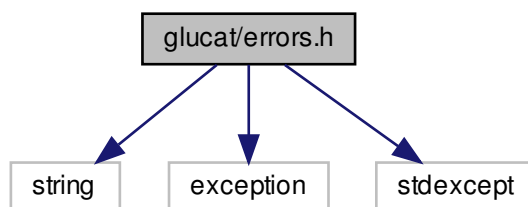
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::odd (const Multivector< Scalar_T, LO, HI > &val)`  
*Odd part.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const std::vector< Scalar_T > glucat::vector\_part (const Multivector< Scalar_T, LO, HI > &val)`  
*Vector part of multivector, as a vector\_t with respect to frame()*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::involute (const Multivector< Scalar_T, LO, HI > &val)`  
*Main involution, each {i} is replaced by -{i} in each term, eg. {1}\*{2} -> (-{2})\*(-{1})*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::reverse (const Multivector< Scalar_T, LO, HI > &val)`  
*Reversion, eg. {1}\*{2} -> {2}\*{1}.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::conj (const Multivector< Scalar_T, LO, HI > &val)`  
*Conjugation, rev o invo == invo o rev.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`Scalar_T glucat::quad (const Multivector< Scalar_T, LO, HI > &val)`  
*Scalar\_T quadratic form == (rev(x)\*x)(0)*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`Scalar_T glucat::norm (const Multivector< Scalar_T, LO, HI > &val)`  
*Scalar\_T norm == sum of norm of coordinates.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`Scalar_T glucat::abs (const Multivector< Scalar_T, LO, HI > &val)`  
*Absolute value == sqrt(norm)*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`Scalar_T glucat::max\_abs (const Multivector< Scalar_T, LO, HI > &val)`  
*Maximum of absolute values of components of multivector: multivector infinity norm.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::complexifier (const Multivector< Scalar_T, LO, HI > &val)`  
*Square root of -1 which commutes with all members of the frame of the given multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::elliptic (const Multivector< Scalar_T, LO, HI > &val)`
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`static void glucat::check\_complex (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)`  
*Check that i is a valid complexifier for val.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::sqrt (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)`  
*Square root of multivector with specified complexifier.*

- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::sqrt (const Multivector< Scalar_T, LO, HI > &val)`  
*Square root of multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::clifford_exp (const Multivector< Scalar_T, LO, HI > &val)`  
*Exponential of multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::log (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)`  
*Natural logarithm of multivector with specified complexifier.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::log (const Multivector< Scalar_T, LO, HI > &val)`  
*Natural logarithm of multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::cosh (const Multivector< Scalar_T, LO, HI > &val)`  
*Hyperbolic cosine of multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::acosh (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)`  
*Inverse hyperbolic cosine of multivector with specified complexifier.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::acosh (const Multivector< Scalar_T, LO, HI > &val)`  
*Inverse hyperbolic cosine of multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::cos (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)`  
*Cosine of multivector with specified complexifier.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::cos (const Multivector< Scalar_T, LO, HI > &val)`  
*Cosine of multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::acos (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)`  
*Inverse cosine of multivector with specified complexifier.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::acos (const Multivector< Scalar_T, LO, HI > &val)`  
*Inverse cosine of multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::sinh (const Multivector< Scalar_T, LO, HI > &val)`  
*Hyperbolic sine of multivector.*
- `template<template< typename, const index_t, const index_t > class Multivector, typename Scalar_T , const index_t LO, const index_t HI>`  
`const Multivector< Scalar_T, LO, HI > glucat::asinh (const Multivector< Scalar_T, LO, HI > &val, const Multivector< Scalar_T, LO, HI > &i, const bool prechecked=false)`

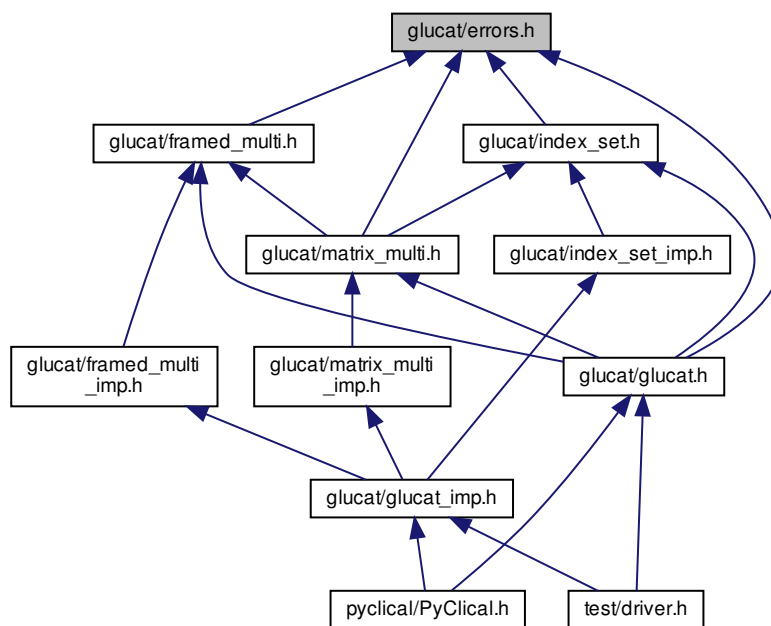


### 7.3 glucat/errors.h File Reference

```
#include <string>
#include <exception>
#include <stdexcept>
Include dependency graph for errors.h:
```



This graph shows which files directly or indirectly include this file:



## Classes

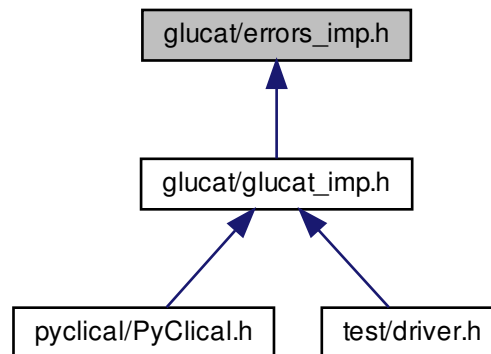
- class `glucat::glucat_error`  
*Abstract exception class.*
- class `glucat::error< Class_T >`  
*Specific exception class.*

## Namespaces

- [glucat](#)

## 7.4 glucat/errors\_imp.h File Reference

This graph shows which files directly or indirectly include this file:



## Namespaces

- [glucat](#)

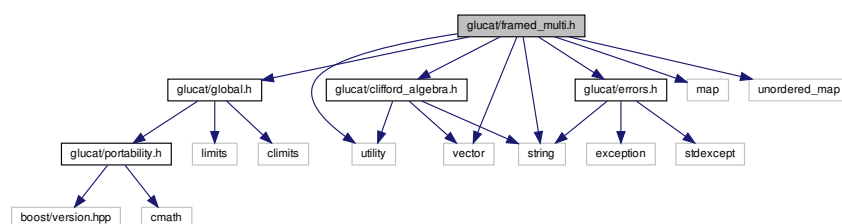
## 7.5 glucat/framed\_multi.h File Reference

```

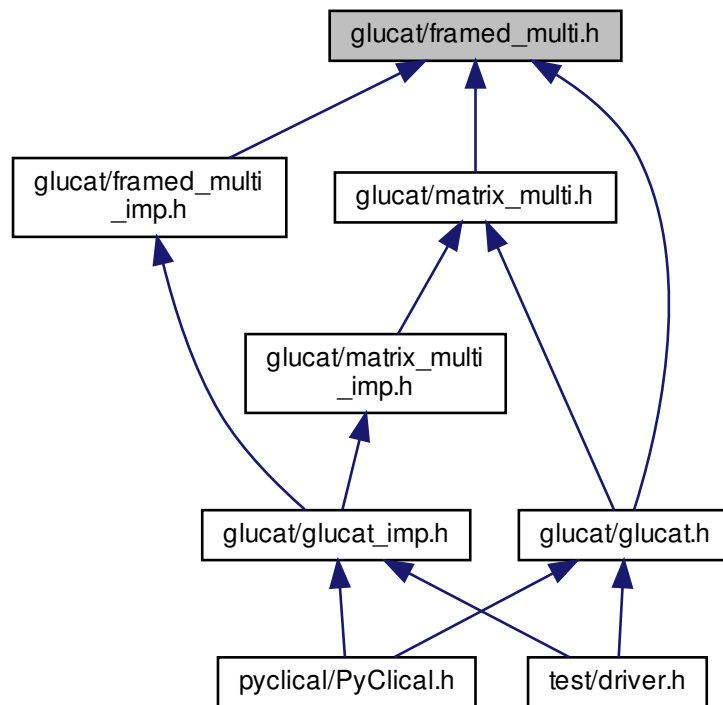
#include "glucat/global.h"
#include "glucat/errors.h"
#include "glucat/clifford_algebra.h"
#include <string>
#include <utility>
#include <map>
#include <vector>
#include <unordered_map>

```

Include dependency graph for `framed_multi.h`:



This graph shows which files directly or indirectly include this file:



## Classes

- class [glucat::framed\\_multi< Scalar\\_T, LO, HI >](#)  
A *framed\_multi<Scalar\_T,LO,HI>* is a framed approximation to a multivector.
- class [glucat::matrix\\_multi< Scalar\\_T, LO, HI >](#)  
A *matrix\_multi<Scalar\_T,LO,HI>* is a matrix approximation to a multivector.
- class [glucat::index\\_set\\_hash< LO, HI >](#)
- class [glucat::framed\\_multi< Scalar\\_T, LO, HI >](#)  
A *framed\_multi<Scalar\_T,LO,HI>* is a framed approximation to a multivector.
- class [glucat::framed\\_multi< Scalar\\_T, LO, HI >::hash\\_size\\_t](#)
- class [glucat::framed\\_multi< Scalar\\_T, LO, HI >::var\\_term](#)  
Variable term.
- struct [std::numeric\\_limits< glucat::framed\\_multi< Scalar\\_T, LO, HI > >](#)  
Numeric limits for *framed\_multi* inherit limits for the corresponding scalar type.

## Namespaces

- [glucat](#)
- [std](#)

## Macros

- `#define _GLUCAT_MAP_IS_HASH`

## Functions

- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const framed_multi< Scalar_T, LO, HI > glucat::operator\* (const framed_multi< Scalar_T, LO, HI > &lhs,`  
`const framed_multi< Scalar_T, LO, HI > &rhs)`  
*Geometric product.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const framed_multi< Scalar_T, LO, HI > glucat::operator^ (const framed_multi< Scalar_T, LO, HI > &lhs,`  
`const framed_multi< Scalar_T, LO, HI > &rhs)`  
*Outer product.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const framed_multi< Scalar_T, LO, HI > glucat::operator & (const framed_multi< Scalar_T, LO, HI > &lhs,`  
`const framed_multi< Scalar_T, LO, HI > &rhs)`  
*Inner product.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const framed_multi< Scalar_T, LO, HI > glucat::operator% (const framed_multi< Scalar_T, LO, HI > &lhs,`  
`const framed_multi< Scalar_T, LO, HI > &rhs)`  
*Left contraction.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`Scalar_T glucat::star (const framed_multi< Scalar_T, LO, HI > &lhs, const framed_multi< Scalar_T, LO, HI`  
`> &rhs)`  
*Hestenes scalar product.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const framed_multi< Scalar_T, LO, HI > glucat::operator/ (const framed_multi< Scalar_T, LO, HI > &lhs,`  
`const framed_multi< Scalar_T, LO, HI > &rhs)`  
*Geometric quotient.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const framed_multi< Scalar_T, LO, HI > glucat::operator| (const framed_multi< Scalar_T, LO, HI > &lhs,`  
`const framed_multi< Scalar_T, LO, HI > &rhs)`  
*Transformation via twisted adjoint action.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`std::istream & glucat::operator>> (std::istream &s, framed_multi< Scalar_T, LO, HI > &val)`  
*Read multivector from input.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`std::ostream & glucat::operator<< (std::ostream &os, const framed_multi< Scalar_T, LO, HI > &val)`  
*Write multivector to output.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`std::ostream & glucat::operator<< (std::ostream &os, const std::pair< const index_set< LO, HI >, Scalar_T`  
`> &term)`  
*Write term to output.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const framed_multi< Scalar_T, LO, HI > glucat::exp (const framed_multi< Scalar_T, LO, HI > &val)`  
*Exponential of multivector.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`static Scalar_T glucat::crd\_of\_mult (const std::pair< const index_set< LO, HI >, Scalar_T > &lhs, const`  
`std::pair< const index_set< LO, HI >, Scalar_T > &rhs)`  
*Coordinate of product of terms.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const std::pair< const index_set< LO, HI >, Scalar_T > glucat::operator\* (const std::pair< const index_↵`  
`set< LO, HI >, Scalar_T > &lhs, const std::pair< const index_set< LO, HI >, Scalar_T > &rhs)`

*Product of terms.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const framed_multi< Scalar_T, LO, HI > glucat::sqrt (const framed_multi< Scalar_T, LO, HI > &val, const framed_multi< Scalar_T, LO, HI > &i, bool prechecked)`

*Square root of multivector with specified complexifier.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const framed_multi< Scalar_T, LO, HI > glucat::log (const framed_multi< Scalar_T, LO, HI > &val, const framed_multi< Scalar_T, LO, HI > &i, bool prechecked)`

*Natural logarithm of multivector with specified complexifier.*

## 7.5.1 Macro Definition Documentation

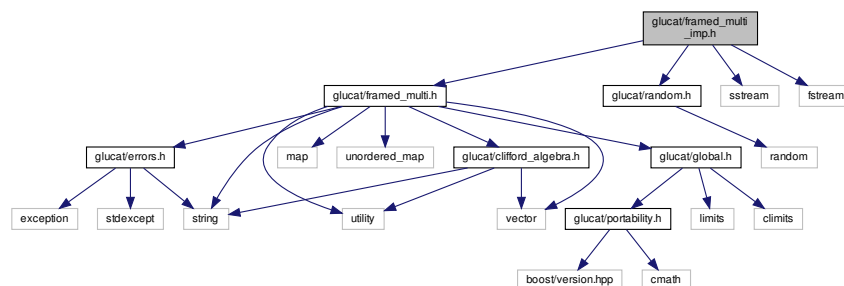
### 7.5.1.1 \_GLUCAT\_MAP\_IS\_HASH

```
#define _GLUCAT_MAP_IS_HASH
```

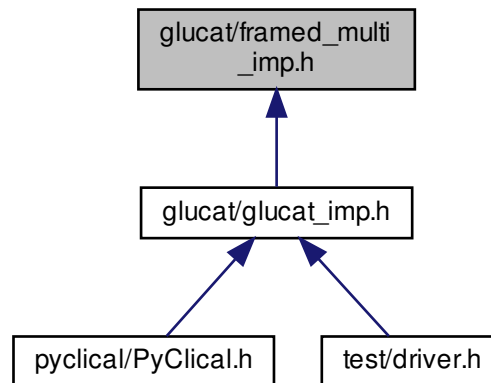
Definition at line 55 of file framed\_multi.h.

## 7.6 glucat/framed\_multi\_imp.h File Reference

```
#include "glucat/framed_multi.h"
#include "glucat/random.h"
#include <sstream>
#include <fstream>
Include dependency graph for framed_multi_imp.h:
```



This graph shows which files directly or indirectly include this file:



## Classes

- class [glucat::sorted\\_range< Map\\_T, Sorted\\_Map\\_T >](#)  
*Sorted range for use with output.*
- class [glucat::sorted\\_range< Sorted\\_Map\\_T, Sorted\\_Map\\_T >](#)

## Namespaces

- [glucat](#)

## Macros

- [#define \\_GLUCAT\\_HASH\\_N\(x\)](#)
- [#define \\_GLUCAT\\_HASH\\_SIZE\\_T\(x\)](#)

## Functions

- [template<typename Scalar\\_T , const index\\_t LO, const index\\_t HI>](#)  
[const framed\\_multi< Scalar\\_T, LO, HI >](#) [glucat::operator\\*](#) ([const framed\\_multi< Scalar\\_T, LO, HI >](#) &lhs,  
[const framed\\_multi< Scalar\\_T, LO, HI >](#) &rhs)  
*Geometric product.*
- [template<typename Scalar\\_T , const index\\_t LO, const index\\_t HI>](#)  
[const framed\\_multi< Scalar\\_T, LO, HI >](#) [glucat::operator^](#) ([const framed\\_multi< Scalar\\_T, LO, HI >](#) &lhs,  
[const framed\\_multi< Scalar\\_T, LO, HI >](#) &rhs)  
*Outer product.*
- [template<typename Scalar\\_T , const index\\_t LO, const index\\_t HI>](#)  
[const framed\\_multi< Scalar\\_T, LO, HI >](#) [glucat::operator &](#) ([const framed\\_multi< Scalar\\_T, LO, HI >](#) &lhs,  
[const framed\\_multi< Scalar\\_T, LO, HI >](#) &rhs)  
*Inner product.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const framed_multi< Scalar_T, LO, HI > glucat::operator% (const framed_multi< Scalar_T, LO, HI > &lhs,`  
`const framed_multi< Scalar_T, LO, HI > &rhs)`  
*Left contraction.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`Scalar_T glucat::star (const framed_multi< Scalar_T, LO, HI > &lhs, const framed_multi< Scalar_T, LO, HI`  
`> &rhs)`  
*Hestenes scalar product.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const framed_multi< Scalar_T, LO, HI > glucat::operator/ (const framed_multi< Scalar_T, LO, HI > &lhs,`  
`const framed_multi< Scalar_T, LO, HI > &rhs)`  
*Geometric quotient.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const framed_multi< Scalar_T, LO, HI > glucat::operator| (const framed_multi< Scalar_T, LO, HI > &lhs,`  
`const framed_multi< Scalar_T, LO, HI > &rhs)`  
*Transformation via twisted adjoint action.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`std::ostream & glucat::operator<< (std::ostream &os, const framed_multi< Scalar_T, LO, HI > &val)`  
*Write multivector to output.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`std::ostream & glucat::operator<< (std::ostream &os, const std::pair< const index_set< LO, HI >, Scalar_T`  
`> &term)`  
*Write term to output.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`std::istream & glucat::operator>> (std::istream &s, framed_multi< Scalar_T, LO, HI > &val)`  
*Read multivector from input.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`static Scalar_T glucat::crd_of_mult (const std::pair< const index_set< LO, HI >, Scalar_T > &lhs, const`  
`std::pair< const index_set< LO, HI >, Scalar_T > &rhs)`  
*Coordinate of product of terms.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const std::pair< const index_set< LO, HI >, Scalar_T > glucat::operator* (const std::pair< const index_↔`  
`set< LO, HI >, Scalar_T > &lhs, const std::pair< const index_set< LO, HI >, Scalar_T > &rhs)`  
*Product of terms.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const framed_multi< Scalar_T, LO, HI > glucat::sqrt (const framed_multi< Scalar_T, LO, HI > &val, const`  
`framed_multi< Scalar_T, LO, HI > &i, bool prechecked)`  
*Square root of multivector with specified complexifier.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const framed_multi< Scalar_T, LO, HI > glucat::exp (const framed_multi< Scalar_T, LO, HI > &val)`  
*Exponential of multivector.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const framed_multi< Scalar_T, LO, HI > glucat::log (const framed_multi< Scalar_T, LO, HI > &val, const`  
`framed_multi< Scalar_T, LO, HI > &i, bool prechecked)`  
*Natural logarithm of multivector with specified complexifier.*

### 7.6.1 Macro Definition Documentation

### 7.6.1.1 \_GLUCAT\_HASH\_N

```
#define _GLUCAT_HASH_N(  
    x )
```

Definition at line 60 of file framed\_multi\_imp.h.

### 7.6.1.2 \_GLUCAT\_HASH\_SIZE\_T

```
#define _GLUCAT_HASH_SIZE_T(  
    x )
```

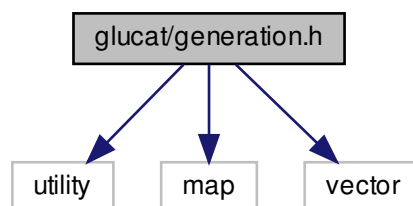
Definition at line 61 of file framed\_multi\_imp.h.

Referenced by `glucat::framed_multi< Scalar_T, LO, HI >::framed_multi()`, `glucat::operator &()`, `glucat::operator%()`, `glucat::operator*()`, and `glucat::operator^()`.

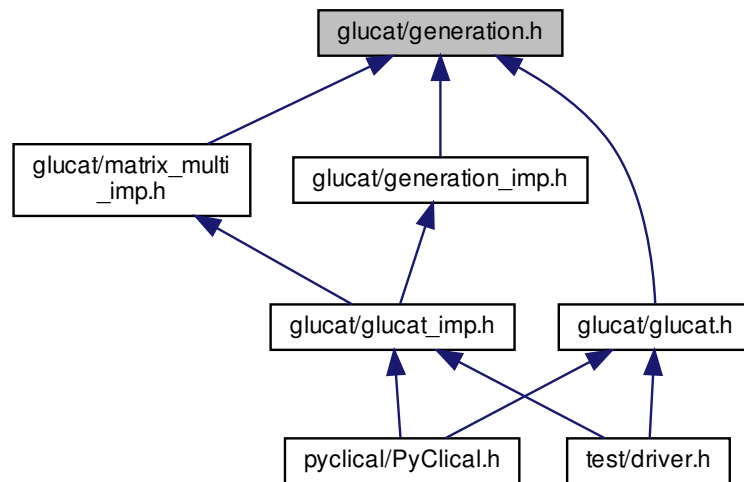
## 7.7 glucat/generation.h File Reference

```
#include <utility>  
#include <map>  
#include <vector>
```

Include dependency graph for generation.h:



This graph shows which files directly or indirectly include this file:



## Classes

- class [glucat::gen::generator\\_table< Matrix\\_T >](#)  
*Table of generators for specific signatures.*

## Namespaces

- [glucat](#)
- [glucat::gen](#)

## Typedefs

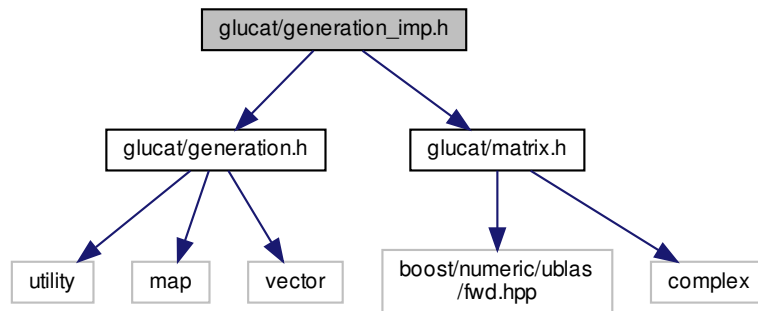
- typedef std::pair< index\_t, index\_t > [glucat::gen::signature\\_t](#)  
*A signature is a pair of indices, p, q, with p == frame.max(), q == -frame.min()*

## Variables

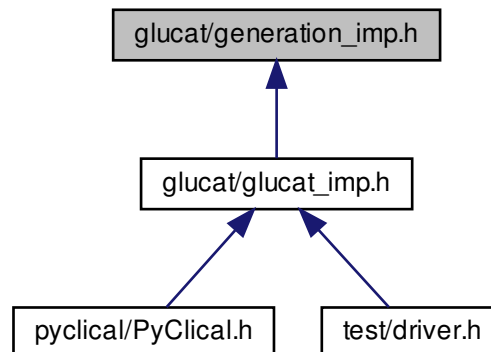
- static const index\_t [glucat::gen::offset\\_to\\_super](#) [] = {0,-1, 0,-1,-2, 3, 2, 1}  
*Offsets between the current signature and that of the real superalgebra.*

## 7.8 glucat/generation\_imp.h File Reference

```
#include "glucat/generation.h"
#include "glucat/matrix.h"
Include dependency graph for generation_imp.h:
```



This graph shows which files directly or indirectly include this file:



### Namespaces

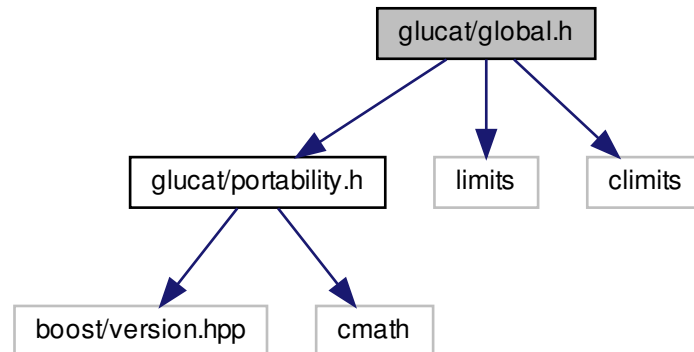
- [glucat](#)
- [glucat::gen](#)

## 7.9 glucat/global.h File Reference

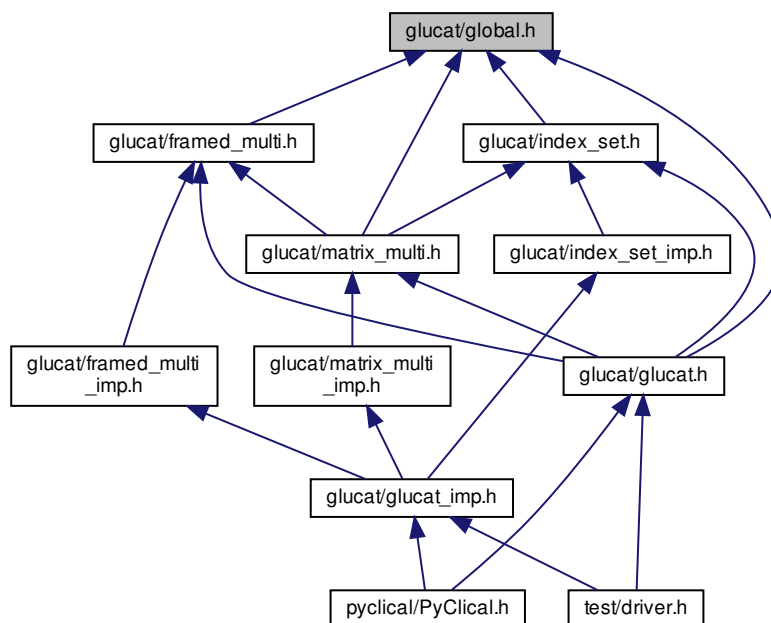
```
#include "glucat/portability.h"
#include <limits>
```

```
#include <climits>
```

Include dependency graph for global.h:



This graph shows which files directly or indirectly include this file:



## Classes

- struct `glucat::CTAssertion< bool >`  
Compile time assertion.
- struct `glucat::CTAssertion< true >`

- class `glucat::compare_types< LHS_T, RHS_T >`  
*Type comparison.*
- class `glucat::compare_types< T, T >`
- class `glucat::bool_to_type< truth_value >`  
*Bool to type.*
- struct `glucat::tuning< Mult_Matrix_Threshold, Div_Max_Steps, Sqrt_Max_Steps, Log_Max_Outer_Steps, Log_Max_Inner_Steps >`  
*Tuning policy.*

## Namespaces

- `glucat`

## Macros

- `#define _GLUCAT_CTAssert(expr, msg) namespace { struct msg { glucat::CTAssertion<(expr)> ERROR↵  
_##msg; }; }`

## Typedefs

- typedef int `glucat::index_t`  
*Size of index\_t should be enough to represent LO, HI.*
- typedef unsigned long `glucat::set_value_t`  
*Size of set\_value\_t should be enough to contain index\_set<LO,HI>*

## Enumerations

- enum `glucat::precision_t` { `glucat::precision_demoted`, `glucat::precision_same`, `glucat::precision_promoted` }  
*Precision policy.*

## Functions

- `glucat::_GLUCAT_CTAssert` (std::numeric\_limits< unsigned char >::radix==2, CannotDetermineBitsPer↵  
Char) const index\_t BITS\_PER\_CHAR  
*If radix of unsigned char is not 2, we can't easily determine number of bits from sizeof.*
- `glucat::_GLUCAT_CTAssert` (\_GLUCAT\_BITS\_PER\_ULONG==BITS\_PER\_SET\_VALUE, BitsPerULong↵  
DoesNotMatchSetValueT) const index\_t DEFAULT\_LO  
*Default lowest index in an index set.*
- template<typename LHS\_T, typename RHS\_T >  
LHS\_T `glucat::pos_mod` (LHS\_T lhs, RHS\_T rhs)  
*Modulo function which works reliably for lhs < 0.*

## Variables

- const double `glucat::MS_PER_S` = 1000.0  
*Timing constant: deprecated here - moved to [test/timing.h](#).*
- const index\_t `glucat::BITS_PER_SET_VALUE` = std::numeric\_limits<set\_value\_t>::digits  
*Number of bits in set\_value\_t.*
- const index\_t `glucat::DEFAULT_HI` = index\_t(BITS\_PER\_SET\_VALUE / 2)  
*Default highest index in an index set.*
- const double `glucat::DEFAULT_TRUNCATION` = std::numeric\_limits<float>::epsilon()  
*Default for truncation.*
- const unsigned int `glucat::DEFAULT_Mult_Matrix_Threshold` = 8
- const unsigned int `glucat::DEFAULT_Div_Max_Steps` = 4
- const unsigned int `glucat::DEFAULT_Sqrt_Max_Steps` = 256
- const unsigned int `glucat::DEFAULT_Log_Max_Outer_Steps` = 256
- const unsigned int `glucat::DEFAULT_Log_Max_Inner_Steps` = 32
- const unsigned int `glucat::DEFAULT_Basis_Max_Count` = 12
- const unsigned int `glucat::DEFAULT_Fast_Size_Threshold` = 1 << 6
- const unsigned int `glucat::DEFAULT_Inv_Fast_Dim_Threshold` = 1 << 3
- const unsigned int `glucat::DEFAULT_Products_Size_Threshold` = 1 << 22
- const precision\_t `glucat::DEFAULT_Function_Precision` = precision\_same

## 7.9.1 Macro Definition Documentation

### 7.9.1.1 \_GLUCAT\_CTAssert

```
#define _GLUCAT_CTAssert(  
    expr,  
    msg ) namespace { struct msg { glucat::CTAssertion<(expr)> ERROR_##msg; }; }
```

Definition at line 48 of file global.h.

## 7.10 glucat/glucat.h File Reference

```
#include "glucat/portability.h"  
#include "glucat/global.h"  
#include "glucat/errors.h"  
#include "glucat/index_set.h"  
#include "glucat/scalar.h"  
#include "glucat/long_double.h"  
#include "glucat/qd.h"  
#include "glucat/clifford_algebra.h"  
#include "glucat/framed_multi.h"  
#include "glucat/generation.h"  
#include "glucat/matrix.h"
```



## Macros

- `#define GLUCAT_HAVE_INTTYPES_H 1`
- `#define GLUCAT_HAVE_MEMORY_H 1`
- `#define GLUCAT_HAVE_STDINT_H 1`
- `#define GLUCAT_HAVE_STDLIB_H 1`
- `#define GLUCAT_HAVE_STRINGS_H 1`
- `#define GLUCAT_HAVE_STRING_H 1`
- `#define GLUCAT_HAVE_SYS_STAT_H 1`
- `#define GLUCAT_HAVE_SYS_TYPES_H 1`
- `#define GLUCAT_HAVE_UNISTD_H 1`
- `#define GLUCAT_PACKAGE "glucat"`
- `#define GLUCAT_PACKAGE_BUGREPORT ""`
- `#define GLUCAT_PACKAGE_NAME "glucat"`
- `#define GLUCAT_PACKAGE_STRING "glucat 0.8.2"`
- `#define GLUCAT_PACKAGE_TARNAME "glucat"`
- `#define GLUCAT_PACKAGE_URL ""`
- `#define GLUCAT_PACKAGE_VERSION "0.8.2"`
- `#define GLUCAT_STDC_HEADERS 1`
- `#define GLUCAT_VERSION "0.8.2"`

### 7.11.1 Macro Definition Documentation

#### 7.11.1.1 GLUCAT\_HAVE\_INTTYPES\_H

```
#define GLUCAT_HAVE_INTTYPES_H 1
```

Definition at line 10 of file `glucat_config.h`.

#### 7.11.1.2 GLUCAT\_HAVE\_MEMORY\_H

```
#define GLUCAT_HAVE_MEMORY_H 1
```

Definition at line 18 of file `glucat_config.h`.

#### 7.11.1.3 GLUCAT\_HAVE\_STDINT\_H

```
#define GLUCAT_HAVE_STDINT_H 1
```

Definition at line 23 of file `glucat_config.h`.

#### 7.11.1.4 GLUCAT\_HAVE\_STDLIB\_H

```
#define GLUCAT_HAVE_STDLIB_H 1
```

Definition at line 28 of file `glucat_config.h`.

#### 7.11.1.5 GLUCAT\_HAVE\_STRING\_H

```
#define GLUCAT_HAVE_STRING_H 1
```

Definition at line 38 of file `glucat_config.h`.

#### 7.11.1.6 GLUCAT\_HAVE\_STRINGS\_H

```
#define GLUCAT_HAVE_STRINGS_H 1
```

Definition at line 33 of file `glucat_config.h`.

#### 7.11.1.7 GLUCAT\_HAVE\_SYS\_STAT\_H

```
#define GLUCAT_HAVE_SYS_STAT_H 1
```

Definition at line 43 of file `glucat_config.h`.

#### 7.11.1.8 GLUCAT\_HAVE\_SYS\_TYPES\_H

```
#define GLUCAT_HAVE_SYS_TYPES_H 1
```

Definition at line 48 of file `glucat_config.h`.

#### 7.11.1.9 GLUCAT\_HAVE\_UNISTD\_H

```
#define GLUCAT_HAVE_UNISTD_H 1
```

Definition at line 53 of file `glucat_config.h`.

#### 7.11.1.10 GLUCAT\_PACKAGE

```
#define GLUCAT_PACKAGE "glucat"
```

Definition at line 58 of file glucat\_config.h.

#### 7.11.1.11 GLUCAT\_PACKAGE\_BUGREPORT

```
#define GLUCAT_PACKAGE_BUGREPORT ""
```

Definition at line 63 of file glucat\_config.h.

#### 7.11.1.12 GLUCAT\_PACKAGE\_NAME

```
#define GLUCAT_PACKAGE_NAME "glucat"
```

Definition at line 68 of file glucat\_config.h.

Referenced by glucat::control\_t::control\_t().

#### 7.11.1.13 GLUCAT\_PACKAGE\_STRING

```
#define GLUCAT_PACKAGE_STRING "glucat 0.8.2"
```

Definition at line 73 of file glucat\_config.h.

#### 7.11.1.14 GLUCAT\_PACKAGE\_TARNAME

```
#define GLUCAT_PACKAGE_TARNAME "glucat"
```

Definition at line 78 of file glucat\_config.h.

#### 7.11.1.15 GLUCAT\_PACKAGE\_URL

```
#define GLUCAT_PACKAGE_URL ""
```

Definition at line 83 of file glucat\_config.h.

#### 7.11.1.16 GLUCAT\_PACKAGE\_VERSION

```
#define GLUCAT_PACKAGE_VERSION "0.8.2"
```

Definition at line 88 of file `glucat_config.h`.

#### 7.11.1.17 GLUCAT\_STDC\_HEADERS

```
#define GLUCAT_STDC_HEADERS 1
```

Definition at line 93 of file `glucat_config.h`.

#### 7.11.1.18 GLUCAT\_VERSION

```
#define GLUCAT_VERSION "0.8.2"
```

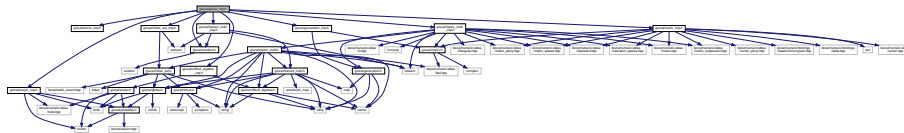
Definition at line 98 of file `glucat_config.h`.

Referenced by `glucat::control_t::control_t()`.

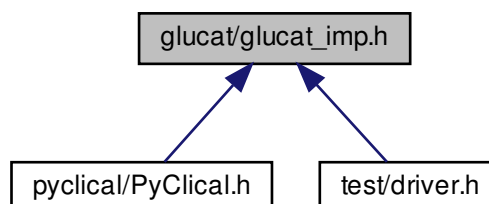
## 7.12 glucat/glucat\_imp.h File Reference

```
#include "glucat/errors_imp.h"
#include "glucat/index_set_imp.h"
#include "glucat/scalar_imp.h"
#include "glucat/clifford_algebra_imp.h"
#include "glucat/random.h"
#include "glucat/framed_multi_imp.h"
#include "glucat/matrix_imp.h"
#include "glucat/generation_imp.h"
#include "glucat/matrix_multi_imp.h"
```

Include dependency graph for `glucat_imp.h`:



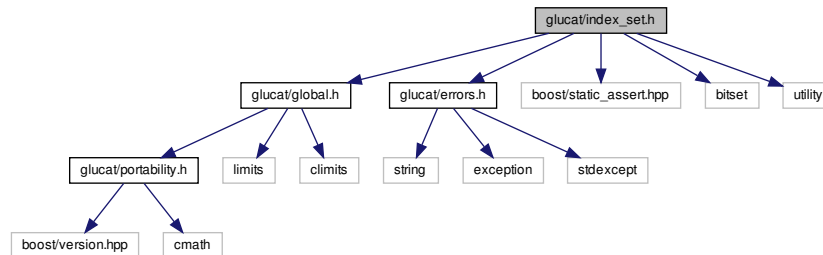
This graph shows which files directly or indirectly include this file:



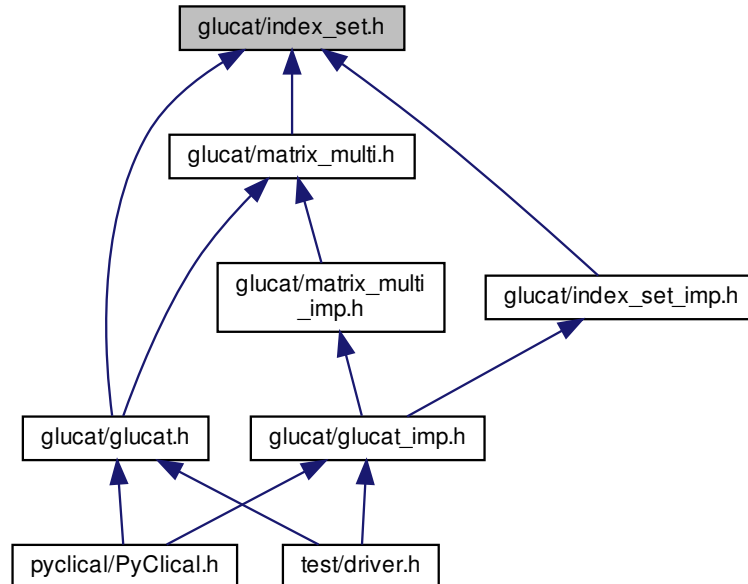
## 7.13 glucat/index\_set.h File Reference

```
#include "glucat/global.h"
#include "glucat/errors.h"
#include <boost/static_assert.hpp>
#include <bitset>
#include <utility>
```

Include dependency graph for index\_set.h:



This graph shows which files directly or indirectly include this file:



### Classes

- class [glucat::index\\_set< LO, HI >](#)

*Index set class based on `std::bitset<>` in Gnu standard C++ library.*

- class [glucat::index\\_set< LO, HI >](#)  
*Index set class based on `std::bitset<>` in Gnu standard C++ library.*
- class [glucat::index\\_set< LO, HI >::reference](#)  
*Index set member reference.*

## Namespaces

- [glucat](#)

## Functions

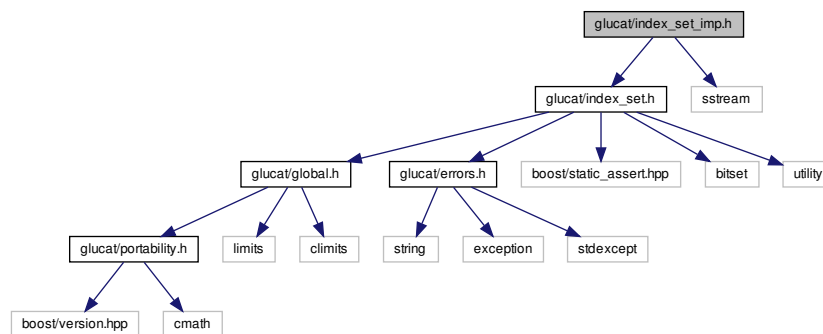
- `template<const index_t LO, const index_t HI>`  
`const index_set< LO, HI > glucat::operator^ (const index_set< LO, HI > &lhs, const index_set< LO, HI > &rhs)`  
*Symmetric set difference: exclusive or.*
- `template<const index_t LO, const index_t HI>`  
`const index_set< LO, HI > glucat::operator & (const index_set< LO, HI > &lhs, const index_set< LO, HI > &rhs)`  
*Set intersection: and.*
- `template<const index_t LO, const index_t HI>`  
`const index_set< LO, HI > glucat::operator| (const index_set< LO, HI > &lhs, const index_set< LO, HI > &rhs)`  
*Set union: or.*
- `template<const index_t LO, const index_t HI>`  
`int glucat::compare (const index_set< LO, HI > &a, const index_set< LO, HI > &b)`  
*"lexicographic compare" eg. {3,4,5} is less than {3,7,8}*
- `glucat::GLUCAT\_CTAssert (sizeof(set_value_t) >=sizeof(std::bitset< DEFAULT_HI-DEFAULT_LO >), Default_index_set_too_big_for_value) template< const index_t LO`  
*Size of `set_value_t` should be enough to contain `bitset<DEFAULT_HI-DEFAULT_LO>`*
- `const index_t HI std::ostream & glucat::operator<< (std::ostream &os, const index_set< LO, HI > &ist)`  
*Write out index set.*
- `template<const index_t LO, const index_t HI>`  
`std::istream & glucat::operator>> (std::istream &s, index_set< LO, HI > &ist)`  
*Read in index set.*
- `int glucat::sign\_of\_square (index_t j)`  
*Square of generator {j}.*
- `template<const index_t LO, const index_t HI>`  
`index_t glucat::min\_neg (const index_set< LO, HI > &ist)`  
*Minimum negative index, or 0 if none.*
- `template<const index_t LO, const index_t HI>`  
`index_t glucat::max\_pos (const index_set< LO, HI > &ist)`  
*Maximum positive index, or 0 if none.*

## 7.14 glucat/index\_set\_imp.h File Reference

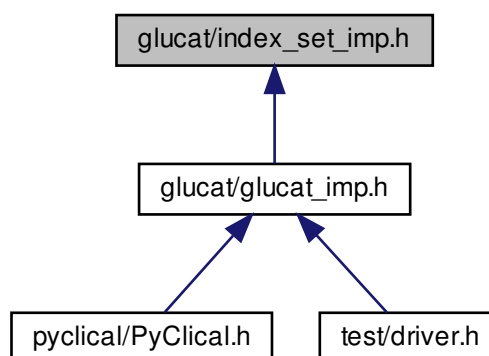
```
#include "glucat/index_set.h"
```

```
#include <sstream>
```

Include dependency graph for index\_set\_imp.h:



This graph shows which files directly or indirectly include this file:



### Namespaces

- [glucat](#)

### Functions

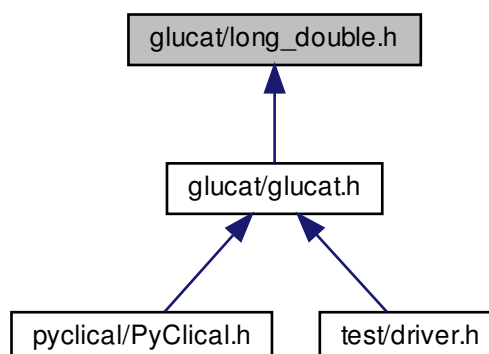
- `template<const index_t LO, const index_t HI>`  
`const index_set< LO, HI > glucat::operator^ (const index_set< LO, HI > &lhs, const index_set< LO, HI > &rhs)`

*Symmetric set difference: exclusive or.*

- `template<const index_t LO, const index_t HI>`  
`const index_set< LO, HI > glucat::operator & (const index_set< LO, HI > &lhs, const index_set< LO, HI > &rhs)`  
*Set intersection: and.*
- `template<const index_t LO, const index_t HI>`  
`const index_set< LO, HI > glucat::operator | (const index_set< LO, HI > &lhs, const index_set< LO, HI > &rhs)`  
*Set union: or.*
- `template<const index_t LO, const index_t HI>`  
`int glucat::compare (const index_set< LO, HI > &a, const index_set< LO, HI > &b)`  
*"lexicographic compare" eg. {3,4,5} is less than {3,7,8}*
- `const index_t HI std::ostream & glucat::operator << (std::ostream &os, const index_set< LO, HI > &ist)`  
*Write out index set.*
- `template<const index_t LO, const index_t HI>`  
`std::istream & glucat::operator >> (std::istream &s, index_set< LO, HI > &ist)`  
*Read in index set.*
- `static unsigned long glucat::inverse\_reversed\_gray (unsigned long x)`  
*Inverse reversed Gray code.*
- `static unsigned long glucat::inverse\_gray (unsigned long x)`  
*Inverse Gray code.*
- `int glucat::sign\_of\_square (index_t j)`  
*Square of generator {j}.*
- `template<const index_t LO, const index_t HI>`  
`index_t glucat::min\_neg (const index_set< LO, HI > &ist)`  
*Minimum negative index, or 0 if none.*
- `template<const index_t LO, const index_t HI>`  
`index_t glucat::max\_pos (const index_set< LO, HI > &ist)`  
*Maximum positive index, or 0 if none.*

## 7.15 glucat/long\_double.h File Reference

This graph shows which files directly or indirectly include this file:



## Classes

- struct `glucat::numeric_traits< Scalar_T >::demoted<>`  
*Demoted type for long double.*

## Namespaces

- `glucat`

## Variables

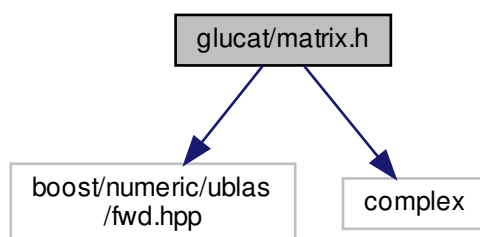
- static const long double `glucat::l_pi` = 3.1415926535897932384626433832795029L
- static const long double `glucat::l_ln2` = 0.6931471805599453094172321214581766L

## 7.16 glucat/matrix.h File Reference

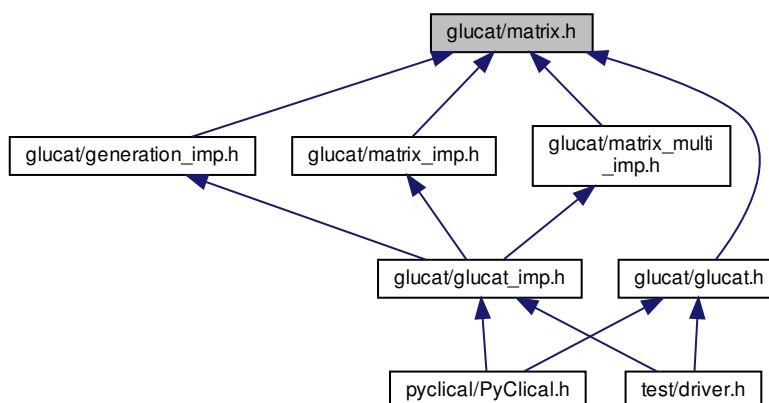
```
#include <boost/numeric/ublas/fwd.hpp>
```

```
#include <complex>
```

Include dependency graph for matrix.h:



This graph shows which files directly or indirectly include this file:



## Classes

- struct [glucat::matrix::eig\\_genus](#)< [Matrix\\_T](#) >  
*Structure containing classification of eigenvalues.*

## Namespaces

- [glucat](#)
- [glucat::matrix](#)

## Enumerations

- enum [glucat::matrix::eig\\_case\\_t](#) { [glucat::matrix::safe\\_eig\\_case](#), [glucat::matrix::negative\\_eig\\_case](#), [glucat::matrix::both\\_eig\\_case](#) }  
*Classification of eigenvalues of a matrix.*

## Functions

- template<typename LHS\_T , typename RHS\_T >  
const RHS\_T [glucat::matrix::kron](#) (const LHS\_T &lhs, const RHS\_T &rhs)  
*Kronecker tensor product of matrices - as per Matlab kron.*
- template<typename LHS\_T , typename RHS\_T >  
const RHS\_T [glucat::matrix::mono\\_kron](#) (const LHS\_T &lhs, const RHS\_T &rhs)  
*Sparse Kronecker tensor product of monomial matrices.*
- template<typename LHS\_T , typename RHS\_T >  
const RHS\_T [glucat::matrix::nork](#) (const LHS\_T &lhs, const RHS\_T &rhs, const bool mono=true)  
*Left inverse of Kronecker product.*
- template<typename LHS\_T , typename RHS\_T >  
const RHS\_T [glucat::matrix::signed\\_perm\\_nork](#) (const LHS\_T &lhs, const RHS\_T &rhs)  
*Left inverse of Kronecker product where lhs is a signed permutation matrix.*
- template<typename Matrix\_T >  
Matrix\_T::size\_type [glucat::matrix::nnz](#) (const Matrix\_T &m)  
*Number of non-zeros.*
- template<typename Matrix\_T >  
bool [glucat::matrix::isnan](#) (const Matrix\_T &m)  
*Not a Number.*
- template<typename Matrix\_T >  
const Matrix\_T [glucat::matrix::unit](#) (const typename Matrix\_T::size\_type n)  
*Unit matrix - as per Matlab eye.*
- template<typename LHS\_T , typename RHS\_T >  
const RHS\_T::expression\_type [glucat::matrix::mono\\_prod](#) (const ublas::matrix\_expression< LHS\_T > &lhs, const ublas::matrix\_expression< RHS\_T > &rhs)  
*Product of monomial matrices.*
- template<typename LHS\_T , typename RHS\_T >  
const RHS\_T::expression\_type [glucat::matrix::sparse\\_prod](#) (const ublas::matrix\_expression< LHS\_T > &lhs, const ublas::matrix\_expression< RHS\_T > &rhs)  
*Product of sparse matrices.*
- template<typename LHS\_T , typename RHS\_T >  
const RHS\_T::expression\_type [glucat::matrix::prod](#) (const ublas::matrix\_expression< LHS\_T > &lhs, const ublas::matrix\_expression< RHS\_T > &rhs)  
*Product of matrices.*

- `template<typename Scalar_T , typename LHS_T , typename RHS_T >`  
`Scalar_T glucat::matrix::inner (const LHS_T &lhs, const RHS_T &rhs)`  
*Inner product:  $\sum(x(i,j)*y(i,j))/x.nrows()$*
- `template<typename Matrix_T >`  
`Matrix_T::value_type glucat::matrix::norm_frob2 (const Matrix_T &val)`  
*Square of Frobenius norm.*
- `template<typename Matrix_T >`  
`Matrix_T::value_type glucat::matrix::trace (const Matrix_T &val)`  
*Matrix trace.*
- `template<typename Matrix_T >`  
`ublas::vector< std::complex< double > > glucat::matrix::eigenvalues (const Matrix_T &val)`  
*Eigenvalues of a matrix.*
- `template<typename Matrix_T >`  
`eig_genus< Matrix_T > glucat::matrix::classify_eigenvalues (const Matrix_T &val)`  
*Classify the eigenvalues of a matrix.*

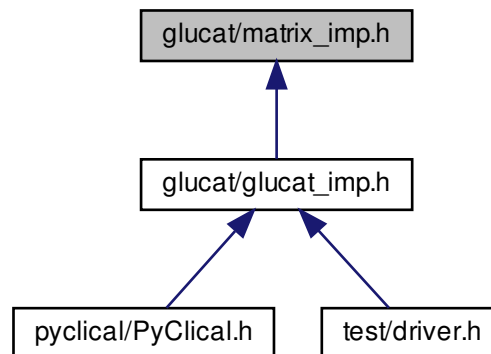
## 7.17 glucat/matrix\_imp.h File Reference

```
#include "glucat/matrix.h"
#include <boost/numeric/ublas/vector.hpp>
#include <boost/numeric/ublas/vector_proxy.hpp>
#include <boost/numeric/ublas/matrix.hpp>
#include <boost/numeric/ublas/matrix_expression.hpp>
#include <boost/numeric/ublas/matrix_proxy.hpp>
#include <boost/numeric/ublas/matrix_sparse.hpp>
#include <boost/numeric/ublas/operation.hpp>
#include <boost/numeric/ublas/operation_sparse.hpp>
#include <boost/numeric/bindings/lapack/driver/gees.hpp>
#include <boost/numeric/bindings/ublas.hpp>
#include <set>
```

Include dependency graph for matrix\_imp.h:



This graph shows which files directly or indirectly include this file:



## Namespaces

- [glucat](#)
- [glucat::matrix](#)

## Functions

- `template<typename LHS_T , typename RHS_T >`  
`const RHS_T glucat::matrix::kron (const LHS_T &lhs, const RHS_T &rhs)`  
*Kronecker tensor product of matrices - as per Matlab kron.*
- `template<typename LHS_T , typename RHS_T >`  
`const RHS_T glucat::matrix::mono\_kron (const LHS_T &lhs, const RHS_T &rhs)`  
*Sparse Kronecker tensor product of monomial matrices.*
- `template<typename LHS_T , typename RHS_T >`  
`void glucat::matrix::nork\_range (RHS_T &result, const typename LHS_T::const_iterator2 lhs_it2, const RHS_T &rhs, const typename RHS_T::size_type res_s1, const typename RHS_T::size_type res_s2)`  
*Utility routine for nork: calculate result for a range of indices.*
- `template<typename LHS_T , typename RHS_T >`  
`const RHS_T glucat::matrix::nork (const LHS_T &lhs, const RHS_T &rhs, const bool mono=true)`  
*Left inverse of Kronecker product.*
- `template<typename LHS_T , typename RHS_T >`  
`const RHS_T glucat::matrix::signed\_perm\_nork (const LHS_T &lhs, const RHS_T &rhs)`  
*Left inverse of Kronecker product where lhs is a signed permutation matrix.*
- `template<typename Matrix_T >`  
`Matrix_T::size_type glucat::matrix::nnz (const Matrix_T &m)`  
*Number of non-zeros.*
- `template<typename Matrix_T >`  
`bool glucat::matrix::isnans (const Matrix_T &m)`  
*Not a Number.*
- `template<typename Matrix_T >`  
`const Matrix_T glucat::matrix::unit (const typename Matrix_T::size_type n)`

- `template<typename LHS_T, typename RHS_T >`  
`const RHS_T::expression_type glucat::matrix::mono_prod (const ublas::matrix_expression< LHS_T > &lhs,`  
`const ublas::matrix_expression< RHS_T > &rhs)`

- `template<typename LHS_T, typename RHS_T >`  
`const RHS_T::expression_type glucat::matrix::sparse_prod (const ublas::matrix_expression< LHS_T >`  
`&lhs, const ublas::matrix_expression< RHS_T > &rhs)`

- `template<typename LHS_T, typename RHS_T >`  
`const RHS_T::expression_type glucatt::matrix::prod (const ublas::matrix_expression< LHS_T > &lhs, const`  
`ublas::matrix_expression< RHS_T > &rhs)`

- `template<typename Scalar_T, typename LHS_T, typename RHS_T >`  
`Scalar_T glucat::matrix::inner (const LHS_T &lhs, const RHS_T &rhs)`

- `template<typename Matrix_T >`  
`Matrix_T::value_type glucat::matrix::norm_frob2 (const Matrix_T &val)`

- `template<typename Matrix_T >`  
`Matrix_T::value_type glucat::matrix::trace (const Matrix_T &val)`

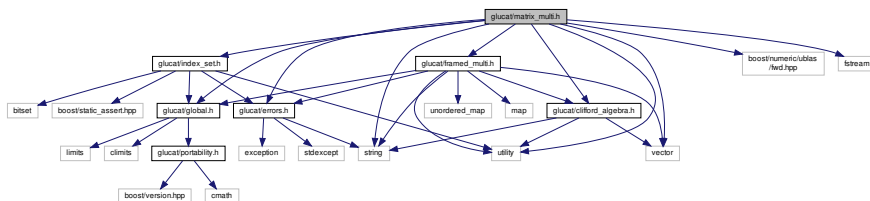
- `template<typename Matrix_T>`  
`static ublas::matrix< double, ublas::column_major> glucatt::matrix::to\_lapack (const Matrix_T &val)`

- `template<typename Matrix_T>`  
`ublas::vector< std::complex< double > > glucat::matrix::eigenvalues (const Matrix_T &val)`

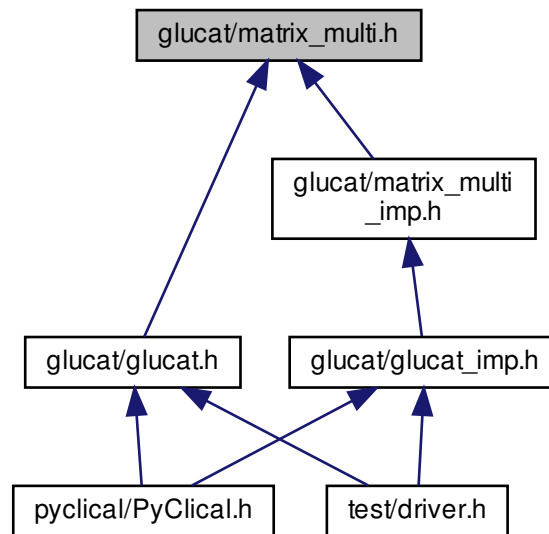
- `template<typename Matrix_T>`  
`eig_genus< Matrix_T> glucat::matrix::classify\_eigenvalues (const Matrix_T &val)`

## 7.18 glucat/matrix\_multi.h File Reference

```
#include "glucat/global.h"
#include "glucat/errors.h"
#include "glucat/index_set.h"
#include "glucat/clifford_algebra.h"
#include "glucat/framed_multi.h"
#include <boost/numeric/ublas/fwd.hpp>
#include <fstream>
#include <string>
#include <utility>
#include <vector>
```



This graph shows which files directly or indirectly include this file:



## Classes

- class [glucat::framed\\_multi< Scalar\\_T, LO, HI >](#)  
A *framed\_multi<Scalar\_T,LO,HI>* is a framed approximation to a multivector.
- class [glucat::matrix\\_multi< Scalar\\_T, LO, HI >](#)  
A *matrix\_multi<Scalar\_T,LO,HI>* is a matrix approximation to a multivector.
- class [glucat::matrix\\_multi< Scalar\\_T, LO, HI >](#)  
A *matrix\_multi<Scalar\_T,LO,HI>* is a matrix approximation to a multivector.
- struct [std::numeric\\_limits< glucat::matrix\\_multi< Scalar\\_T, LO, HI > >](#)  
Numeric limits for *matrix\_multi* inherit limits for the corresponding scalar type.

## Namespaces

- [glucat](#)
- [std](#)

## Functions

- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::operator\* (const matrix_multi< Scalar_T, LO, HI > &lhs,`  
`const matrix_multi< Scalar_T, LO, HI > &rhs)`  
*Geometric product.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::operator^ (const matrix_multi< Scalar_T, LO, HI > &lhs,`  
`const matrix_multi< Scalar_T, LO, HI > &rhs)`

*Outer product.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::operator & (const matrix_multi< Scalar_T, LO, HI > &lhs,`  
`const matrix_multi< Scalar_T, LO, HI > &rhs)`

*Inner product.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::operator% (const matrix_multi< Scalar_T, LO, HI > &lhs,`  
`const matrix_multi< Scalar_T, LO, HI > &rhs)`

*Left contraction.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`Scalar_T glucat::star (const matrix_multi< Scalar_T, LO, HI > &lhs, const matrix_multi< Scalar_T, LO, HI >`  
`&rhs)`

*Hestenes scalar product.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::operator/ (const matrix_multi< Scalar_T, LO, HI > &lhs, const`  
`matrix_multi< Scalar_T, LO, HI > &rhs)`

*Geometric quotient.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::operator| (const matrix_multi< Scalar_T, LO, HI > &lhs, const`  
`matrix_multi< Scalar_T, LO, HI > &rhs)`

*Transformation via twisted adjoint action.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`std::istream & glucat::operator>> (std::istream &s, matrix_multi< Scalar_T, LO, HI > &val)`

*Read multivector from input.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`std::ostream & glucat::operator<< (std::ostream &os, const matrix_multi< Scalar_T, LO, HI > &val)`

*Write multivector to output.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const index_set< LO, HI > glucat::reframe (const matrix_multi< Scalar_T, LO, HI > &lhs, const matrix_↔`  
`multi< Scalar_T, LO, HI > &rhs, matrix_multi< Scalar_T, LO, HI > &lhs_reframed, matrix_multi< Scalar_T,`  
`LO, HI > &rhs_reframed)`

*Find a common frame for operands of a binary operator.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::sqrt (const matrix_multi< Scalar_T, LO, HI > &val, const`  
`matrix_multi< Scalar_T, LO, HI > &i, bool prechecked)`

*Square root of multivector with specified complexifier.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::matrix_sqrt (const matrix_multi< Scalar_T, LO, HI > &val,`  
`const matrix_multi< Scalar_T, LO, HI > &i)`

*Square root of multivector with specified complexifier.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::log (const matrix_multi< Scalar_T, LO, HI > &val, const`  
`matrix_multi< Scalar_T, LO, HI > &i, bool prechecked)`

*Natural logarithm of multivector with specified complexifier.*

- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::matrix_log (const matrix_multi< Scalar_T, LO, HI > &val,`  
`const matrix_multi< Scalar_T, LO, HI > &i)`

*Natural logarithm of multivector with specified complexifier.*

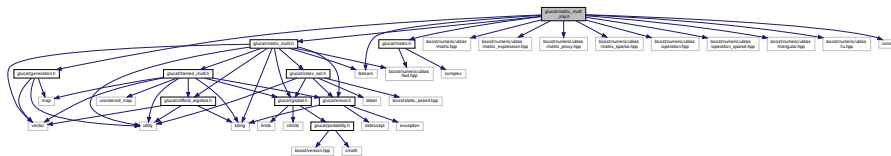
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::exp (const matrix_multi< Scalar_T, LO, HI > &val)`

*Exponential of multivector.*

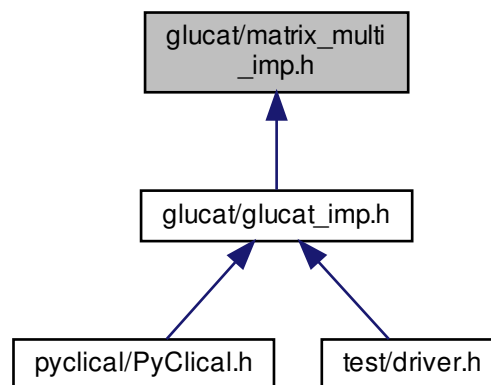
## 7.19 glucat/matrix\_multi\_imp.h File Reference

```
#include "glucat/matrix_multi.h"
#include "glucat/matrix.h"
#include "glucat/generation.h"
#include <boost/numeric/ublas/matrix.hpp>
#include <boost/numeric/ublas/matrix_expression.hpp>
#include <boost/numeric/ublas/matrix_proxy.hpp>
#include <boost/numeric/ublas/matrix_sparse.hpp>
#include <boost/numeric/ublas/operation.hpp>
#include <boost/numeric/ublas/operation_sparse.hpp>
#include <boost/numeric/ublas/triangular.hpp>
#include <boost/numeric/ublas/lu.hpp>
#include <fstream>
#include <iomanip>
```

Include dependency graph for matrix\_multi\_imp.h:



This graph shows which files directly or indirectly include this file:



### Classes

- class [glucat::basis\\_table< Scalar\\_T, LO, HI, Matrix\\_T >](#)  
*Table of basis elements used as a cache by basis\_element()*

### Namespaces

- [glucat](#)

## Functions

- `index_t glucat::offset_level` (const index\_t p, const index\_t q)  
*Determine the log2 dim corresponding to signature p, q.*
- `template<typename Matrix_Index_T, const index_t LO, const index_t HI>`  
`static Matrix_Index_T glucat::folded_dim` (const index\_set< LO, HI > &sub)  
*Determine the matrix dimension of the fold of a subalgebra.*
- `template<typename Scalar_T, const index_t LO, const index_t HI>`  
`const index_set< LO, HI > glucat::reframe` (const matrix\_multi< Scalar\_T, LO, HI > &lhs, const matrix\_multi< Scalar\_T, LO, HI > &rhs, matrix\_multi< Scalar\_T, LO, HI > &lhs\_reframed, matrix\_multi< Scalar\_T, LO, HI > &rhs\_reframed)  
*Find a common frame for operands of a binary operator.*
- `template<typename Scalar_T, const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::operator*` (const matrix\_multi< Scalar\_T, LO, HI > &lhs, const matrix\_multi< Scalar\_T, LO, HI > &rhs)  
*Geometric product.*
- `template<typename Scalar_T, const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::operator^` (const matrix\_multi< Scalar\_T, LO, HI > &lhs, const matrix\_multi< Scalar\_T, LO, HI > &rhs)  
*Outer product.*
- `template<typename Scalar_T, const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::operator &` (const matrix\_multi< Scalar\_T, LO, HI > &lhs, const matrix\_multi< Scalar\_T, LO, HI > &rhs)  
*Inner product.*
- `template<typename Scalar_T, const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::operator%` (const matrix\_multi< Scalar\_T, LO, HI > &lhs, const matrix\_multi< Scalar\_T, LO, HI > &rhs)  
*Left contraction.*
- `template<typename Scalar_T, const index_t LO, const index_t HI>`  
`Scalar_T glucat::star` (const matrix\_multi< Scalar\_T, LO, HI > &lhs, const matrix\_multi< Scalar\_T, LO, HI > &rhs)  
*Hestenes scalar product.*
- `template<typename Scalar_T, const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::operator/` (const matrix\_multi< Scalar\_T, LO, HI > &lhs, const matrix\_multi< Scalar\_T, LO, HI > &rhs)  
*Geometric quotient.*
- `template<typename Scalar_T, const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::operator|` (const matrix\_multi< Scalar\_T, LO, HI > &lhs, const matrix\_multi< Scalar\_T, LO, HI > &rhs)  
*Transformation via twisted adjoint action.*
- `template<typename Scalar_T, const index_t LO, const index_t HI>`  
`std::ostream & glucat::operator<<` (std::ostream &os, const matrix\_multi< Scalar\_T, LO, HI > &val)  
*Write multivector to output.*
- `template<typename Scalar_T, const index_t LO, const index_t HI>`  
`std::istream & glucat::operator>>` (std::istream &s, matrix\_multi< Scalar\_T, LO, HI > &val)  
*Read multivector from input.*
- `template<typename Multivector_T, typename Matrix_T, typename Basis_Matrix_T>`  
`static Multivector_T glucat::fast` (const Matrix\_T &X, index\_t level)  
*Inverse generalized Fast Fourier Transform.*
- `template<typename Scalar_T, const index_t LO, const index_t HI>`  
`static const matrix_multi< Scalar_T, LO, HI > glucat::pade_approx` (const int array\_size, const Scalar\_T a[], const Scalar\_T b[], const matrix\_multi< Scalar\_T, LO, HI > &X)  
*Pade' approximation.*

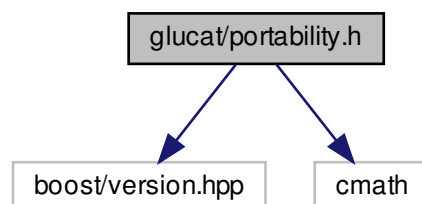
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`static void glucat::db\_step (matrix_multi< Scalar_T, LO, HI > &M, matrix_multi< Scalar_T, LO, HI > &Y)`  
*Single step of product form of Denman-Beavers square root iteration.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`static const matrix_multi< Scalar_T, LO, HI > glucat::db\_sqrt (const matrix_multi< Scalar_T, LO, HI > &val)`  
*Product form of Denman-Beavers square root iteration.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::sqrt (const matrix_multi< Scalar_T, LO, HI > &val, const matrix_multi< Scalar_T, LO, HI > &i, bool prechecked)`  
*Square root of multivector with specified complexifier.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::matrix\_sqrt (const matrix_multi< Scalar_T, LO, HI > &val, const matrix_multi< Scalar_T, LO, HI > &i)`  
*Square root of multivector with specified complexifier.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`static const matrix_multi< Scalar_T, LO, HI > glucat::pade\_log (const matrix_multi< Scalar_T, LO, HI > &val)`  
*Pade' approximation of log.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`static const matrix_multi< Scalar_T, LO, HI > glucat::cascade\_log (const matrix_multi< Scalar_T, LO, HI > &val)`  
*Incomplete square root cascade and Pade' approximation of log.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::log (const matrix_multi< Scalar_T, LO, HI > &val, const matrix_multi< Scalar_T, LO, HI > &i, bool prechecked)`  
*Natural logarithm of multivector with specified complexifier.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::matrix\_log (const matrix_multi< Scalar_T, LO, HI > &val, const matrix_multi< Scalar_T, LO, HI > &i)`  
*Natural logarithm of multivector with specified complexifier.*
- `template<typename Scalar_T , const index_t LO, const index_t HI>`  
`const matrix_multi< Scalar_T, LO, HI > glucat::exp (const matrix_multi< Scalar_T, LO, HI > &val)`  
*Exponential of multivector.*

## 7.20 `glucat/portability.h` File Reference

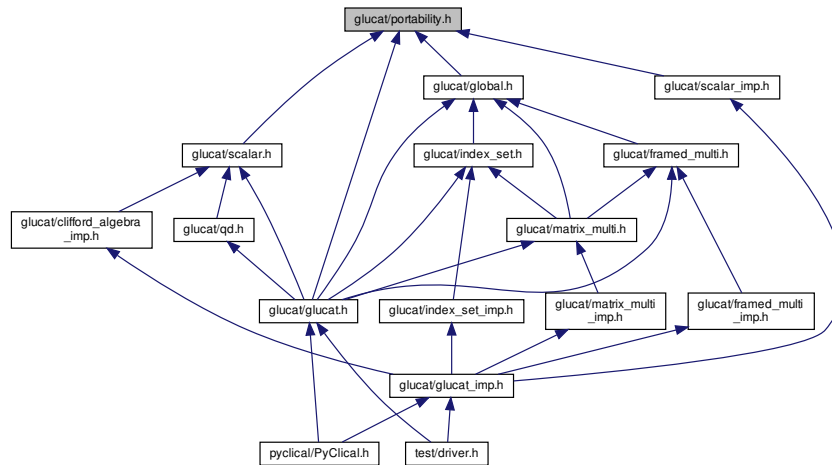
```
#include <boost/version.hpp>
```

```
#include <cmath>
```

Include dependency graph for `portability.h`:



This graph shows which files directly or indirectly include this file:



## Macros

- `#define _GLUCAT_ISNAN(x) (x != x)`
- `#define _GLUCAT_ISINF(x) (!_GLUCAT_ISNAN(x) && _GLUCAT_ISNAN(x-x))`
- `#define UBLAS_ABS abs`
- `#define UBLAS_SQRT sqrt`

## 7.20.1 Macro Definition Documentation

### 7.20.1.1 \_GLUCAT\_ISINF

```

#define _GLUCAT_ISINF(
    x ) ( !_GLUCAT_ISNAN(x) && _GLUCAT_ISNAN(x-x) )

```

Definition at line 48 of file portability.h.

Referenced by `glucat::numeric_traits< Scalar_T >::isInf()`.

### 7.20.1.2 \_GLUCAT\_ISNAN

```

#define _GLUCAT_ISNAN(
    x ) ( x != x )

```

Definition at line 47 of file portability.h.

Referenced by `glucat::numeric_traits< Scalar_T >::isNaN()`.

### 7.20.1.3 UBLAS\_ABS

```
#define UBLAS_ABS abs
```

Definition at line 56 of file portability.h.

Referenced by `glucat::numeric_traits< Scalar_T >::abs()`.

### 7.20.1.4 UBLAS\_SQRT

```
#define UBLAS_SQRT sqrt
```

Definition at line 57 of file portability.h.

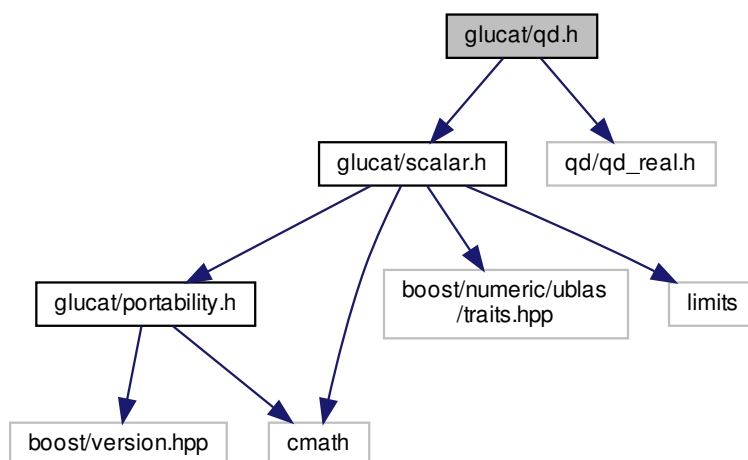
Referenced by `glucat::numeric_traits< Scalar_T >::sqrt()`.

## 7.21 glucat/qd.h File Reference

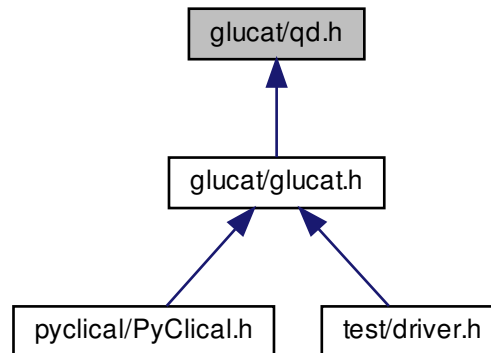
```
#include "glucat/scalar.h"
```

```
#include <qd/qd_real.h>
```

Include dependency graph for qd.h:



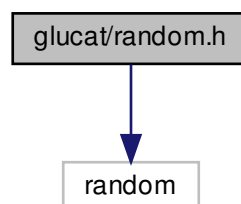
This graph shows which files directly or indirectly include this file:



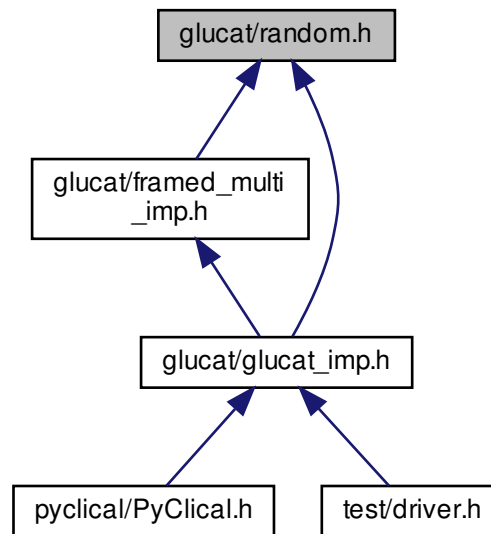
## 7.22 glucat/random.h File Reference

```
#include <random>
```

Include dependency graph for `random.h`:



This graph shows which files directly or indirectly include this file:



## Classes

- class [glucat::random\\_generator< Scalar\\_T >](#)  
*Random number generator with single instance per Scalar\_T.*

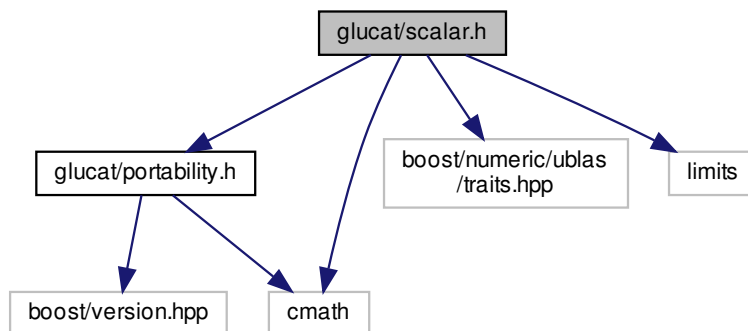
## Namespaces

- [glucat](#)

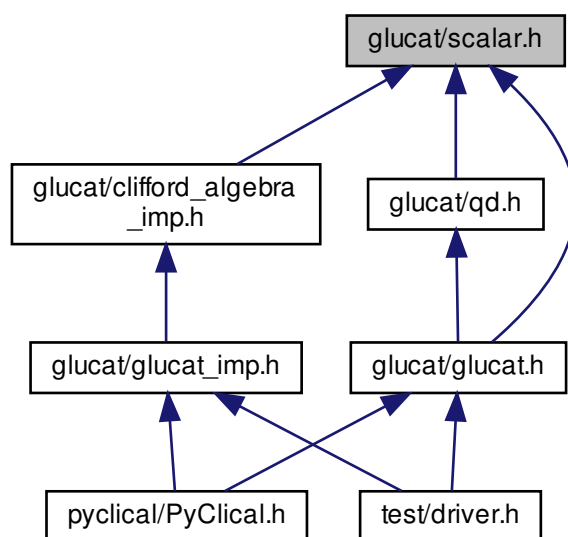
## 7.23 glucat/scalar.h File Reference

```
#include "glucat/portability.h"  
#include <boost/numeric/ublas/traits.hpp>  
#include <cmath>  
#include <limits>
```

Include dependency graph for scalar.h:



This graph shows which files directly or indirectly include this file:



## Classes

- class `glucat::numeric_traits< Scalar_T >`  
Extra traits which extend numeric limits.
- struct `glucat::numeric_traits< Scalar_T >::promoted`  
Promoted type.
- struct `glucat::numeric_traits< Scalar_T >::demoted<>`  
Demoted type for long double.

## Namespaces

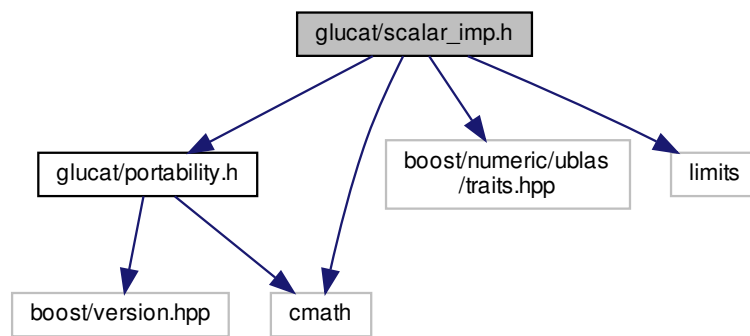
- [glucat](#)

## Functions

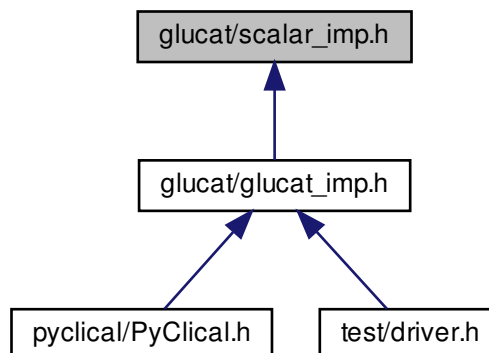
- `template<typename Scalar_T >`  
`Scalar_T glucat::log2 (const Scalar_T &x)`  
*Log base 2 of scalar.*

## 7.24 glucat/scalar\_imp.h File Reference

```
#include "glucat/portability.h"
#include <boost/numeric/ublas/traits.hpp>
#include <cmath>
#include <limits>
Include dependency graph for scalar_imp.h:
```



This graph shows which files directly or indirectly include this file:



## Namespaces

- [glucat](#)

## Functions

- `template<typename Scalar_T >`  
`numeric_traits< Scalar_T >::promoted::type` [glucat::to\\_promote](#) (const Scalar\_T &val)  
*Cast to promote.*
- `template<typename Scalar_T >`  
`numeric_traits< Scalar_T >::demoted::type` [glucat::to\\_demote](#) (const Scalar\_T &val)  
*Cast to demote.*

## 7.25 pyclical/glucat.pxd File Reference

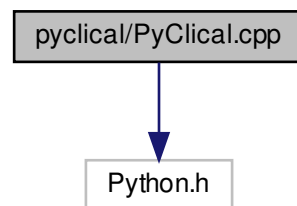
### Namespaces

- [glucat](#)

## 7.26 pyclical/PyClical.cpp File Reference

```
#include "Python.h"
```

Include dependency graph for PyClical.cpp:



## Macros

- `#define` [PY\\_SSIZE\\_T\\_CLEAN](#)

### 7.26.1 Macro Definition Documentation

### 7.26.1.1 PY\_SSIZE\_T\_CLEAN

```
#define PY_SSIZE_T_CLEAN
```

Definition at line 56 of file PyClical.cpp.

## 7.27 pyclical/PyClical.h File Reference

```
#include "glucat/glucat.h"
#include "glucat/glucat_imp.h"
#include <iostream>
#include <sstream>
#include <iomanip>
```

Include dependency graph for PyClical.h:



### Namespaces

- [cga3](#)  
*Definitions for 3D Conformal Geometric Algebra [DL].*

### Typedefs

- typedef [glucat::tuning](#)< [glucat::DEFAULT\\_Mult\\_Matrix\\_Threshold](#), [glucat::DEFAULT\\_Div\\_Max\\_Steps](#), [glucat::DEFAULT\\_Sqrt\\_Max\\_Steps](#), [glucat::DEFAULT\\_Log\\_Max\\_Outer\\_Steps](#), [glucat::DEFAULT\\_Log\\_Max\\_Inner\\_Steps](#), [glucat::DEFAULT\\_Basis\\_Max\\_Count](#), [glucat::DEFAULT\\_Fast\\_Size\\_Threshold](#), [glucat::DEFAULT\\_Inv\\_Fast\\_Dim\\_Threshold](#), [glucat::DEFAULT\\_Products\\_Size\\_Threshold](#), [glucat::precision\\_promoted](#) > [Tune\\_P](#)
- typedef std::string [String](#)
- typedef [index\\_set](#)< [lo\\_ndx](#), [hi\\_ndx](#) > [IndexSet](#)
- typedef double [scalar\\_t](#)
- typedef [matrix\\_multi](#)< [scalar\\_t](#) > [Clifford](#)

### Functions

- template<typename [Scalar\\_T](#) >  
[PyObject](#) \* [PyFloat\\_FromDouble](#) ([Scalar\\_T](#) v)
- template<typename [Index\\_Set\\_T](#) >  
[String](#) [index\\_set\\_to\\_repr](#) (const [Index\\_Set\\_T](#) &ist)  
*The "official" string representation of [Index\\_Set\\_T](#) ist.*
- template<typename [Index\\_Set\\_T](#) >  
[String](#) [index\\_set\\_to\\_str](#) (const [Index\\_Set\\_T](#) &ist)  
*The "informal" string representation of [Index\\_Set\\_T](#) ist.*
- template<typename [Multivector\\_T](#) >  
[String](#) [clifford\\_to\\_repr](#) (const [Multivector\\_T](#) &mv)

The "official" string representation of `Multivector_T` mv.

- template<typename `Multivector_T`>  
[String clifford\\_to\\_str](#) (const `Multivector_T` &mv)

The "informal" string representation of `Multivector_T` mv.

- template<typename `Multivector_T`>  
`Multivector_T` [cga3::cga3](#) (const `Multivector_T` &x)

Convert Euclidean 3D vector to Conformal Geometric Algebra null vector [DL (10.50)].

- template<typename `Multivector_T`>  
`Multivector_T` [cga3::cga3std](#) (const `Multivector_T` &X)

Convert CGA3 null vector to standard Conformal Geometric Algebra null vector [DL (10.52)].

- template<typename `Multivector_T`>  
`Multivector_T` [cga3::agc3](#) (const `Multivector_T` &X)

Convert CGA3 null vector to Euclidean 3D vector [DL (10.50)].

## Variables

- const [index\\_t lo\\_ndx](#) = DEFAULT\_LO
- const [index\\_t hi\\_ndx](#) = DEFAULT\_HI

### 7.27.1 Typedef Documentation

#### 7.27.1.1 Clifford

```
typedef matrix\_multi<scalar\_t> Clifford
```

Definition at line 160 of file `PyClical.h`.

#### 7.27.1.2 IndexSet

```
typedef index\_set<lo\_ndx,hi\_ndx> IndexSet
```

Definition at line 157 of file `PyClical.h`.

#### 7.27.1.3 scalar\_t

```
typedef double scalar\_t
```

Definition at line 159 of file `PyClical.h`.

#### 7.27.1.4 String

```
typedef std::string String
```

Definition at line 65 of file PyClical.h.

#### 7.27.1.5 Tune\_P

```
typedef glucat::tuning< glucat::DEFAULT_Mult_Matrix_Threshold, glucat::DEFAULT_Div_Max_Steps,
glucat::DEFAULT_Sqrt_Max_Steps, glucat::DEFAULT_Log_Max_Outer_Steps, glucat::DEFAULT_Log_Max_Inner_Steps,
glucat::DEFAULT_Basis_Max_Count, glucat::DEFAULT_Fast_Size_Threshold, glucat::DEFAULT_Inv_Fast_Dim_Threshold,
glucat::DEFAULT_Products_Size_Threshold, glucat::precision_promoted > Tune_P
```

Definition at line 49 of file PyClical.h.

### 7.27.2 Function Documentation

#### 7.27.2.1 clifford\_to\_repr()

```
template<typename Multivector_T >
String clifford_to_repr (
    const Multivector_T & mv ) [inline]
```

The "official" string representation of Multivector\_T mv.

Definition at line 87 of file PyClical.h.

Referenced by PyClical.clifford::\_\_repr\_\_().

#### 7.27.2.2 clifford\_to\_str()

```
template<typename Multivector_T >
String clifford_to_str (
    const Multivector_T & mv ) [inline]
```

The "informal" string representation of Multivector\_T mv.

Definition at line 98 of file PyClical.h.

References glucat::abs(), and PyClical::e().

Referenced by PyClical.clifford::\_\_str\_\_().

### 7.27.2.3 index\_set\_to\_repr()

```
template<typename Index_Set_T >
String index_set_to_repr (
    const Index_Set_T & ist ) [inline]
```

The "official" string representation of Index\_Set\_T ist.

Definition at line 69 of file PyClical.h.

References PyClical::ist.

Referenced by PyClical.index\_set::\_\_repr\_\_().

### 7.27.2.4 index\_set\_to\_str()

```
template<typename Index_Set_T >
String index_set_to_str (
    const Index_Set_T & ist ) [inline]
```

The "informal" string representation of Index\_Set\_T ist.

Definition at line 78 of file PyClical.h.

References PyClical::ist.

Referenced by PyClical.index\_set::\_\_str\_\_().

### 7.27.2.5 PyFloat\_FromDouble()

```
template<typename Scalar_T >
PyObject* PyFloat_FromDouble (
    Scalar_T v ) [inline]
```

Create a PyFloatObject object from Scalar\_T v. Needed because Scalar\_T might not be the same as double.

Definition at line 59 of file PyClical.h.

## 7.27.3 Variable Documentation

### 7.27.3.1 hi\_ndx

```
const index_t hi_ndx = DEFAULT_HI
```

Definition at line 156 of file PyClical.h.

### 7.27.3.2 lo\_ndx

```
const index_t lo_ndx = DEFAULT_LO
```

Definition at line 155 of file PyClical.h.

## 7.28 pyclical/PyClical.pxd File Reference

### Namespaces

- [PyClical](#)

## 7.29 pyclical/PyClical.pyx File Reference

### Classes

- class [PyClical.index\\_set](#)
- class [PyClical.index\\_set](#)
- class [PyClical.clifford](#)
- class [PyClical.clifford](#)

### Namespaces

- [PyClical](#)

### Functions

- def [PyClical.index\\_set\\_hidden\\_doctests](#) ()
- def [PyClical.clifford\\_hidden\\_doctests](#) ()
- def [PyClical.e](#) (obj)
- def [PyClical.istpq](#) (p, q)
- def [PyClical.\\_test](#) ()

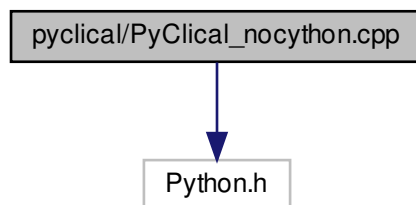
### Variables

- string [PyClical.\\_\\_version\\_\\_](#) = "0.8.2"
- [PyClical.obj](#)
- [PyClical.i](#)
- [PyClical.ixt](#)
- [PyClical.fill](#)
- float [PyClical.tau](#) = atan(clifford(1.0)) \* 8.0
- float [PyClical.pi](#) = tau / 2.0
- [PyClical.cl](#) = clifford
- [PyClical.ist](#) = index\_set
- def [PyClical.ninf3](#) = e(4) + e(-1)
- def [PyClical.nbar3](#) = e(4) - e(-1)

## 7.30 pyclical/PyClical\_nocython.cpp File Reference

```
#include "Python.h"
```

Include dependency graph for PyClical\_nocython.cpp:



### Macros

- `#define PY_SSIZE_T_CLEAN`

#### 7.30.1 Macro Definition Documentation

##### 7.30.1.1 PY\_SSIZE\_T\_CLEAN

```
#define PY_SSIZE_T_CLEAN
```

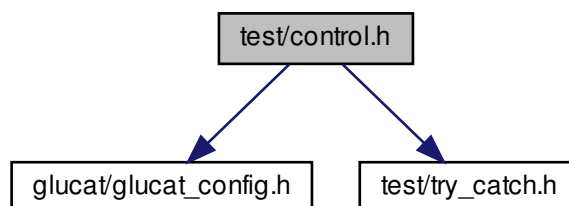
Definition at line 52 of file PyClical\_nocython.cpp.

## 7.31 test/control.h File Reference

```
#include "glucat/glucat_config.h"
```

```
#include "test/try_catch.h"
```

Include dependency graph for control.h:





## Functions

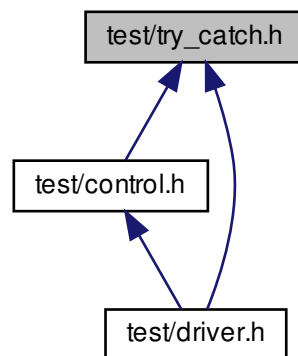
- static double `glucat::timing::elapsed` (clock\_t cpu\_time)  
*Elapsed time in milliseconds.*

## Variables

- const double `glucat::timing::MS_PER_SEC` = 1000.0  
*Timing constant: milliseconds per second.*
- const double `glucat::timing::MS_PER_CLOCK` = MS\_PER\_SEC / double(CLOCKS\_PER\_SEC)  
*Timing constant: milliseconds per clock.*
- const int `glucat::timing::EXTRA_TRIALS` = 2  
*Timing constant: trial expansion factor.*

## 7.34 test/try\_catch.h File Reference

This graph shows which files directly or indirectly include this file:



## Namespaces

- `glucat`

## Typedefs

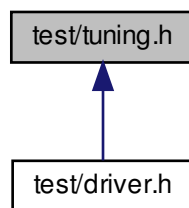
- typedef int(\* `glucat::intfn`) ()  
*For exception catching: pointer to function returning int.*
- typedef int(\* `glucat::intintfn`) (int)  
*For exception catching: pointer to function of int returning int.*

## Functions

- int [glucat::try\\_catch](#) (intfn f)  
*Exception catching for functions returning int.*
- int [glucat::try\\_catch](#) (intintfn f, int arg)  
*Exception catching for functions of int returning int.*

## 7.35 test/tuning.h File Reference

This graph shows which files directly or indirectly include this file:



## Macros

- `#define \_\_TEST\_TUNING\_DEFAULT\_CONSTANT(SUFFIX) const unsigned int Test_Tuning_##SUFFIX = glucat::DEFAULT_##SUFFIX`

## Typedefs

- typedef [glucat::precision\\_t](#) [precision\\_t](#)
- typedef [glucat::tuning](#) < Test\_Tuning\_Mult\_Matrix\_Threshold, Test\_Tuning\_Div\_Max\_Steps, Test\_Tuning\_Sqrt\_Max\_Steps, Test\_Tuning\_Log\_Max\_Outer\_Steps, Test\_Tuning\_Log\_Max\_Inner\_Steps, Test\_Tuning\_Basis\_Max\_Count, Test\_Tuning\_Fast\_Size\_Threshold, Test\_Tuning\_Inv\_Fast\_Dim\_Threshold, Test\_Tuning\_Products\_Size\_Threshold, [Test\\_Tuning\\_Function\\_Precision](#) > [Tune\\_P](#)  
*Tuning policy.*

## Functions

- [\\_GLUCAT\\_CTAssert](#) (std::numeric\_limits< unsigned int >::radix==2, CannotSetThresholds) const unsigned int Test\_Tuning\_Int\_Digits
- [\\_\\_TEST\\_TUNING\\_DEFAULT\\_CONSTANT](#) (Mult\_Matrix\_Threshold)
- [\\_\\_TEST\\_TUNING\\_DEFAULT\\_CONSTANT](#) (Div\_Max\_Steps)
- [\\_\\_TEST\\_TUNING\\_DEFAULT\\_CONSTANT](#) (Sqrt\_Max\_Steps)
- [\\_\\_TEST\\_TUNING\\_DEFAULT\\_CONSTANT](#) (Log\_Max\_Outer\_Steps)
- [\\_\\_TEST\\_TUNING\\_DEFAULT\\_CONSTANT](#) (Log\_Max\_Inner\_Steps)
- [\\_\\_TEST\\_TUNING\\_DEFAULT\\_CONSTANT](#) (Basis\_Max\_Count)
- [\\_\\_TEST\\_TUNING\\_DEFAULT\\_CONSTANT](#) (Fast\_Size\_Threshold)
- [\\_\\_TEST\\_TUNING\\_DEFAULT\\_CONSTANT](#) (Inv\_Fast\_Dim\_Threshold)
- [\\_\\_TEST\\_TUNING\\_DEFAULT\\_CONSTANT](#) (Products\_Size\_Threshold)

## Variables

- const unsigned int `Test_Tuning_Max_Threshold` = 1 << `Test_Tuning_Int_Digits`
- const `precision_t` `Test_Tuning_Function_Precision` = `glucat::DEFAULT_Function_Precision`

## 7.35.1 Macro Definition Documentation

### 7.35.1.1 \_\_TEST\_TUNING\_DEFAULT\_CONSTANT

```
#define __TEST_TUNING_DEFAULT_CONSTANT(  
    SUFFIX ) const unsigned int Test_Tuning_##SUFFIX = glucat::DEFAULT_##SUFFIX
```

Definition at line 41 of file `tuning.h`.

## 7.35.2 Typedef Documentation

### 7.35.2.1 precision\_t

```
typedef glucat::precision_t precision_t
```

Definition at line 39 of file `tuning.h`.

### 7.35.2.2 Tune\_P

```
typedef glucat::tuning< Test_Tuning_Mult_Matrix_Threshold, Test_Tuning_Div_Max_Steps, Test_↵  
_Tuning_Sqrt_Max_Steps, Test_Tuning_Log_Max_Outer_Steps, Test_Tuning_Log_Max_Inner_Steps,  
Test_Tuning_Basis_Max_Count, Test_Tuning_Fast_Size_Threshold, Test_Tuning_Inv_Fast_Dim_↵  
Threshold, Test_Tuning_Products_Size_Threshold, Test_Tuning_Function_Precision > Tune_P
```

Tuning policy.

Definition at line 126 of file `tuning.h`.

## 7.35.3 Function Documentation

**7.35.3.1** `__TEST_TUNING_DEFAULT_CONSTANT()` [1/9]

```
__TEST_TUNING_DEFAULT_CONSTANT (
    Mult_Matrix_Threshold )
```

**7.35.3.2** `__TEST_TUNING_DEFAULT_CONSTANT()` [2/9]

```
__TEST_TUNING_DEFAULT_CONSTANT (
    Div_Max_Steps )
```

**7.35.3.3** `__TEST_TUNING_DEFAULT_CONSTANT()` [3/9]

```
__TEST_TUNING_DEFAULT_CONSTANT (
    Sqrt_Max_Steps )
```

**7.35.3.4** `__TEST_TUNING_DEFAULT_CONSTANT()` [4/9]

```
__TEST_TUNING_DEFAULT_CONSTANT (
    Log_Max_Outer_Steps )
```

**7.35.3.5** `__TEST_TUNING_DEFAULT_CONSTANT()` [5/9]

```
__TEST_TUNING_DEFAULT_CONSTANT (
    Log_Max_Inner_Steps )
```

**7.35.3.6** `__TEST_TUNING_DEFAULT_CONSTANT()` [6/9]

```
__TEST_TUNING_DEFAULT_CONSTANT (
    Basis_Max_Count )
```

**7.35.3.7** `__TEST_TUNING_DEFAULT_CONSTANT()` [7/9]

```
__TEST_TUNING_DEFAULT_CONSTANT (
    Fast_Size_Threshold )
```

7.35.3.8 `__TEST_TUNING_DEFAULT_CONSTANT()` [8/9]

```
__TEST_TUNING_DEFAULT_CONSTANT (
    Inv_Fast_Dim_Threshold )
```

7.35.3.9 `__TEST_TUNING_DEFAULT_CONSTANT()` [9/9]

```
__TEST_TUNING_DEFAULT_CONSTANT (
    Products_Size_Threshold )
```

7.35.3.10 `_GLUCAT_CTAssert()`

```
_GLUCAT_CTAssert (
    std::numeric_limits< unsigned int >::radix  = 2,
    CannotSetThresholds ) const
```

## 7.35.4 Variable Documentation

7.35.4.1 `Test_Tuning_Function_Precision`

```
const precision_t Test_Tuning_Function_Precision = glucat::DEFAULT_Function_Precision
```

Definition at line 110 of file tuning.h.

7.35.4.2 `Test_Tuning_Max_Threshold`

```
const unsigned int Test_Tuning_Max_Threshold = 1 << Test_Tuning_Int_Digits
```

Definition at line 37 of file tuning.h.

## 7.36 test/undefine.h File Reference



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